



12

Thick lens

Martin Murin

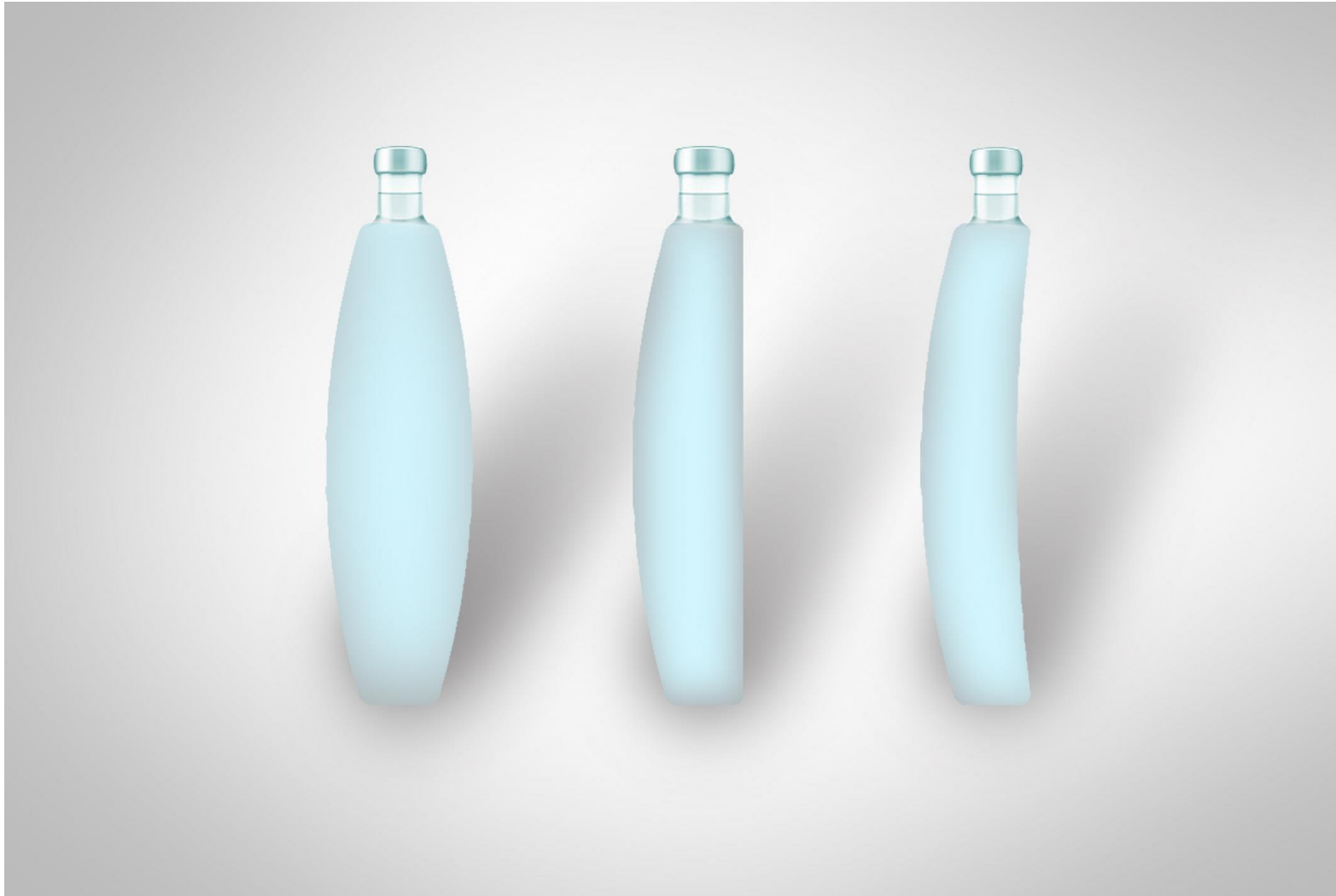


12. Thick Lens:

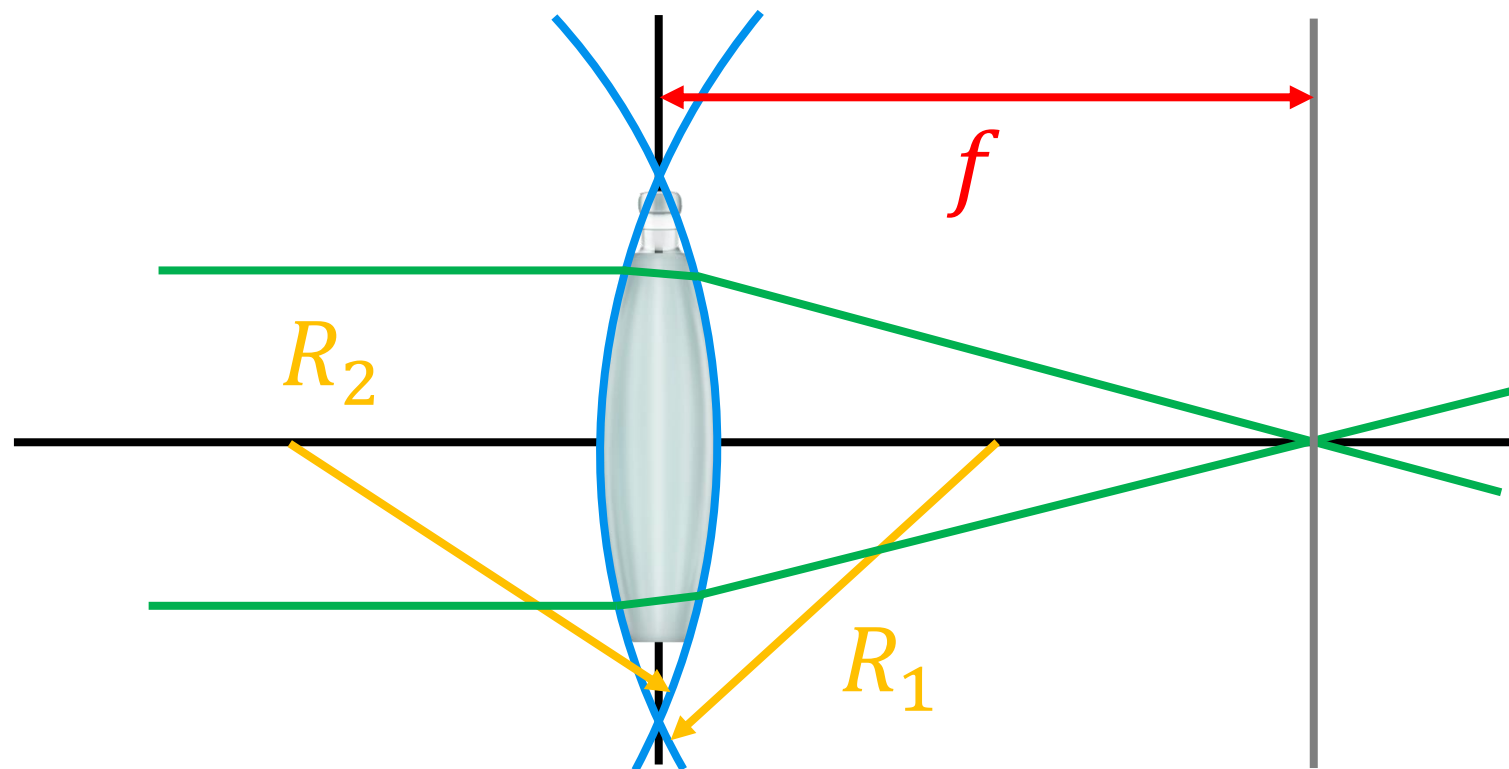
“A bottle filled with a liquid can work as a lens. Arguably, such a bottle is dangerous if left on a table on a sunny day.

Can one use such a ‘lens’ to scorch a surface?”

Bottle as a thick lens



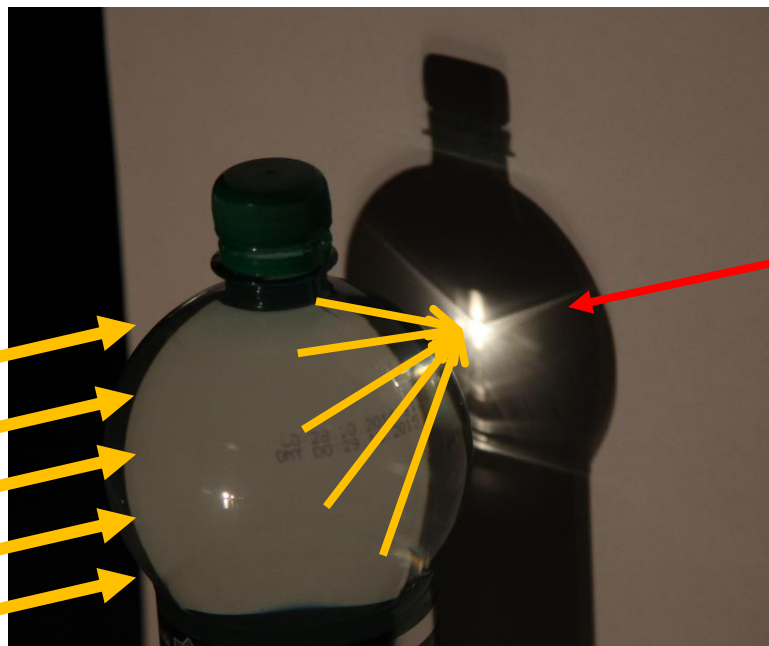
Bottle as a thick lens



How it works

incoming light

I_0

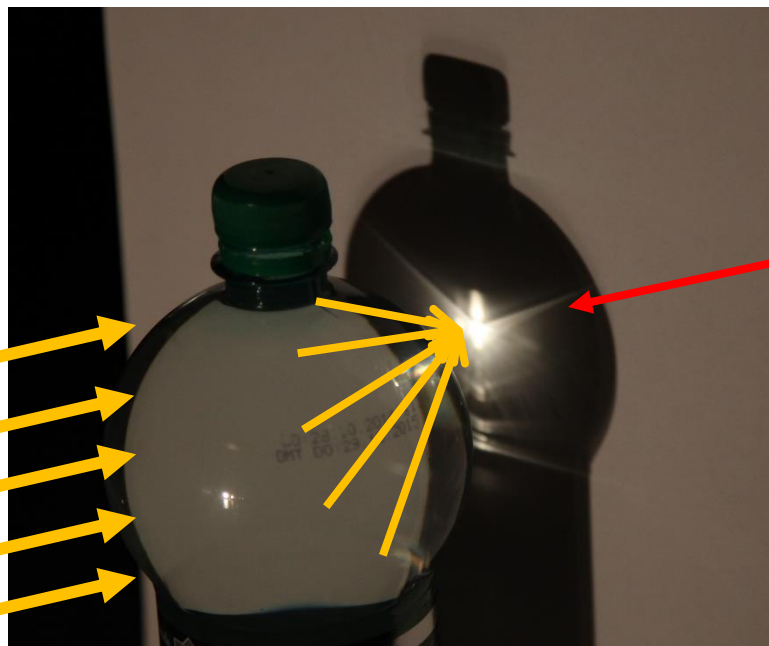


Concentrated light
= power

How it works

incoming light

I_0



**Concentrated light
= power**

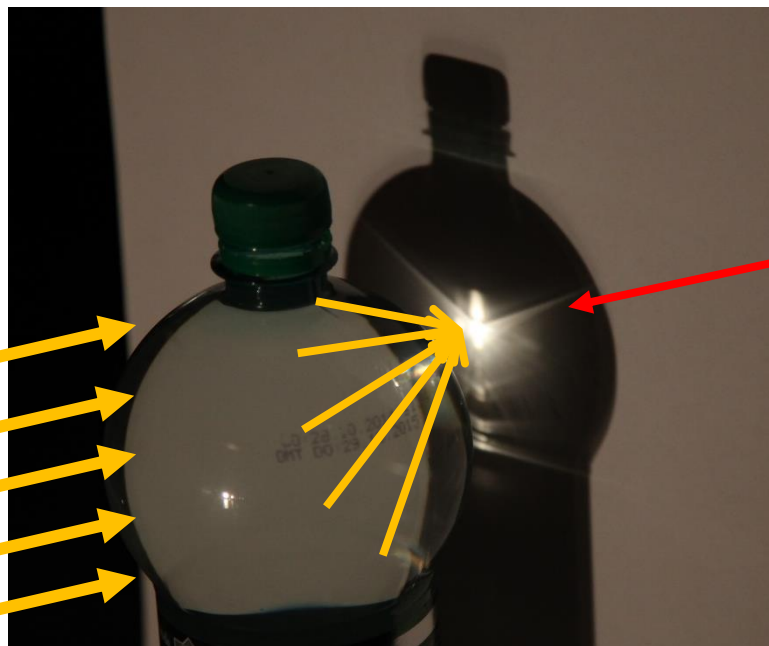


Material heats up

How it works

incoming light

I_0



**Concentrated light
= power**



Material heats up

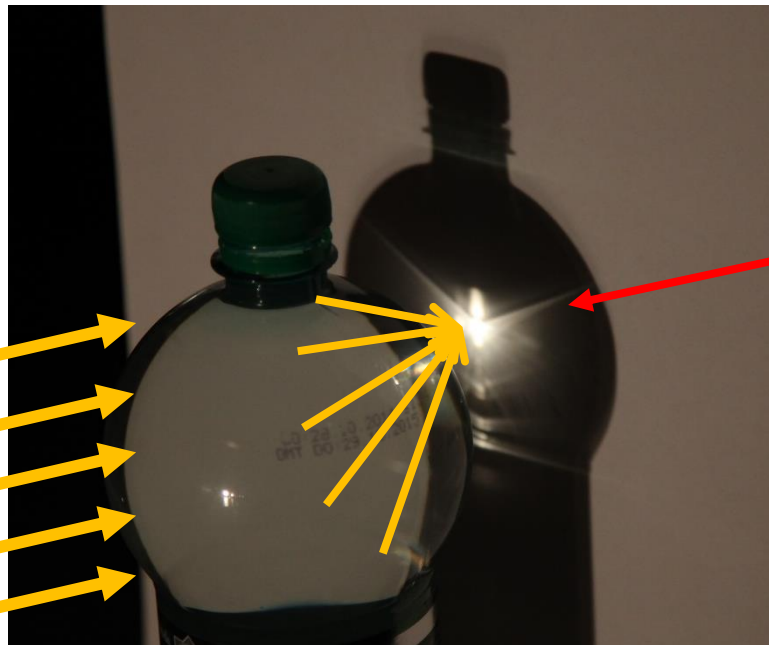


Ignition

How it works

incoming light

I_0



**Concentrated light
= power**



Material heats up



Ignition

Section 1

Light passing through the bottle
Intensity of incident light

Section 2

Energy of light
Reflection, absorption, dissipation

Different shapes of bottles



Undefined
shape



Cylinder

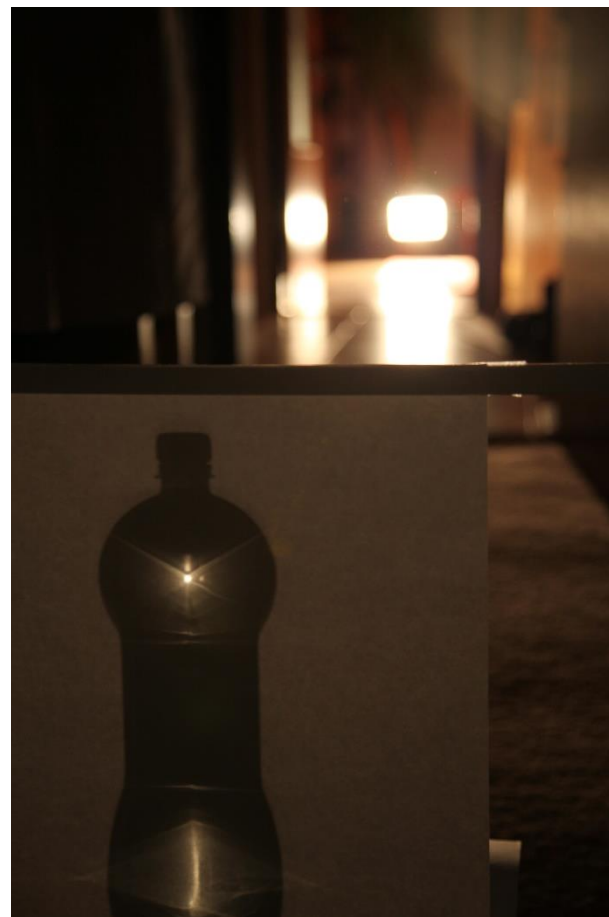
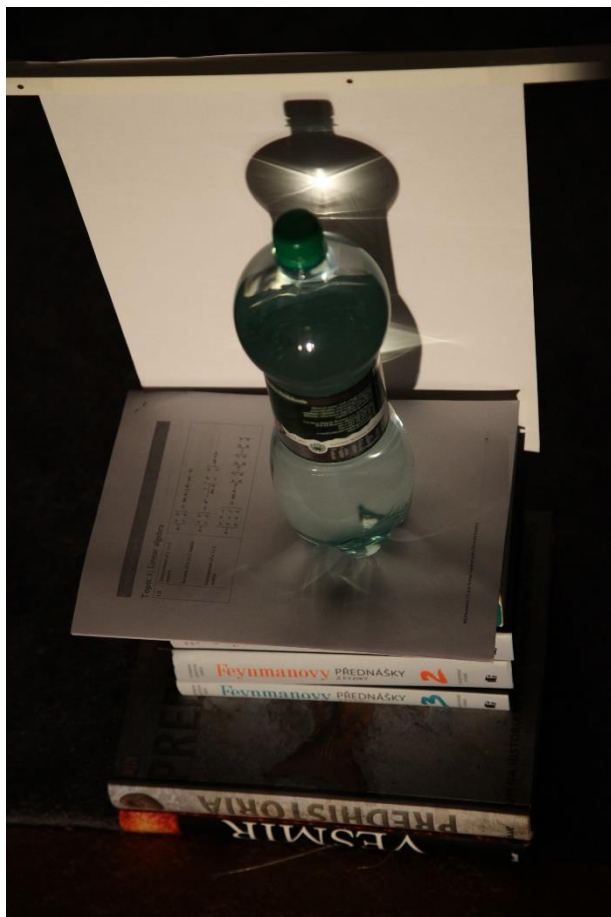


Top view:

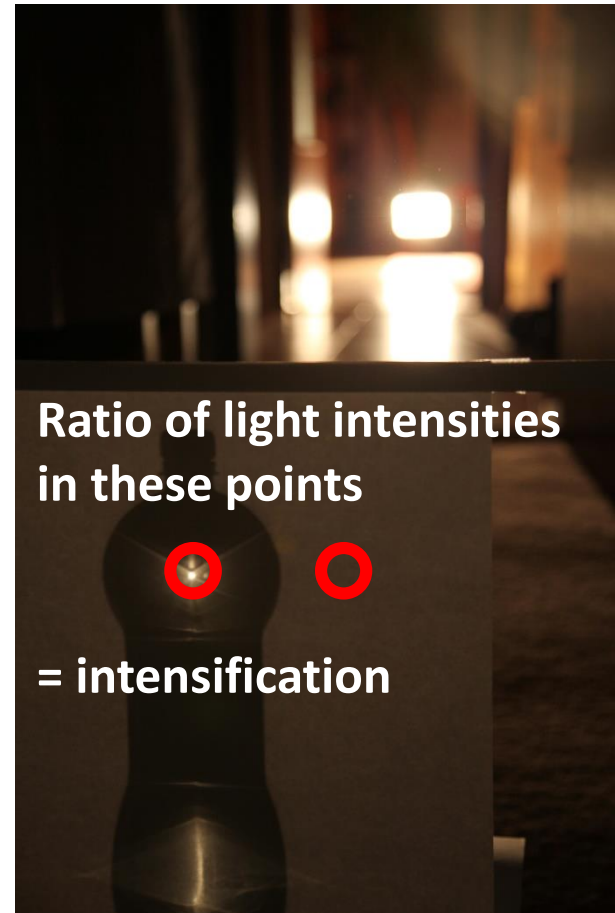
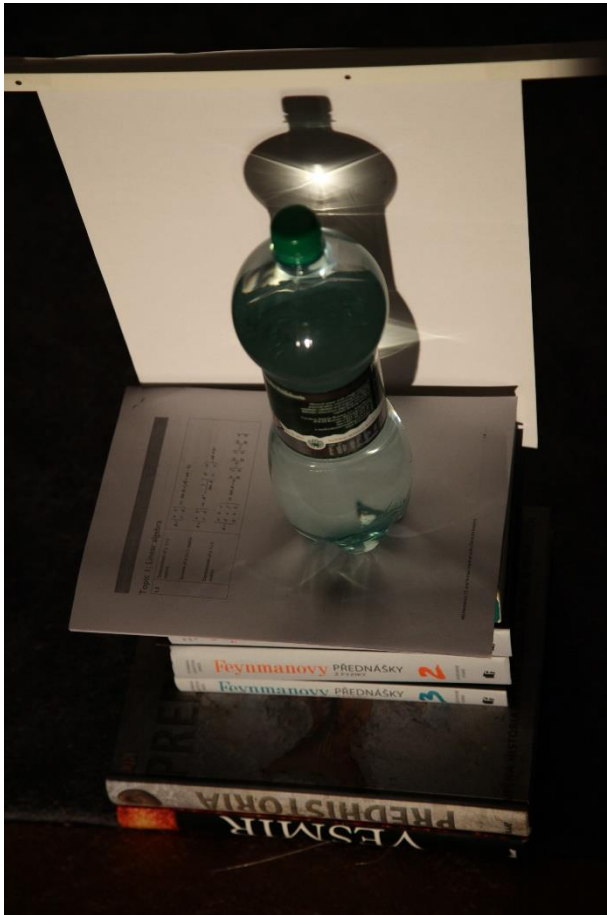


Sphere

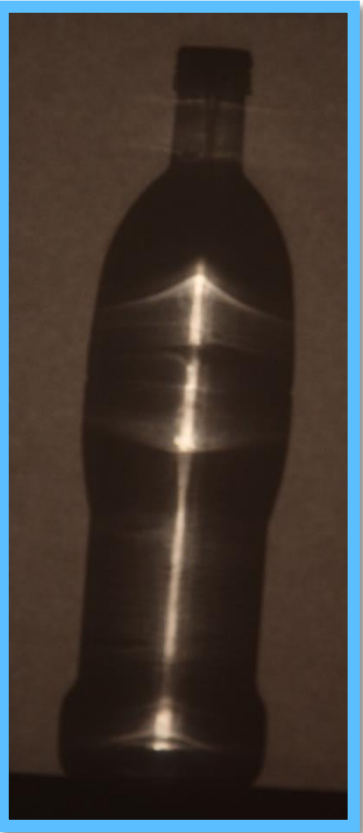
Intensification of light - experiment



Intensification of light - experiment



Patterns and intensifications observed



Patterns and intensifications observed



5x

Patterns and intensifications observed

undefined
focus



5x

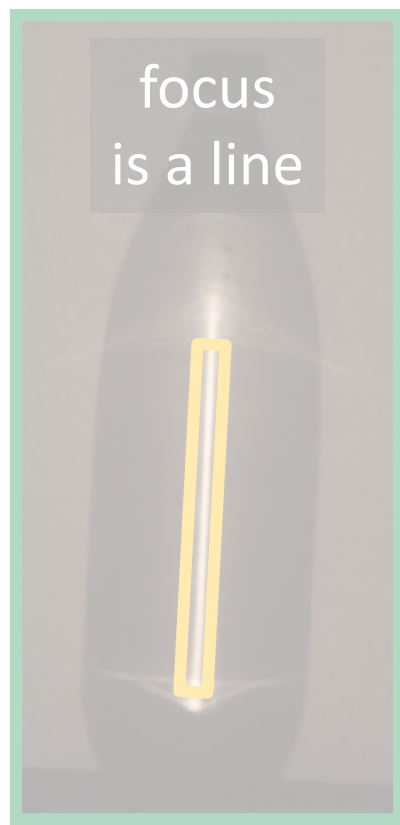
Patterns and intensifications observed



5x

5x

Patterns and intensifications observed



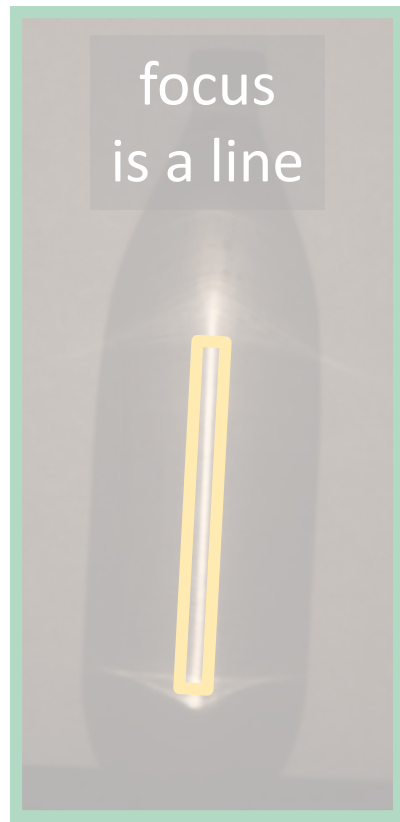
5x

5x

Patterns and intensifications observed



5x

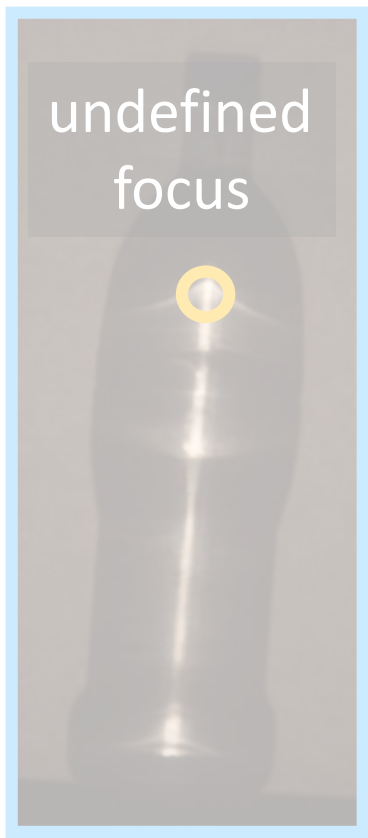


5x

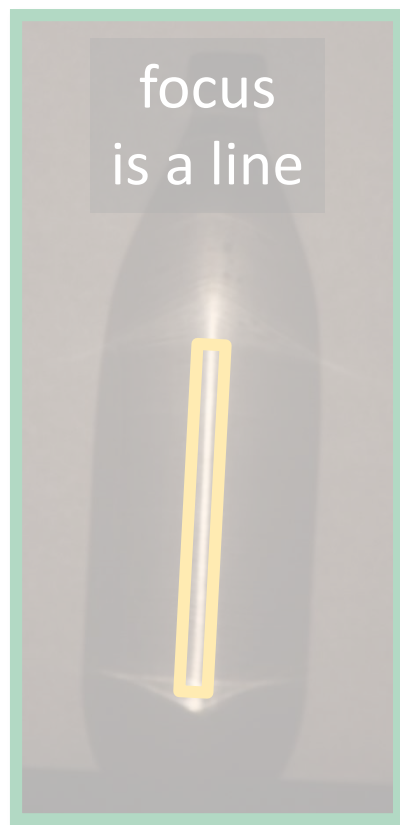


25x

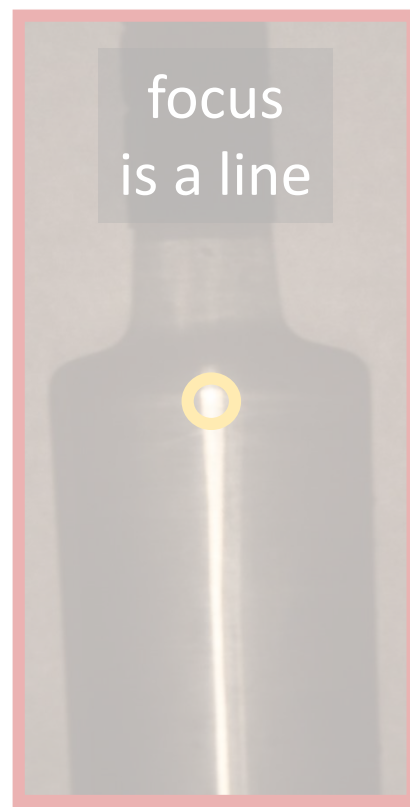
Patterns and intensifications observed



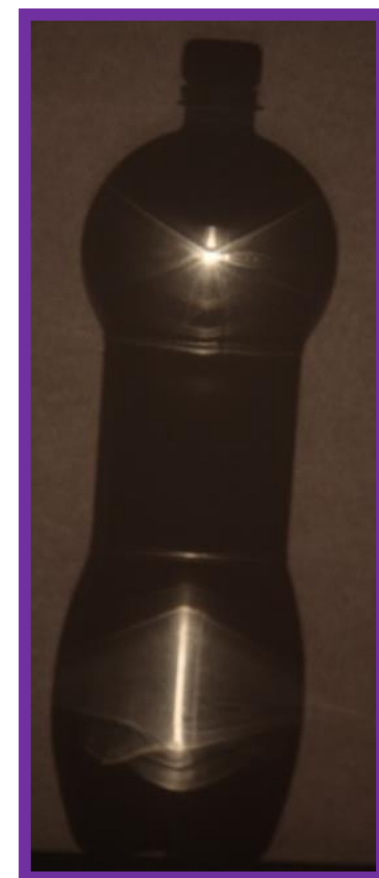
5x



5x



25x



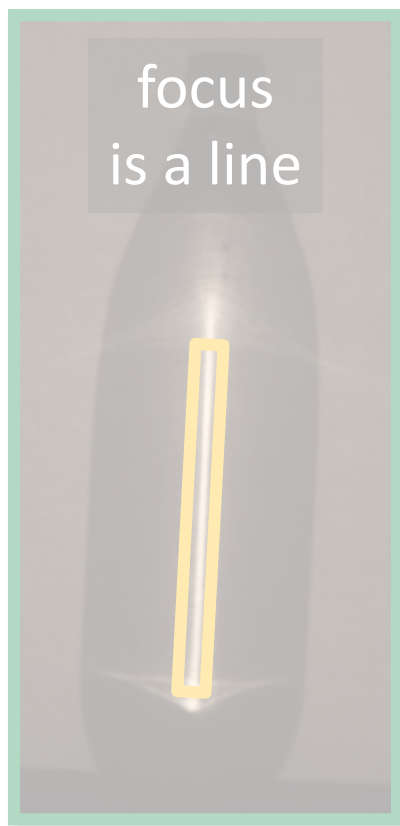
Patterns and intensifications observed

undefined
focus



5x

focus
is a line



5x

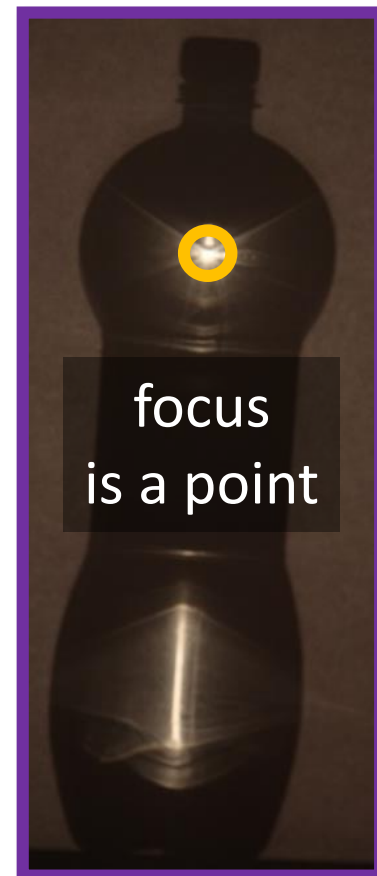
focus
is a line



25x

1500x

focus
is a point



Patterns and intensifications observed

1500x

undefined
focus

focus
is a line

focus
is a line

Spherical bottle is the most dangerous

is a point

5x

5x

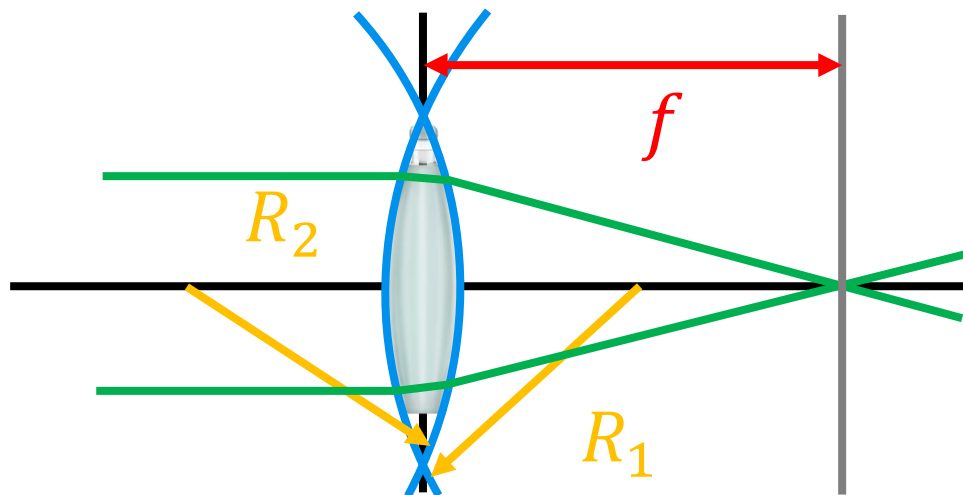
25x

Section 1:

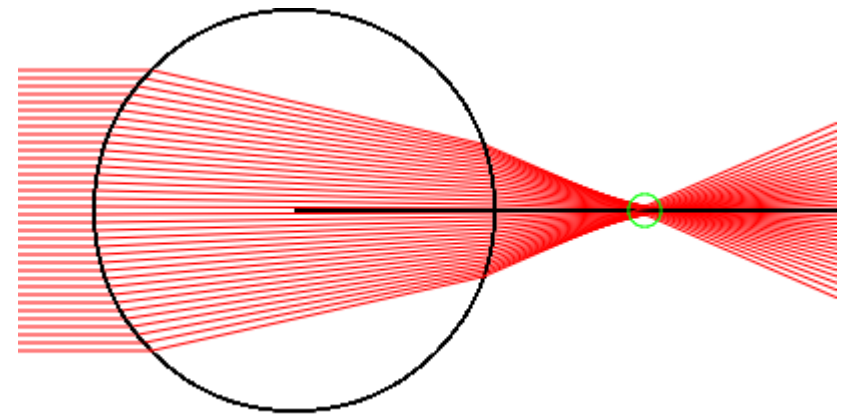
Theoretical estimate of intensification

Two theoretical models

Geometrical model



Numerical ray tracing

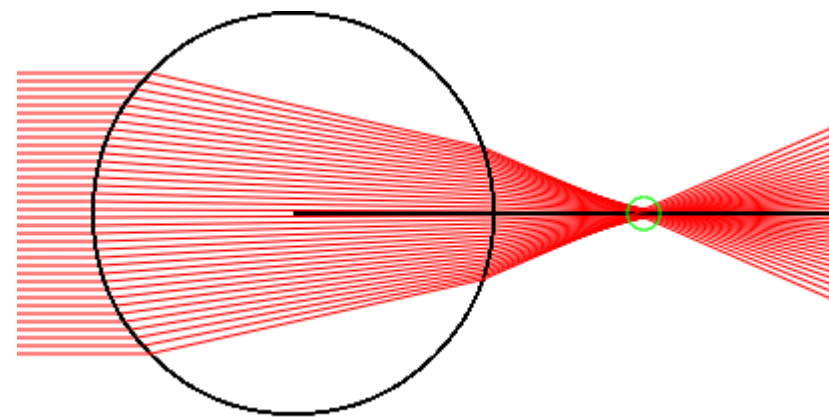
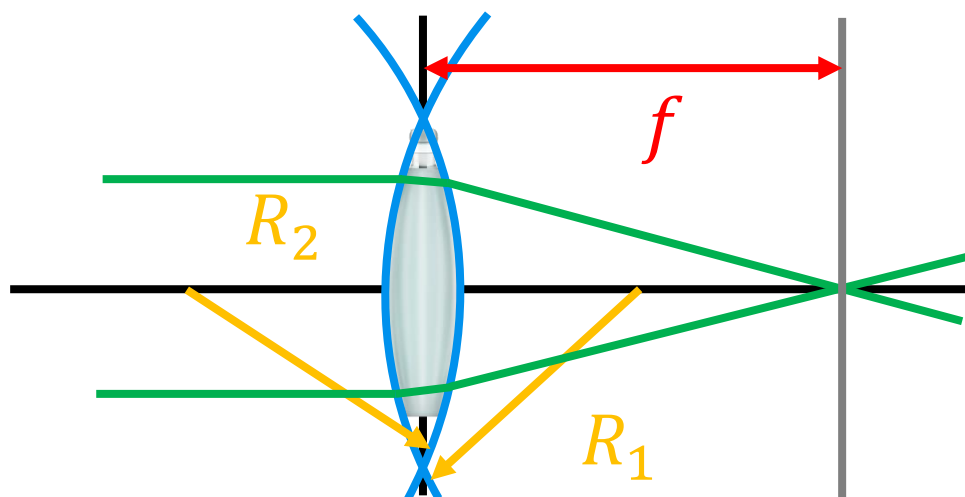


Section 1:

Theoretical estimate of intensification

Two theoretical models

Geometrical model  Numerical ray tracing





GEOMETRICAL MODEL



Focus of a sphere

“Lensmaker’s equation”

$$\frac{1}{f} = (n - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} + \frac{(n - 1)d}{nR_1R_2} \right]$$



Focus of a sphere

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(For a sphere: $R_2 = -R_1 = -R$ $d = 2R$)

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(For a sphere: $R_2 = -R_1 = -R$ $d = 2R$)

$$f = \frac{nR}{2n - 2} \longrightarrow \text{For water } n = 1.33 \approx \frac{4}{3} \longrightarrow f = 2R$$

Focus of a sphere

“Lensmaker’s equation”

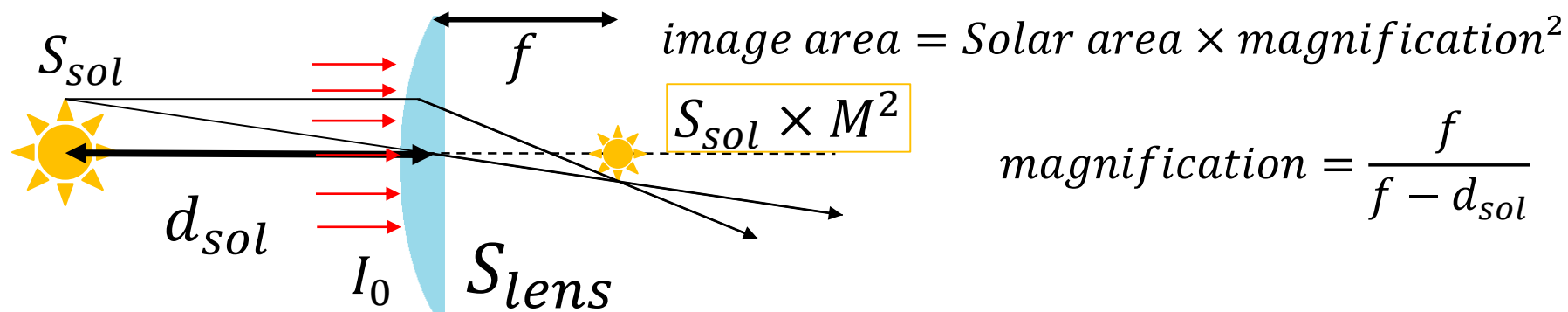
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EXPERIMENTALLY CONFIRMED

Maximum achievable intensity?



Maximum achievable intensity?

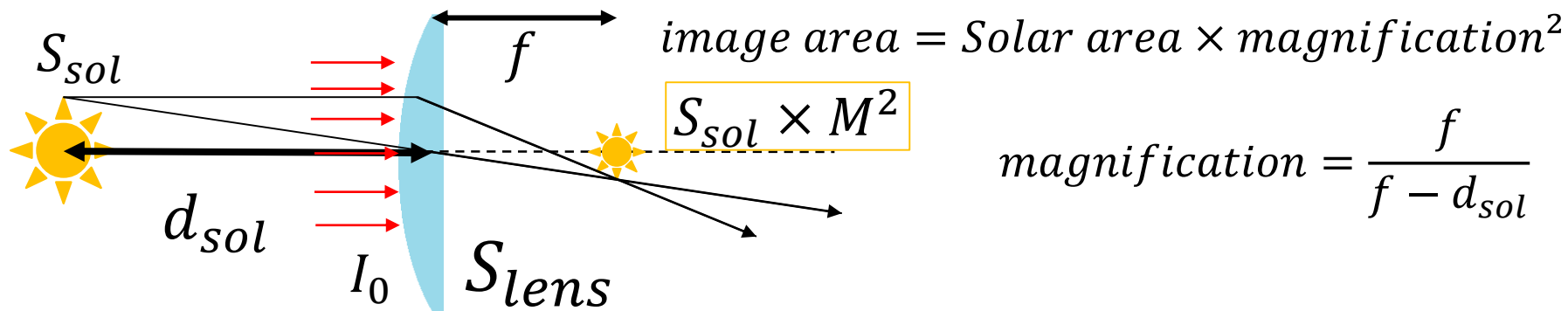


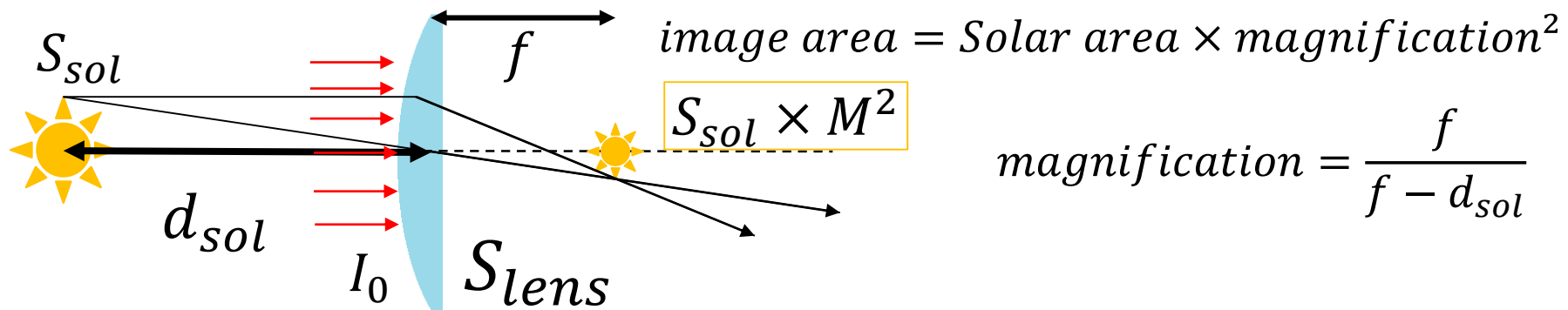
image area = Solar area \times magnification²

$$\text{magnification} = \frac{f}{f - d_{sol}}$$

(power is conserved)

$$I = k I_0 \frac{S_{lens}}{S_{sol} M^2}$$

Maximum achievable intensity?

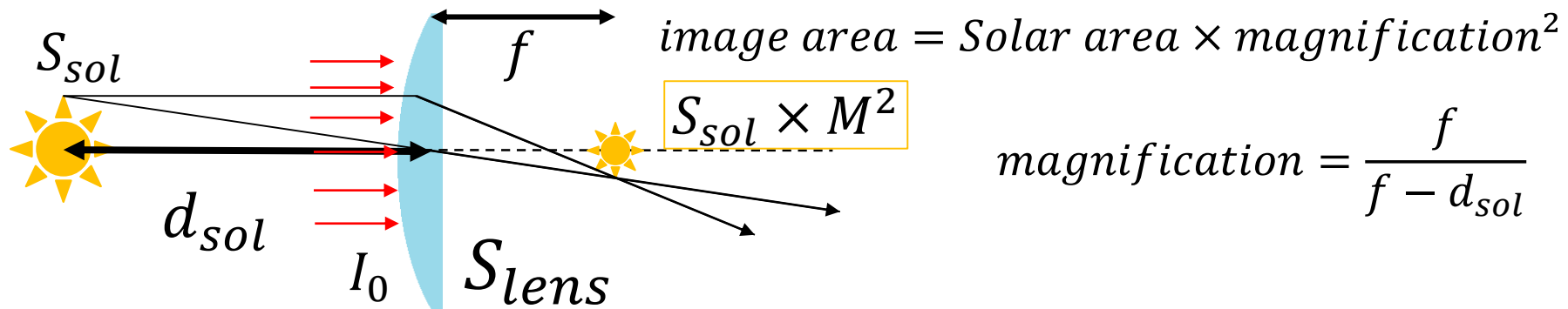


(power is conserved)

$$I = k I_0 \frac{S_{lens}}{S_{sol} M^2}$$

$$I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$

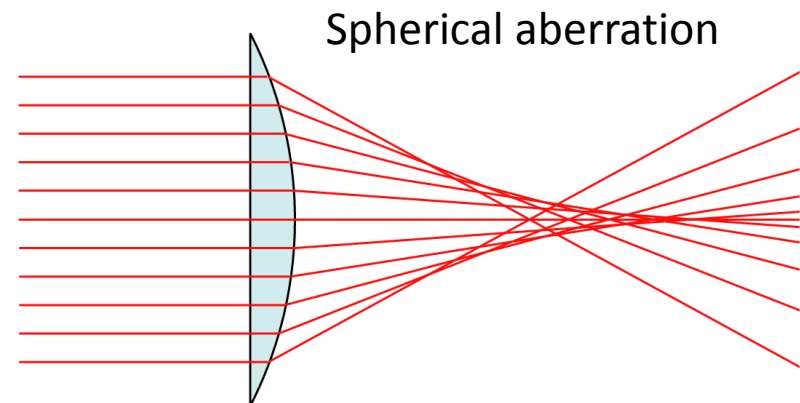
Maximum achievable intensity?



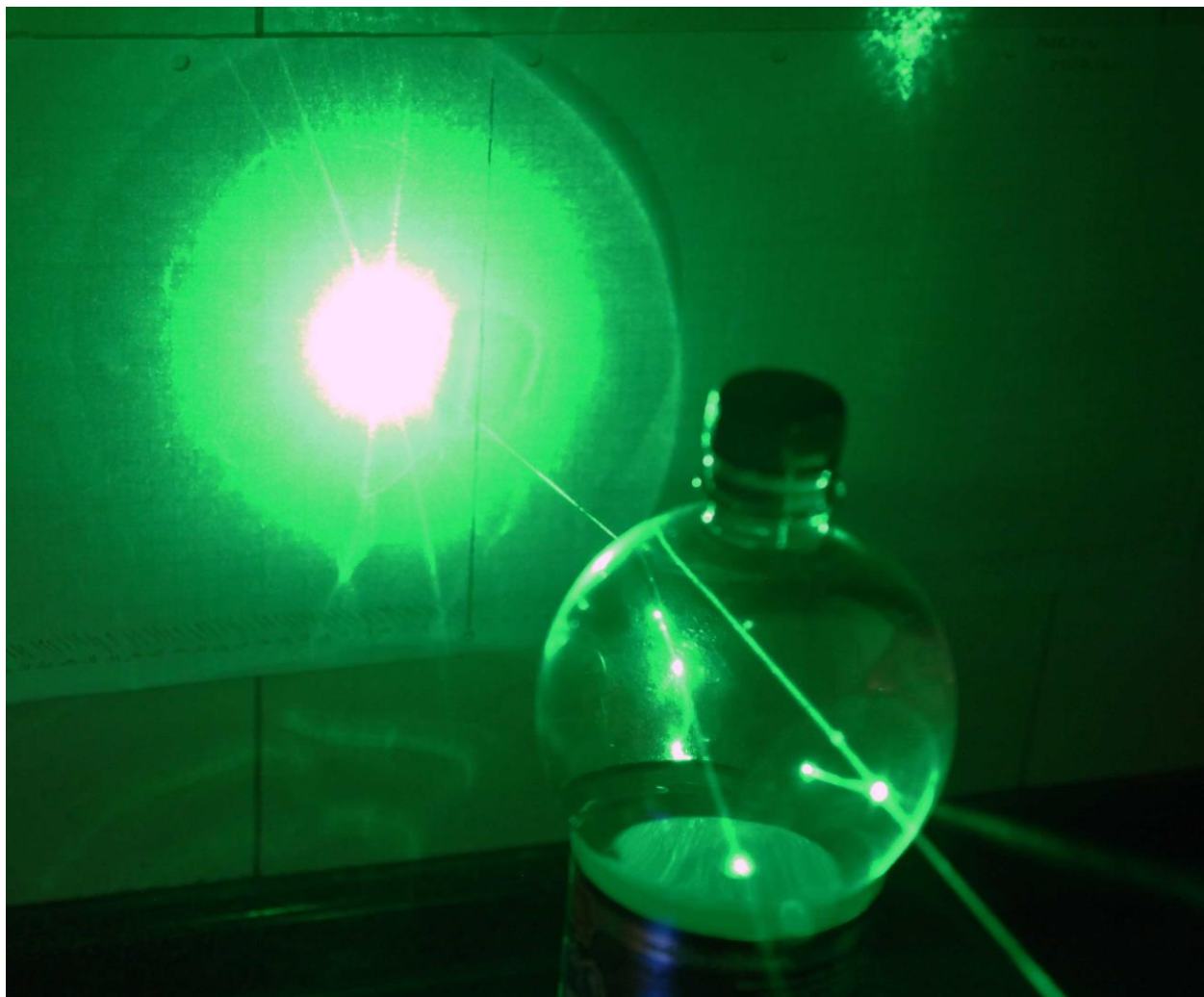
(power is conserved)

$$I = k I_0 \frac{S_{lens}}{S_{sol} M^2}$$

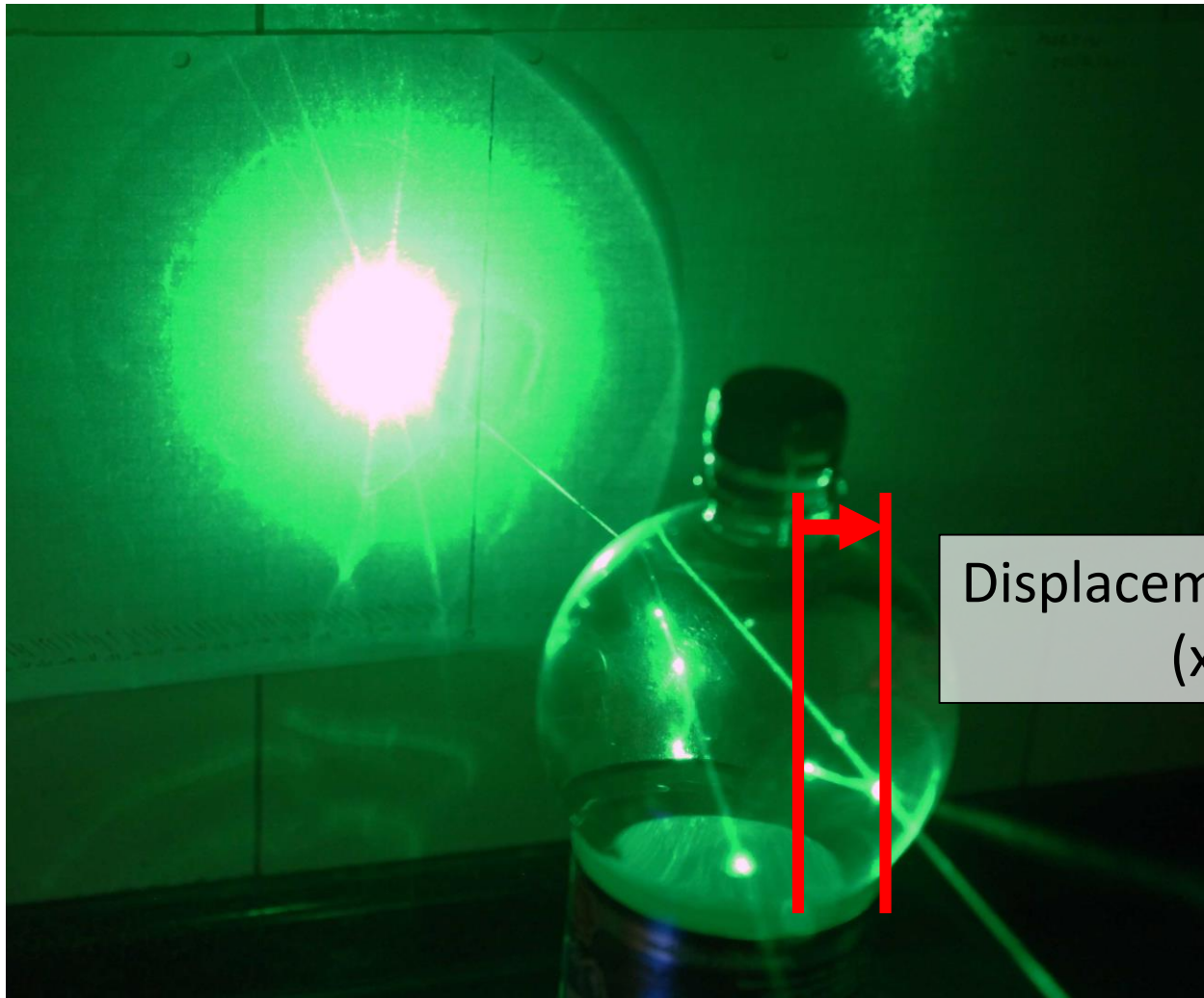
$$I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$



ABERRATION EXPERIMENT

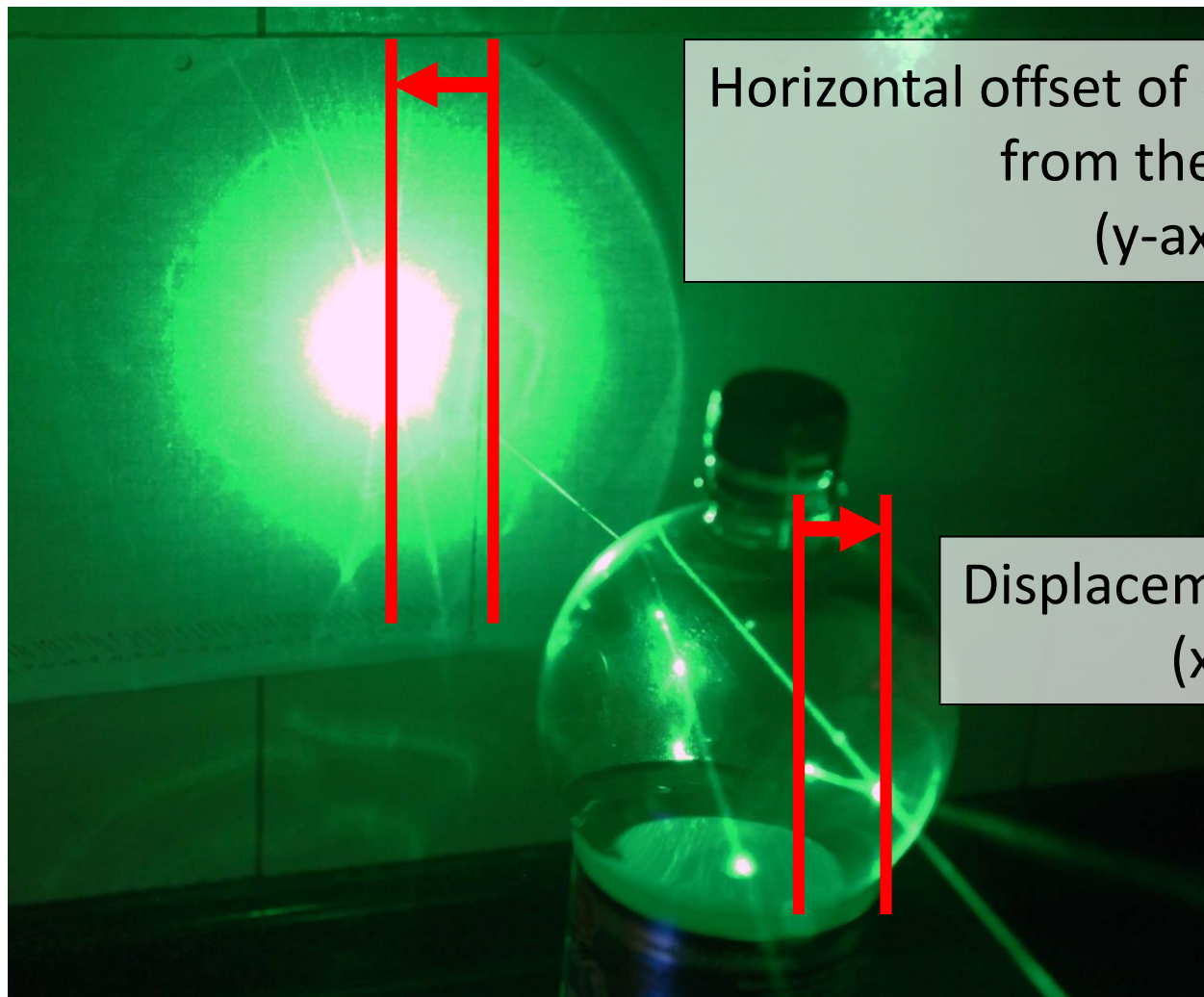


ABERRATION EXPERIMENT



Displacement of the ray
(x-axis)

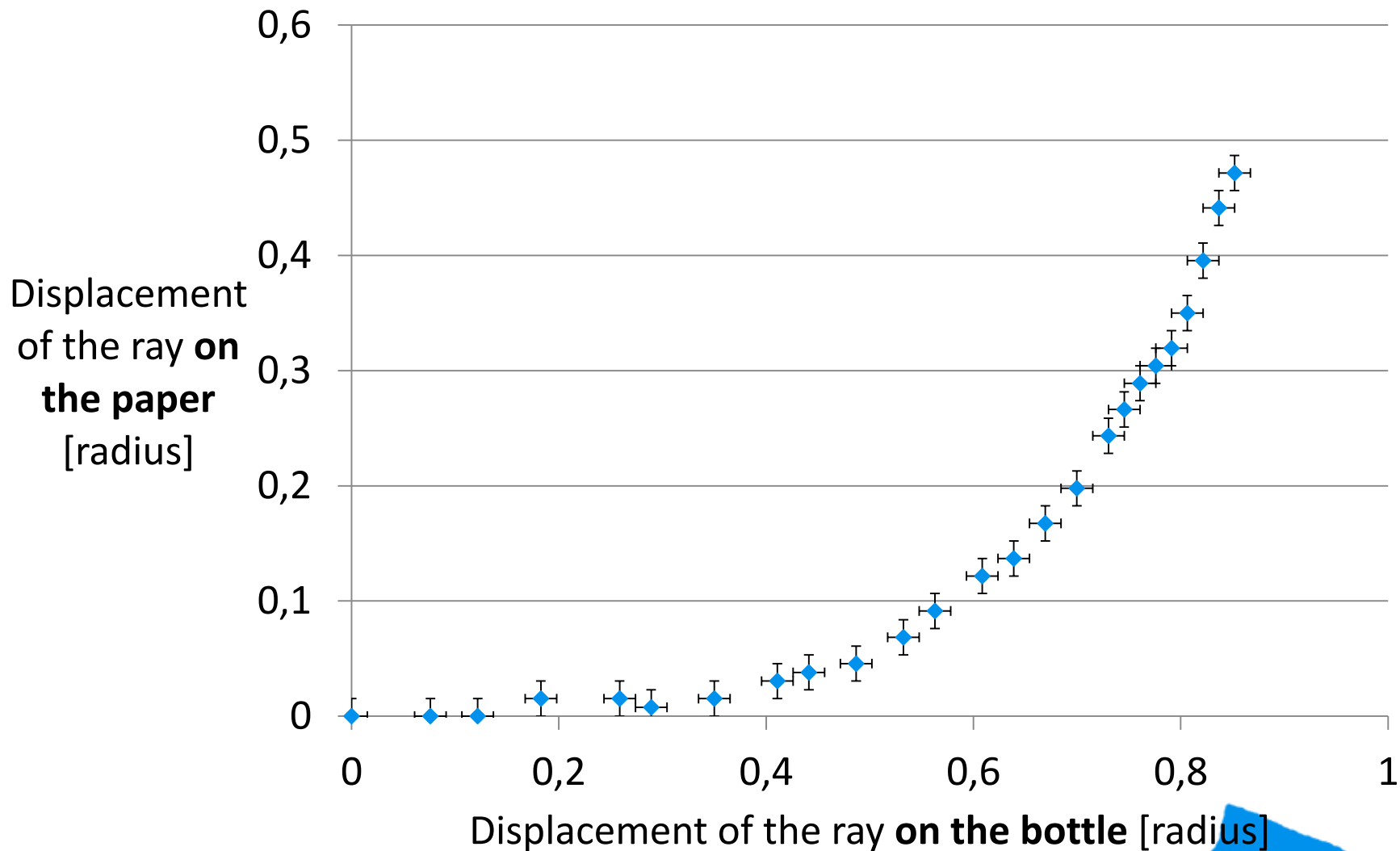
ABERRATION EXPERIMENT



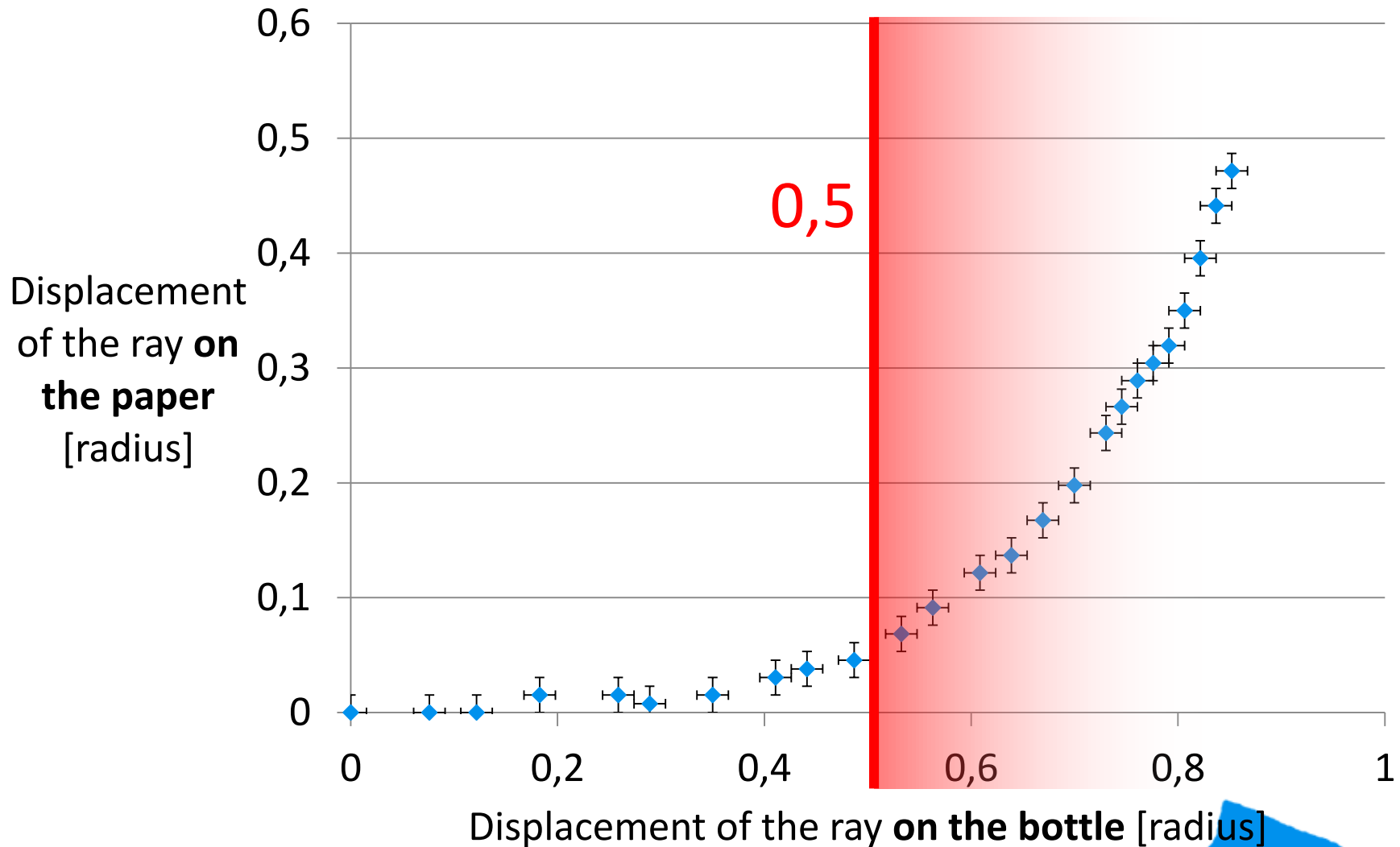
Horizontal offset of concentrated light
from the focus
(y-axis)

Displacement of the ray
(x-axis)

Effective area – ABERRATION EXPERIMENT



Effective area – ABERRATION EXPERIMENT





Theoretical prediction of maximal intensity

$$I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$

$$I = k I_0 \frac{\frac{\pi R^2}{4}}{S_{sol}} \frac{d_{sol}^2}{4R^2} \quad \frac{d_{sol}^2}{S_{sol}} \cong 14000$$



Theoretical prediction of maximal intensity

$$I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$

$$I = k I_0 \frac{\frac{\pi R^2}{4}}{S_{sol}} \frac{d_{sol}^2}{4R^2} \quad \frac{d_{sol}^2}{S_{sol}} \cong 14000$$

$$I = k \frac{14000\pi}{16} I_0 \cong 2750k I_0$$

Comparison with the experiment



$$I = k \frac{14000\pi}{16} I_0 \cong 2750k I_0$$

Permeability constant includes

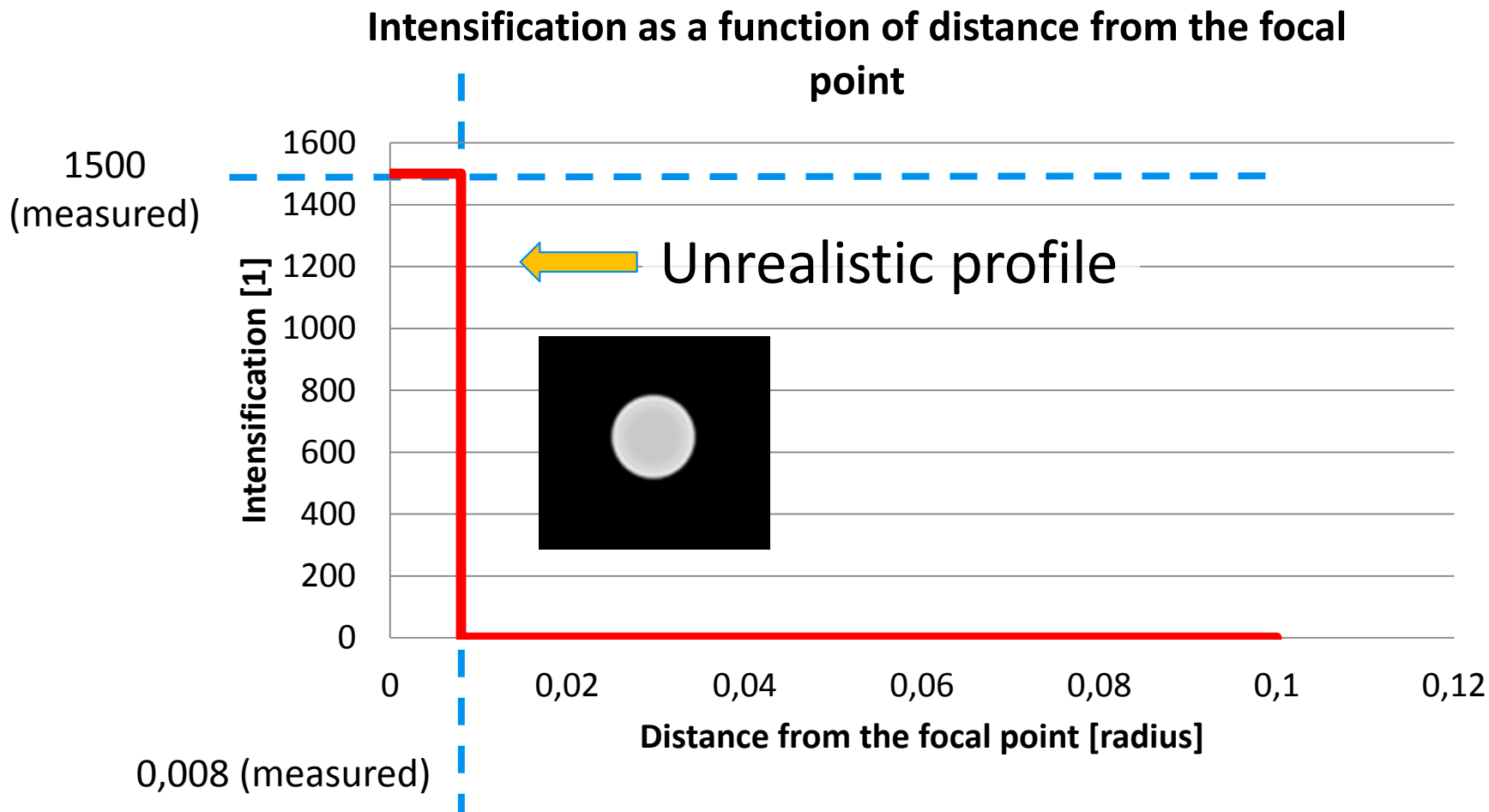
- Reflection on plastics-air interface
- Reflection on plastics-liquid interface (2x)
- Scattering in the liquid
- Absorption in the liquid (depends on the frequency of the light)

1500x

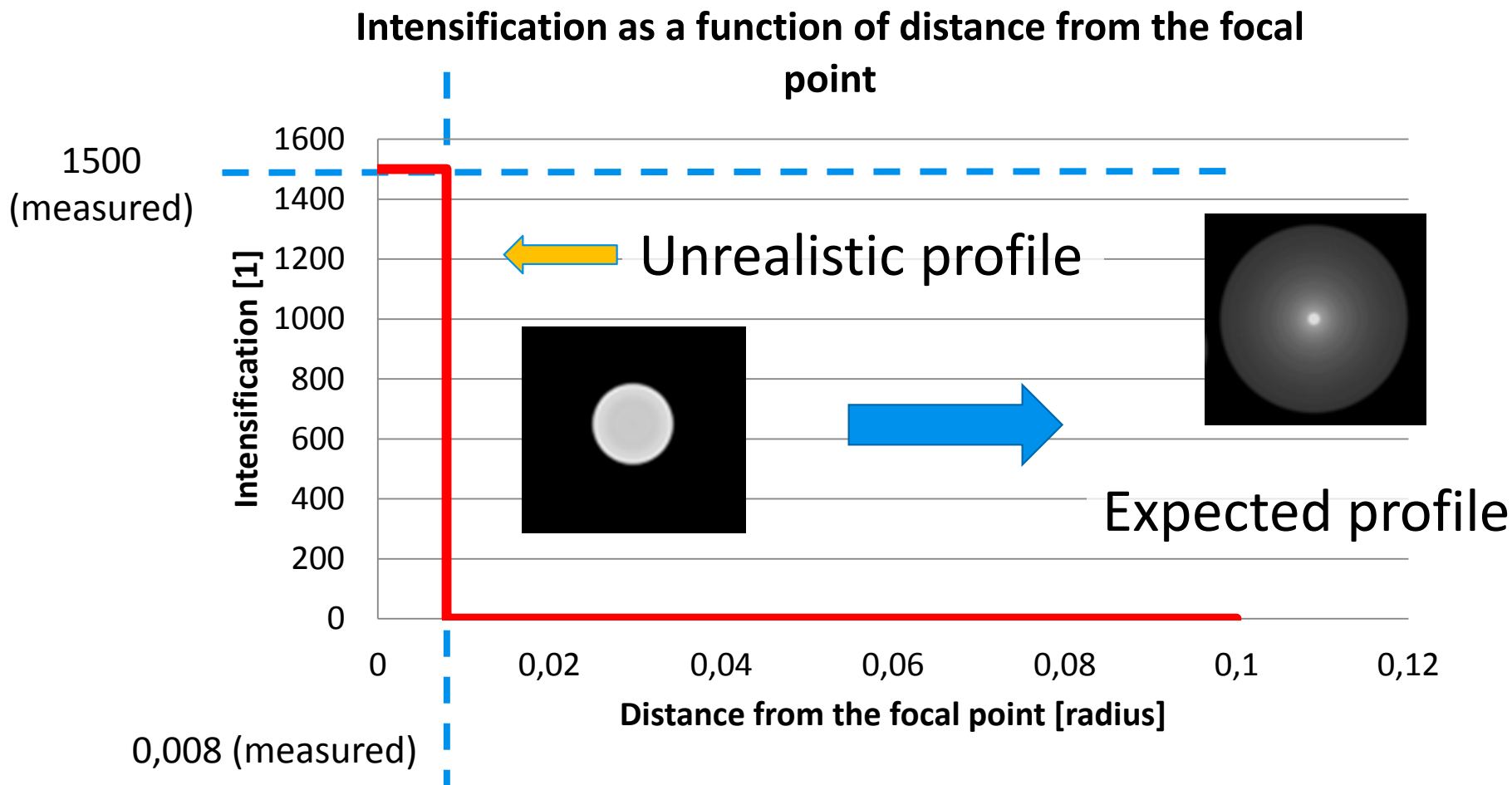
+ other undeterminable losses

$$k \cong 0.55$$

Motivation for better model



Motivation for better model



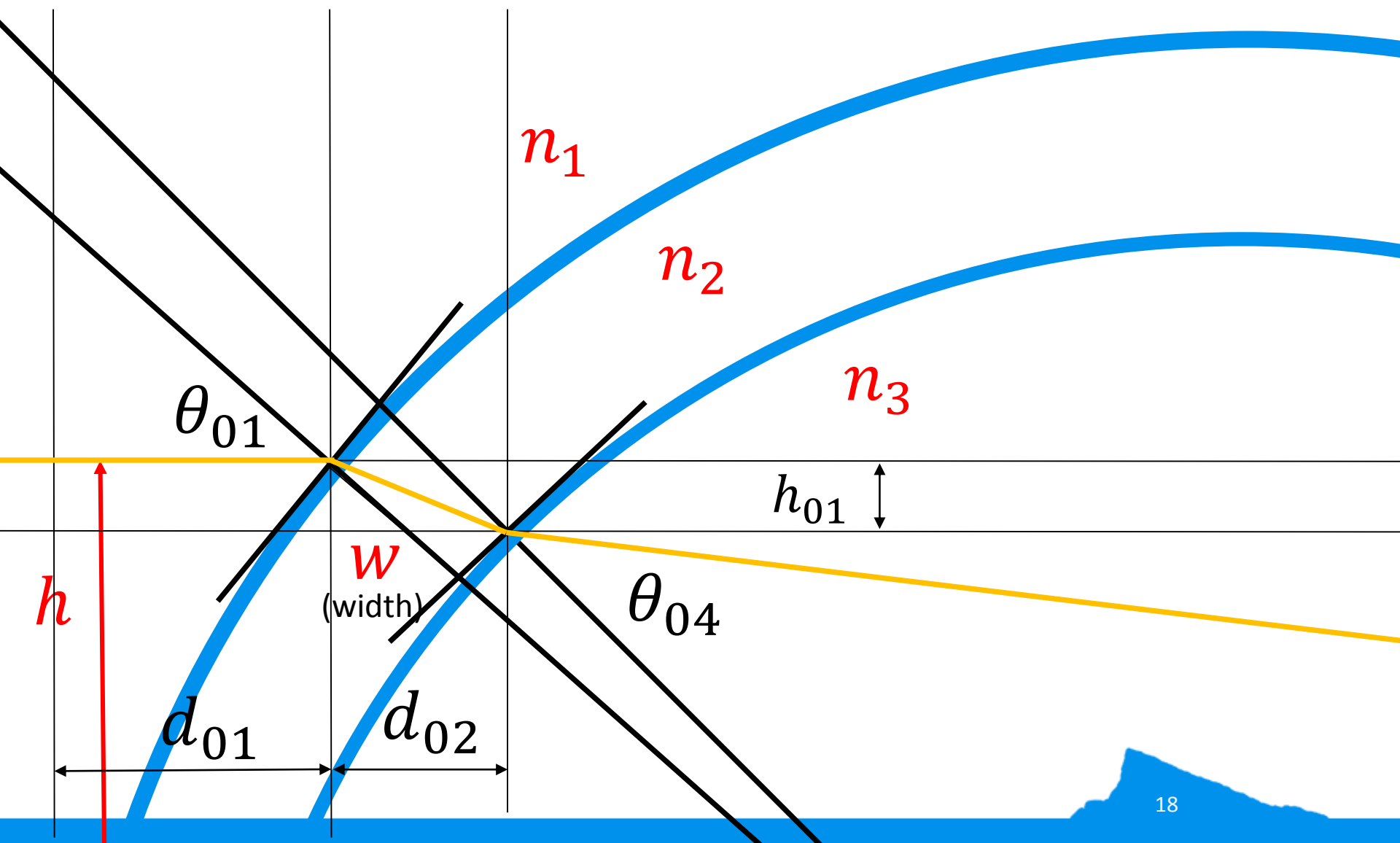


NUMERICAL RAY TRACING

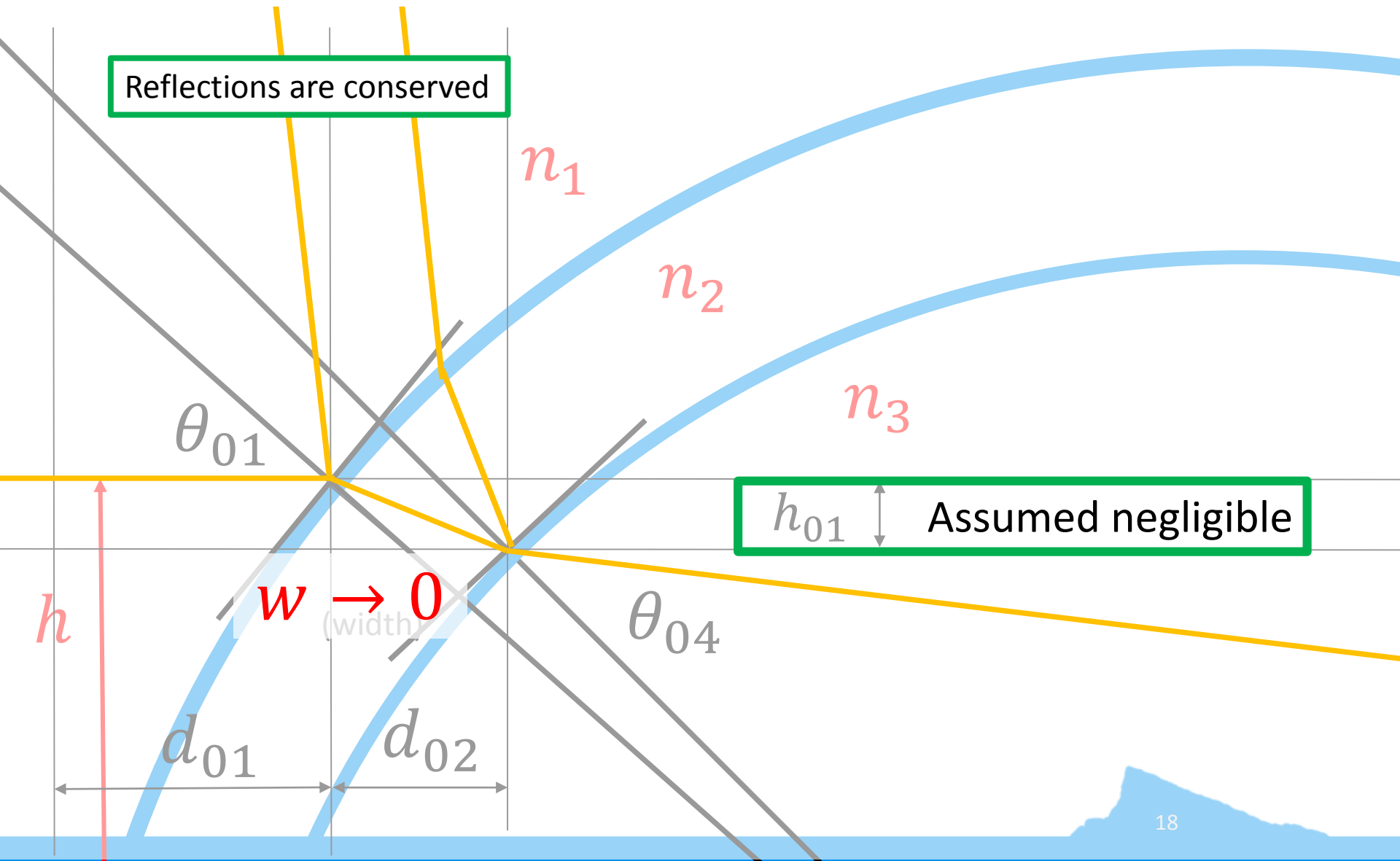
Advantages:

accuracy – spherical aberration, reflection, dispersion were assumed
results – full image of intensity profile curve

Reflection + refraction at the interfaces



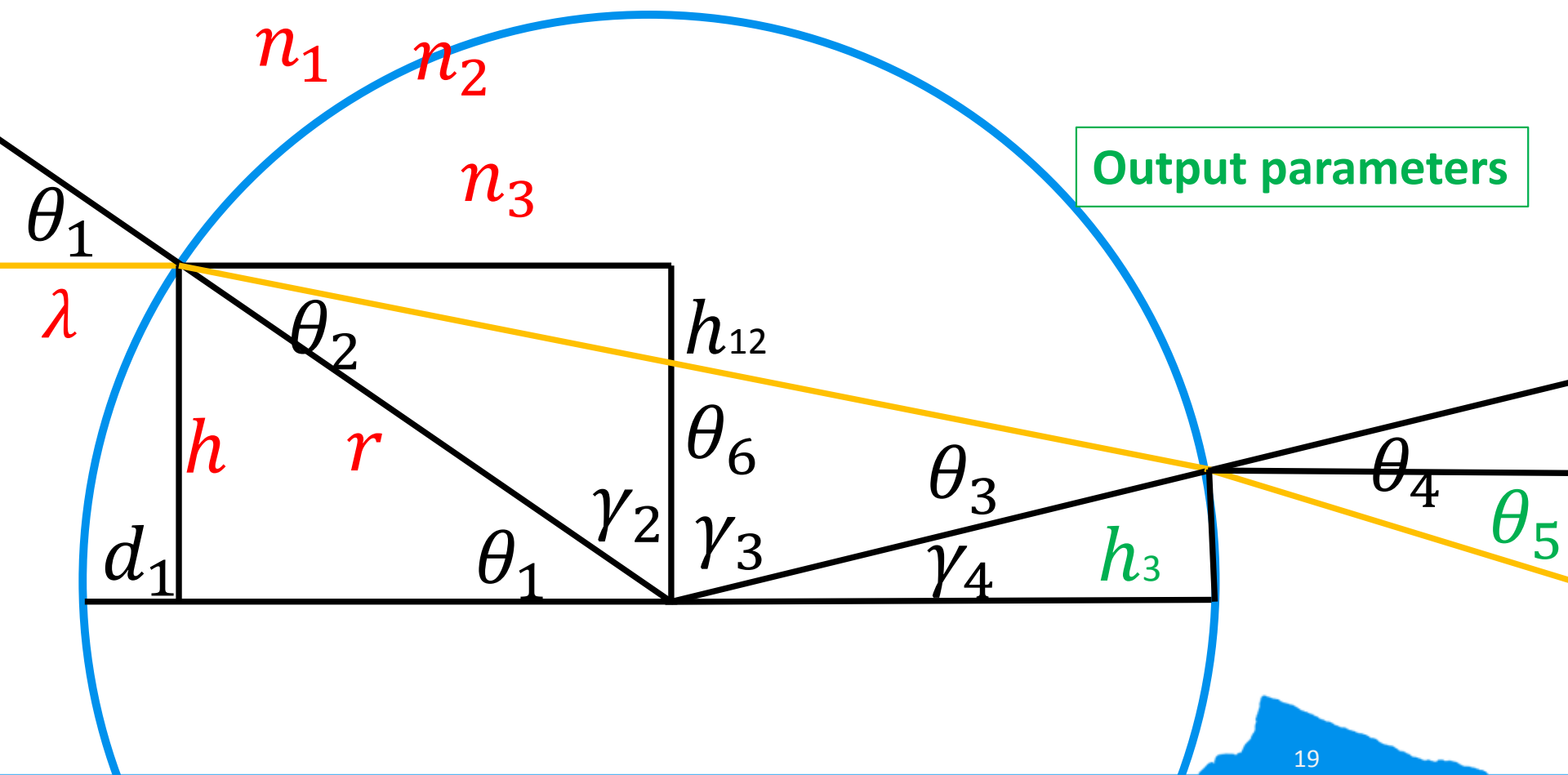
Reflection + refraction at the interfaces



Ray tracing – ins and outs

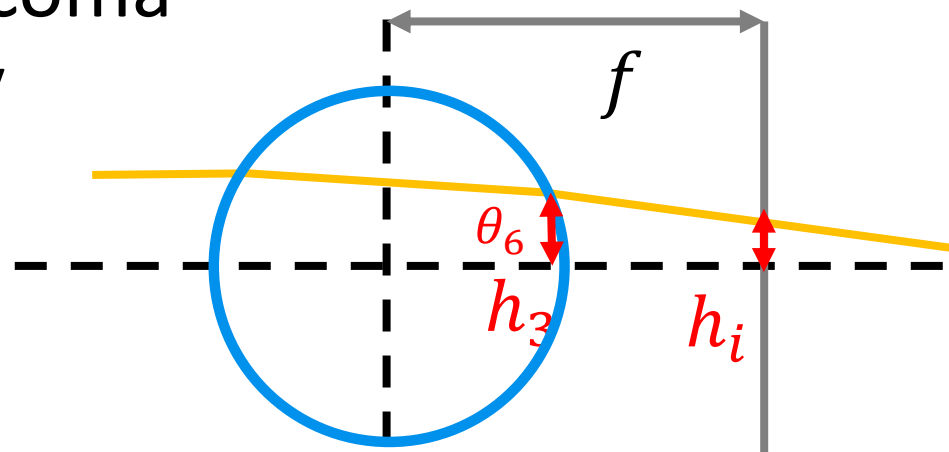
Input parameters

Output parameters

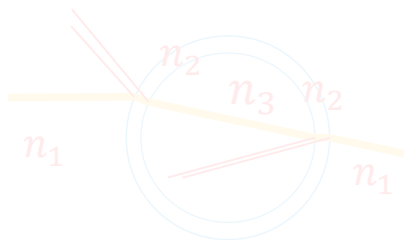


Method: included effects

- Aberration and coma included by geometry



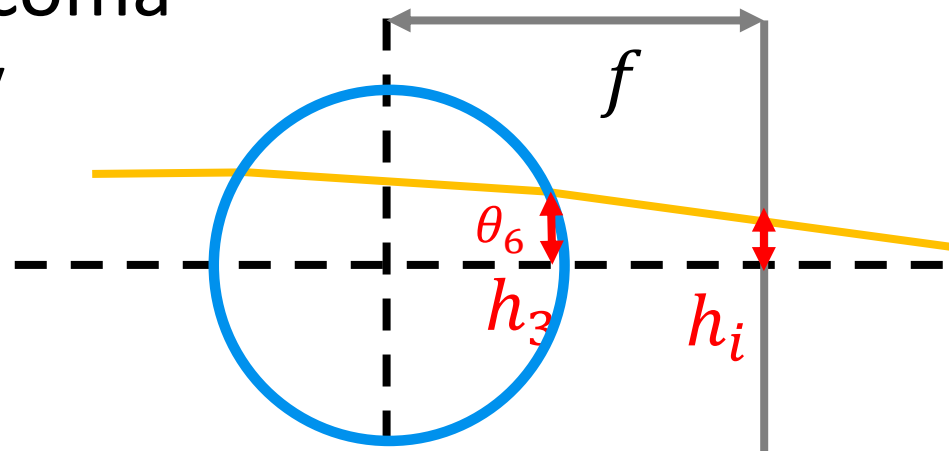
- Reflection – Fresnel equations *unpolarized light assumed



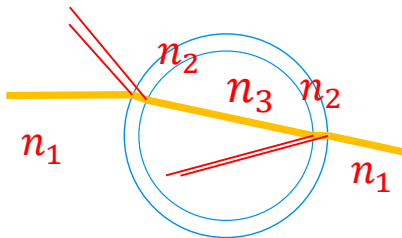
$$R = \frac{\left| \frac{n_1 \cos \theta_i - n_2 \cos \theta_t}{n_1 \cos \theta_i + n_2 \cos \theta_t} \right|^2 + \left| \frac{n_1 \cos \theta_t - n_2 \cos \theta_i}{n_1 \cos \theta_t + n_2 \cos \theta_i} \right|^2}{2}$$

Method: included effects

- Aberration and coma included by geometry



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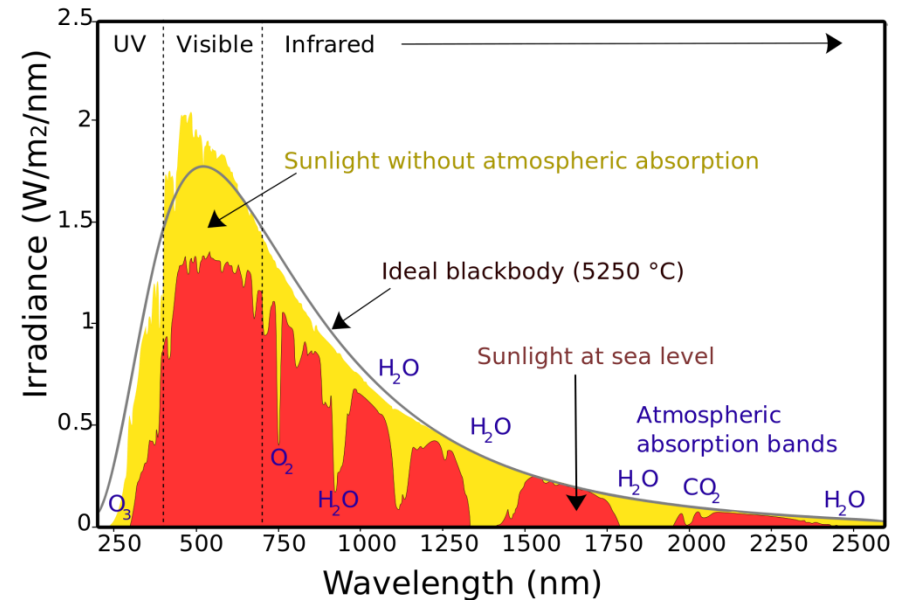
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Method: included effects

- Sun's spectrum
- black body radiation

$$I_{(v,T)} = \frac{2hv^3}{c^2} \frac{1}{e^{\frac{hv}{kT}} - 1} \left[\frac{W}{m^2 sr Hz} \right]$$

Spectrum of Solar Radiation (Earth)



- Dispersion – Cauchy's equation *for water:

$$n(\lambda) = 1.13199 + \frac{6878}{\lambda^2} + \frac{1.132 \times 10^9}{\lambda^4} + \frac{1.11 \times 10^{14}}{\lambda^6} \dots [1]$$

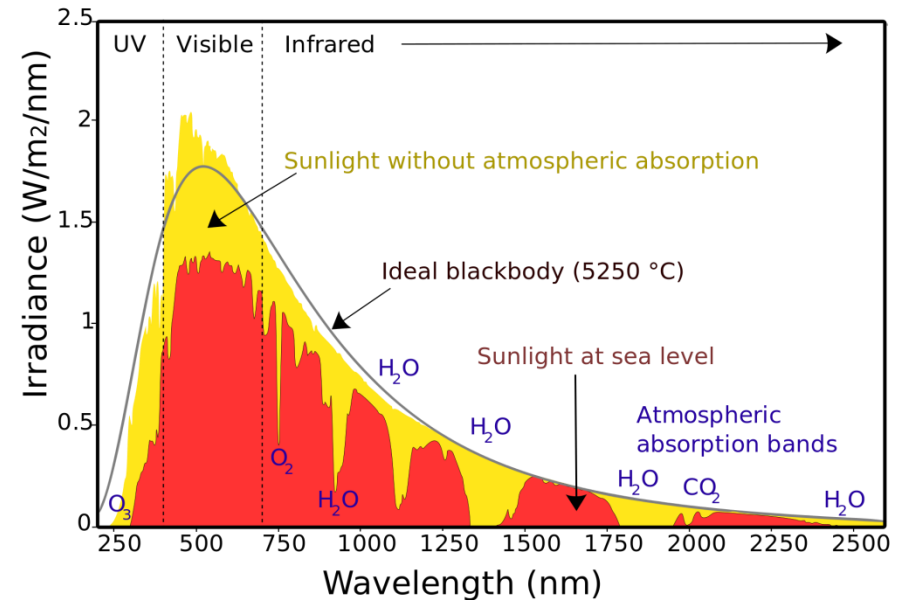
[1] Water Refractive Index in Dependence on Temperature and Wavelength, by Alexey N. Bashkatov, Elina A. Genina, Optics Department Saratov State University, Saratov, Russia

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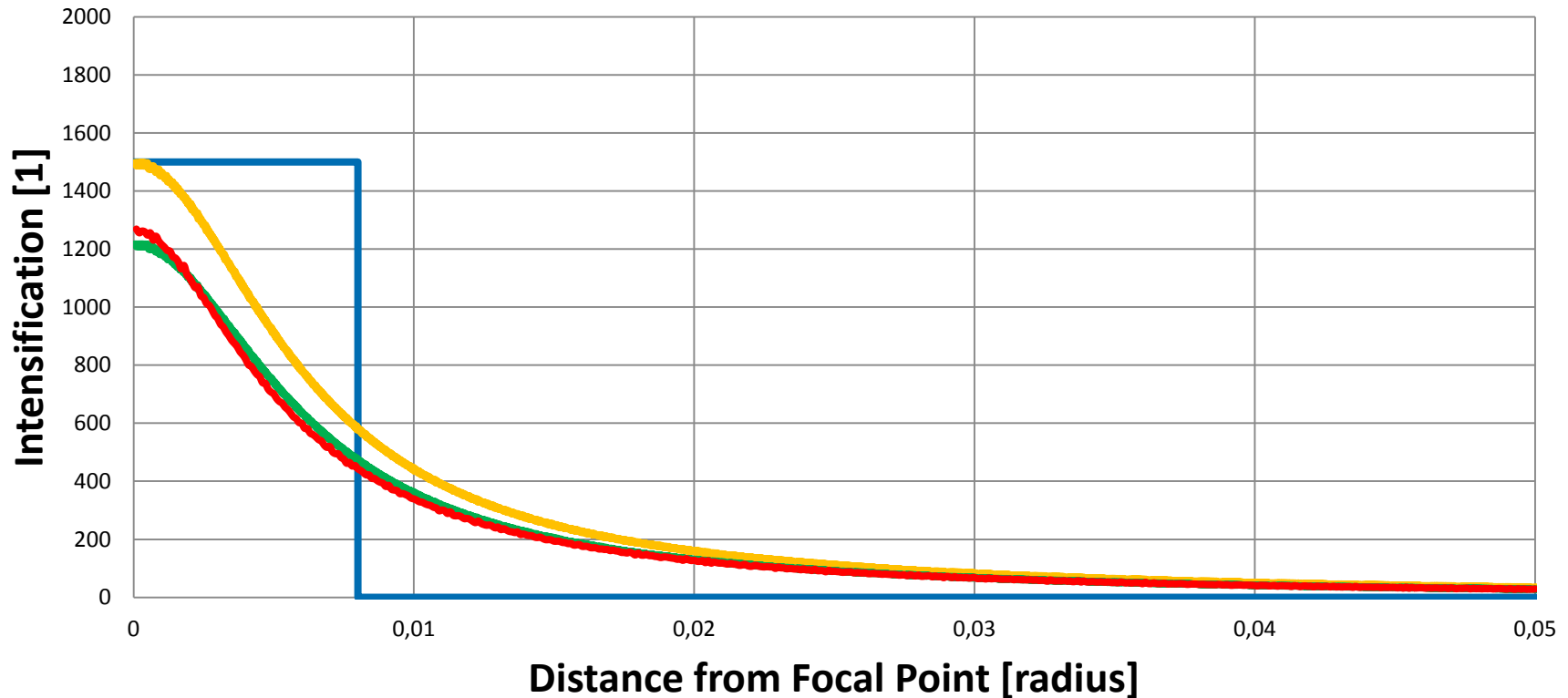
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Ray tracing – processed output

Intensification



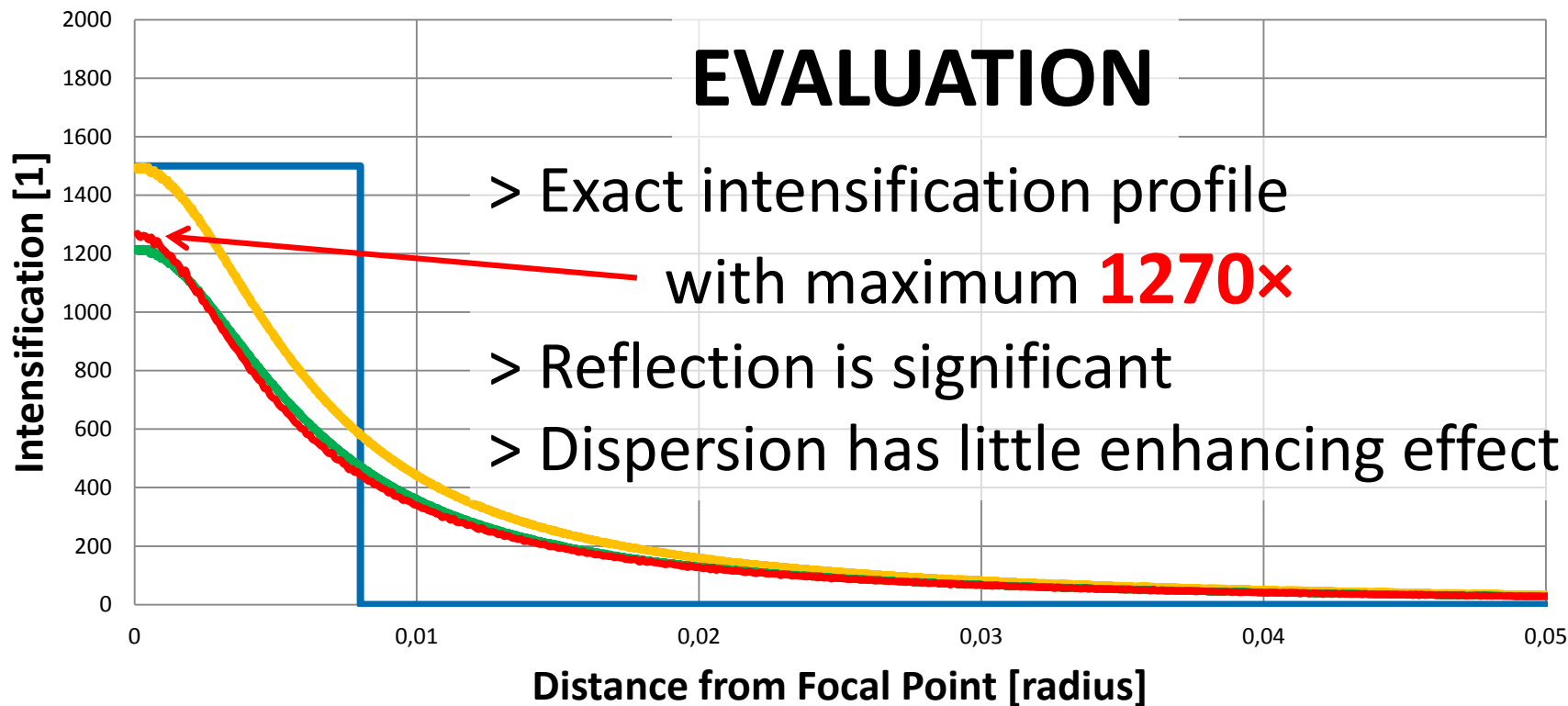
—without tracing —tracing —tracing + reflection —tracking + reflection + dispersion

Ray tracing – processed output

Intensification

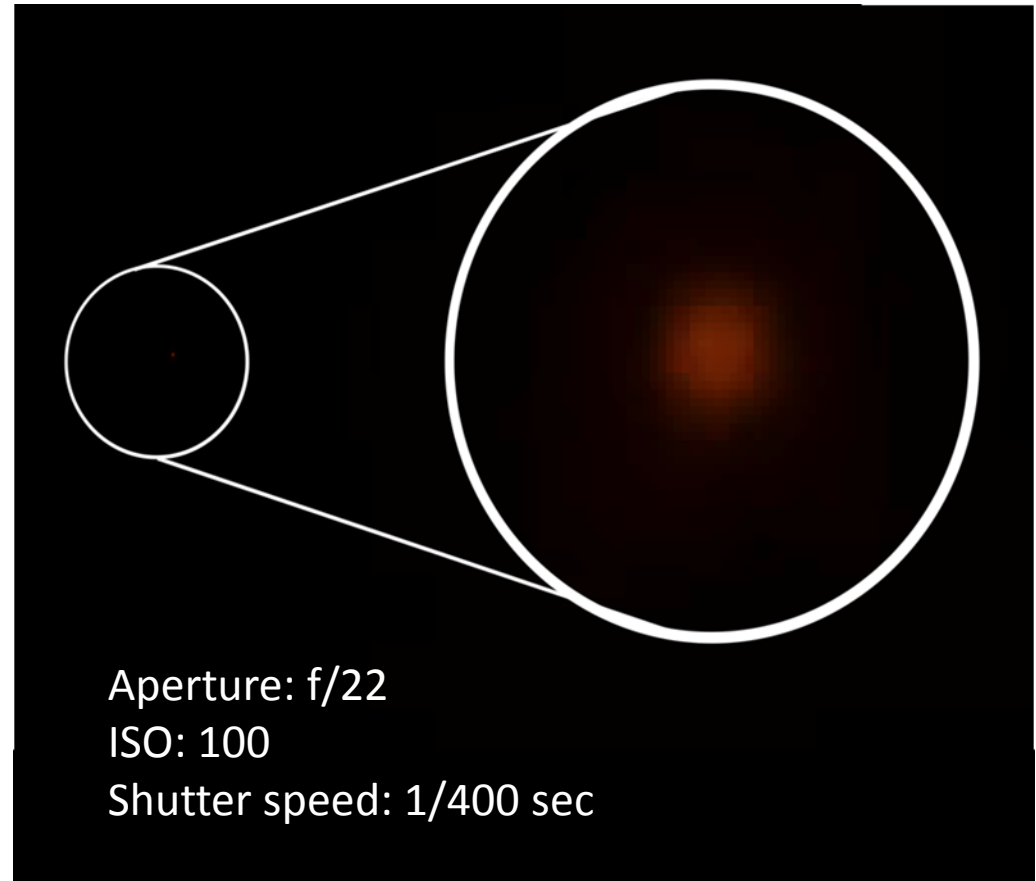
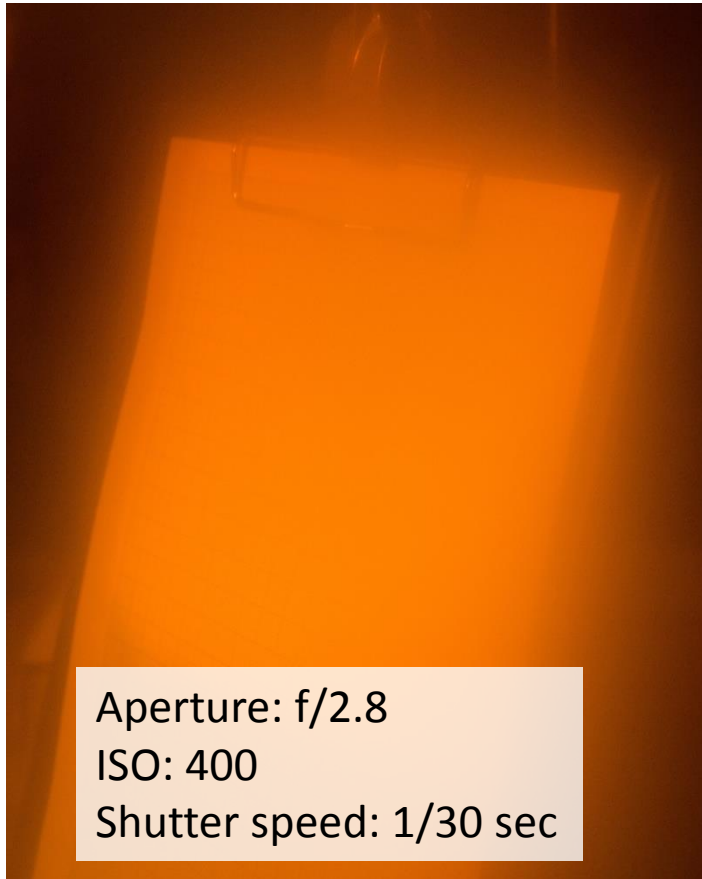
EVALUATION

- > Exact intensification profile with maximum **1270×**
- > Reflection is significant
- > Dispersion has little enhancing effect



—without tracing —tracing —tracing + reflection —tracking + reflection + dispersion

Perform more accurate measurement

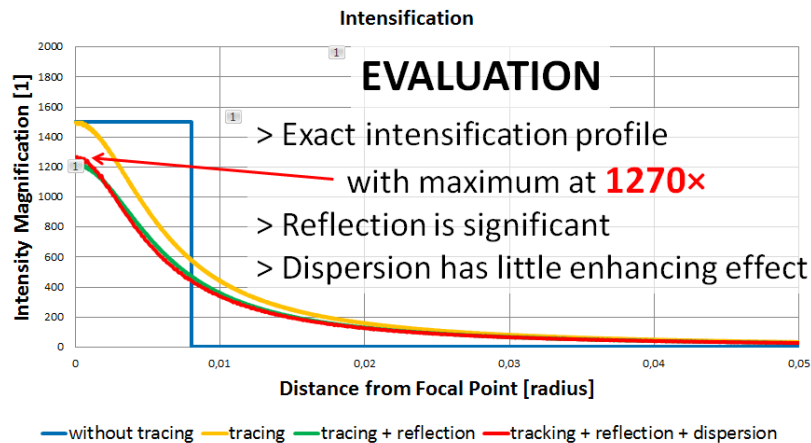


Maximum intensification:

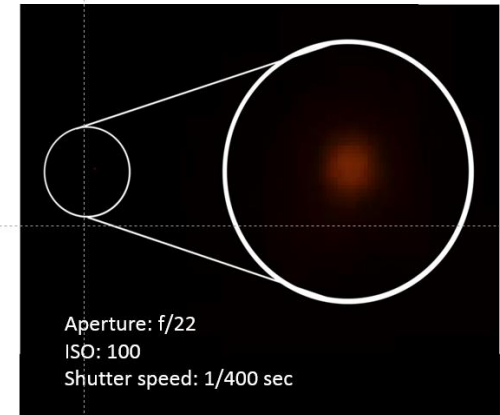
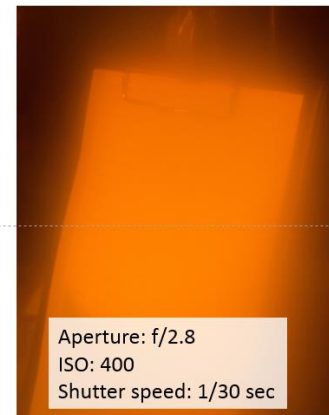
1280×

Ray tracing vs. accurate measurement

Ray tracing – processed output



Perform more accurate measurement

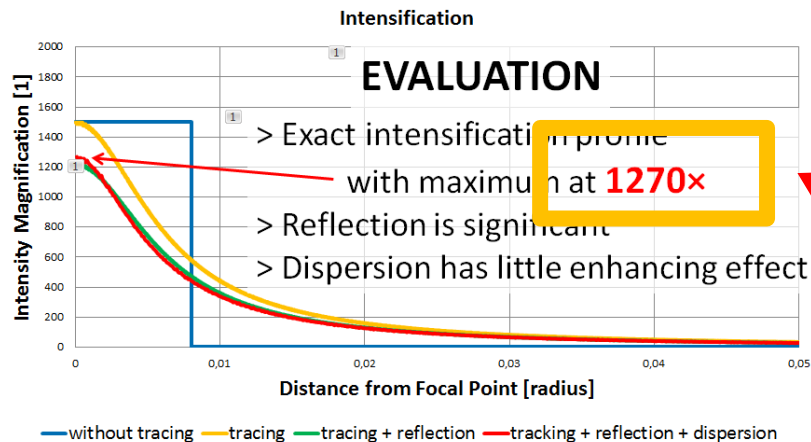


Maximum intensification:

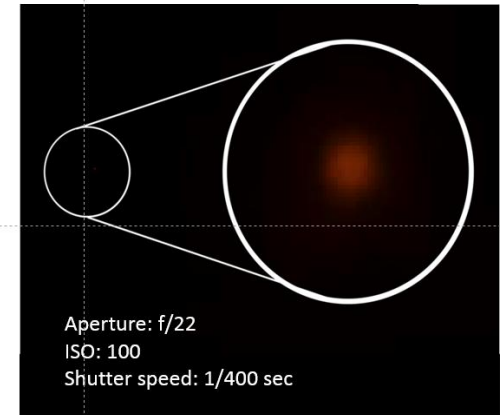
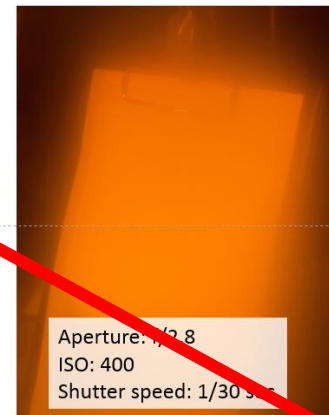
1280×

Ray tracing vs. accurate measurement

Ray tracing – processed output



Perform more accurate measurement



Maximum intensification:

1280×

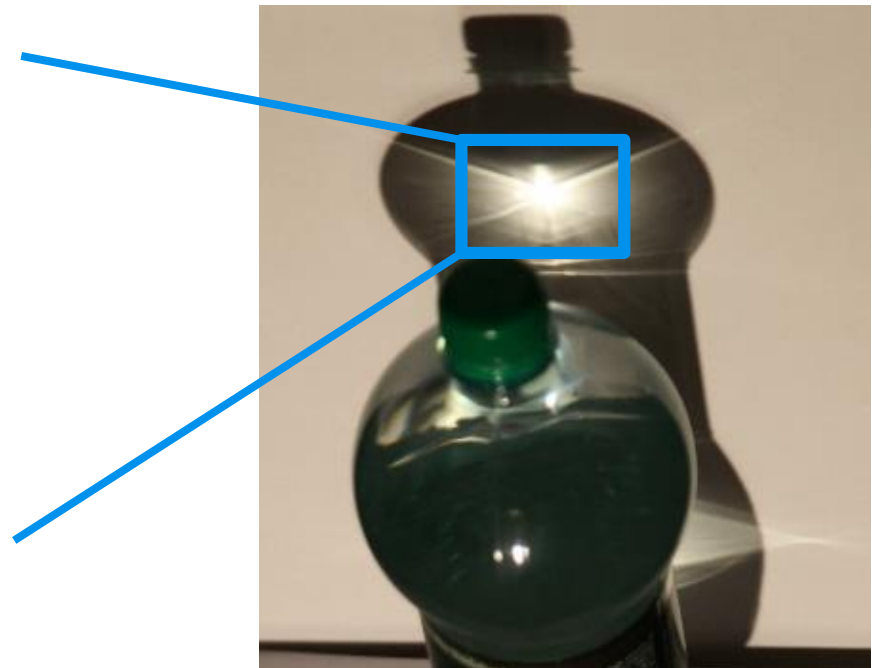
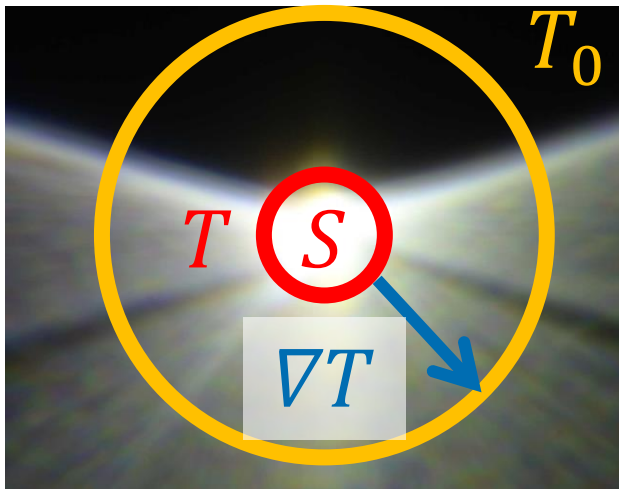
99% correlation!



SECTION 2: DISSIPATION FROM MATERIAL

Heating equation

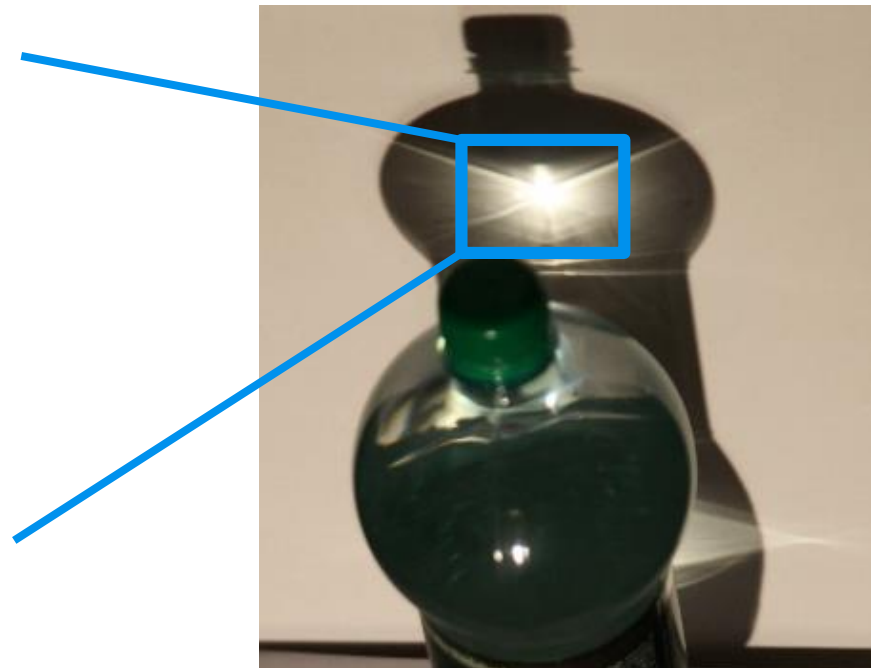
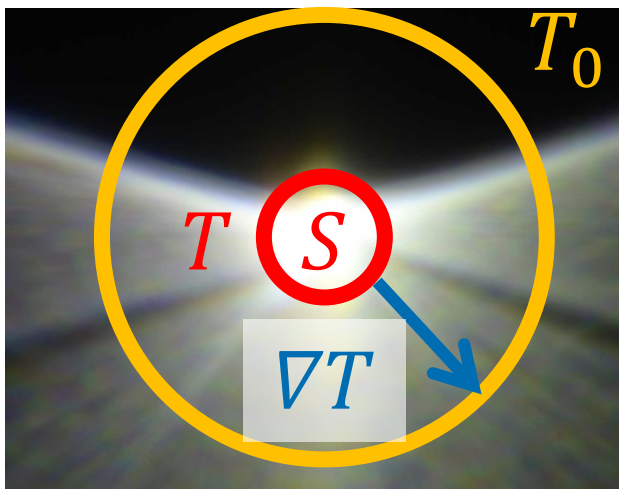
$$mk \frac{dT}{dt} = \epsilon I_{in} \mathbf{S} - \left(c \frac{\mathbf{S}}{l} + h \mathbf{S} \right) \Delta T - \sigma \epsilon \mathbf{S} T^4$$



Heating equation

$$mk \frac{dT}{dt} = \epsilon I_{in} \mathbf{S} - \left(c \frac{\mathbf{S}}{l} + h \mathbf{S} \right) \Delta T - \sigma \epsilon \mathbf{S} T^4$$

Change in internal energy

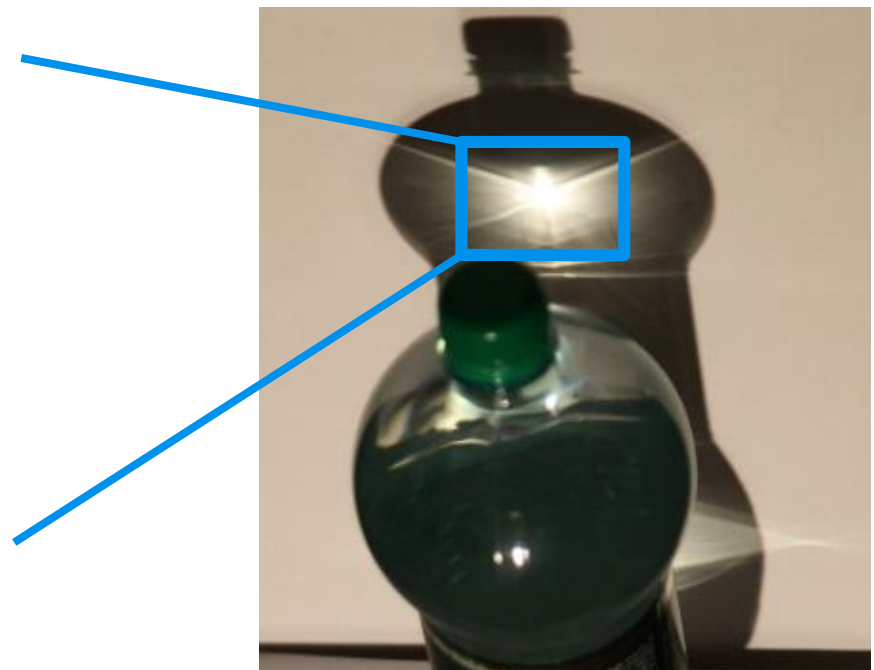
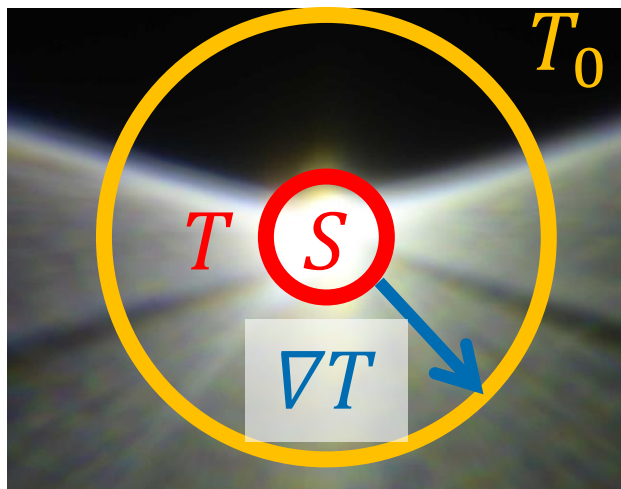


Heating equation

$$mk \frac{dT}{dt} = \epsilon I_{in} S - \left(c \frac{S}{l} + hS \right) \Delta T - \sigma \epsilon S T^4$$

Change in internal energy

Net power input



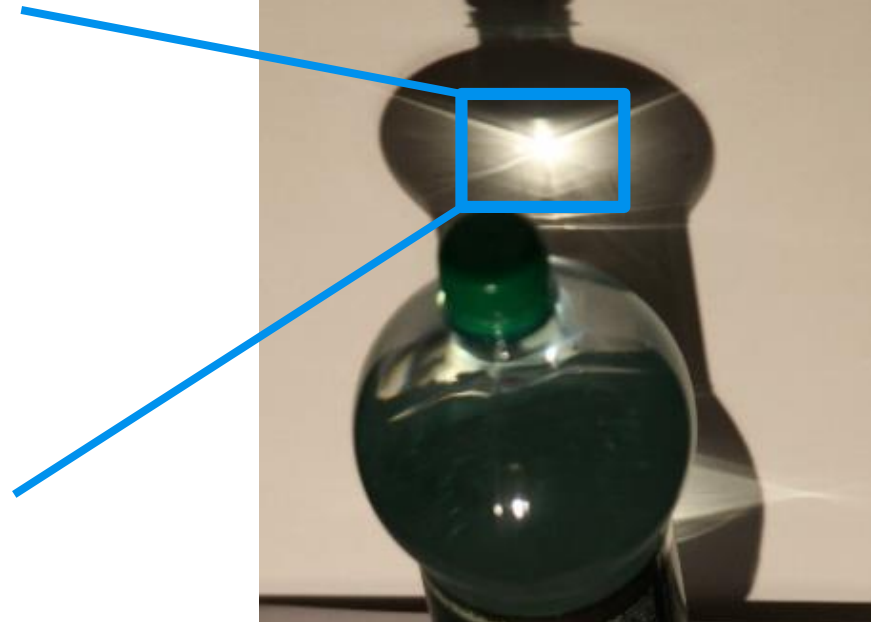
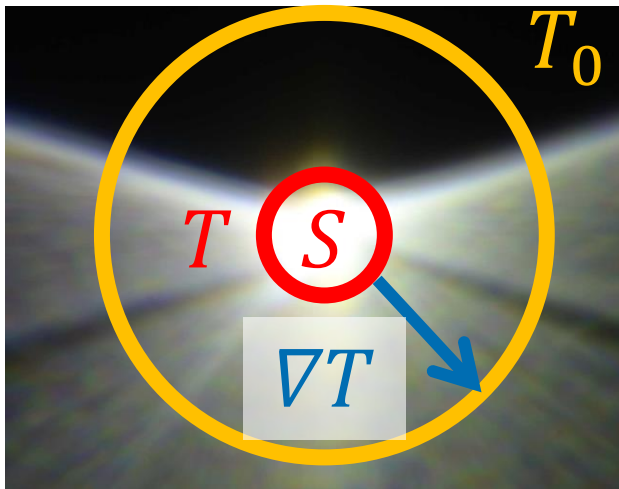
Heating equation

$$mk \frac{dT}{dt} = \epsilon I_{in} S - \left(c \frac{S}{l} + hS \right) \Delta T - \sigma \epsilon S T^4$$

Change in internal energy

Heat dissipated to surroundings by...

Net power input



Heating equation

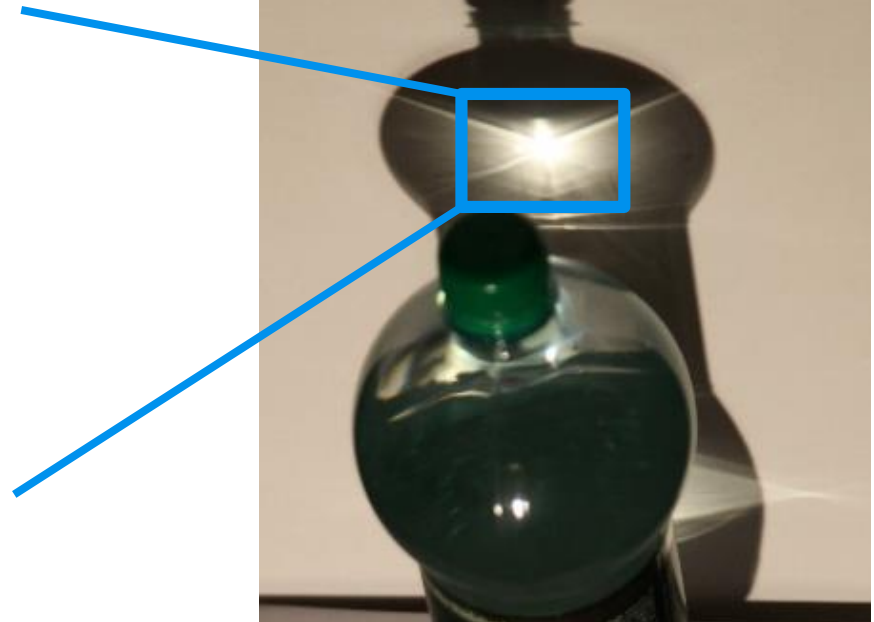
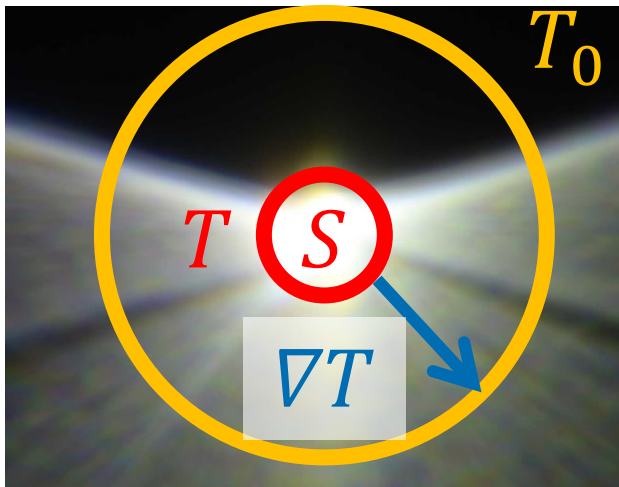
$$mk \frac{dT}{dt} = \epsilon I_{in} S - \left(c \frac{S}{l} + hS \right) \Delta T - \sigma \epsilon S T^4$$

Change in internal energy

Heat dissipated to surroundings by...

Net power input

conduction



Heating equation

$$mk \frac{dT}{dt} = \epsilon I_{in} S - \left(c \frac{S}{l} + hS \right) \Delta T - \sigma \epsilon S T^4$$

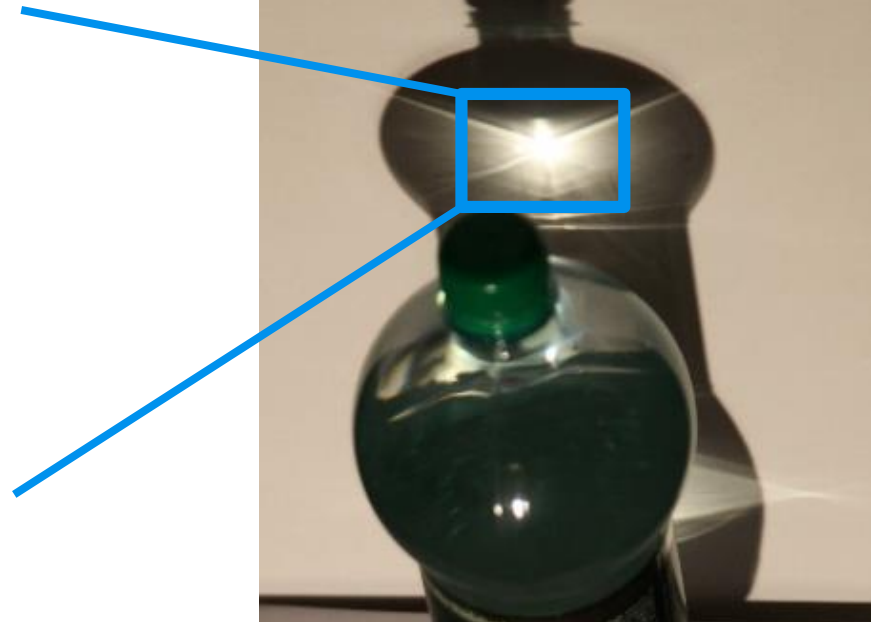
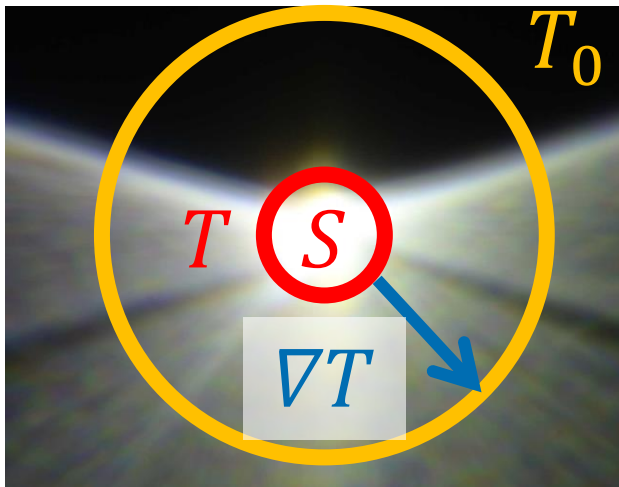
Change in internal energy

Heat dissipated to surroundings by...

Net power input

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convection



Heating equation

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Change in internal energy

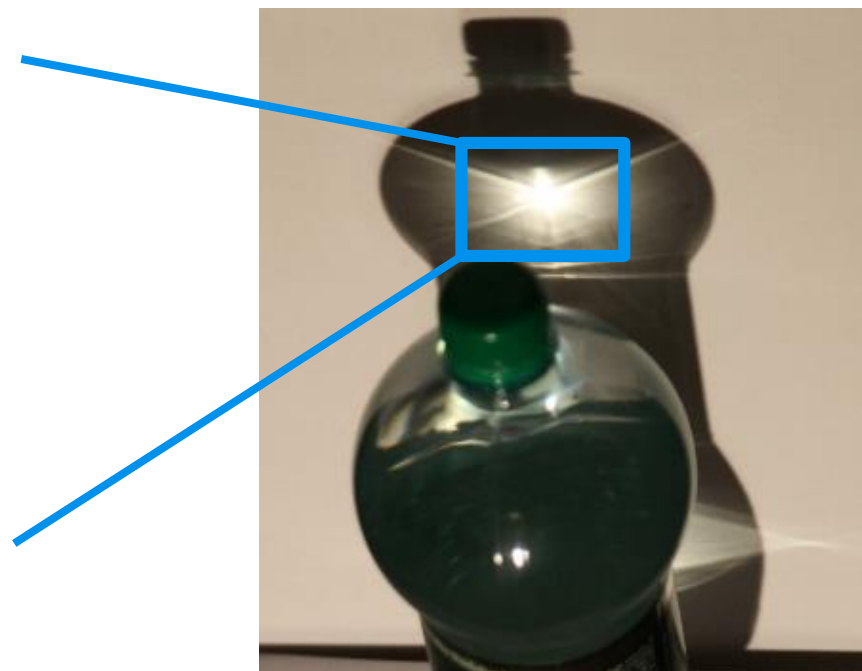
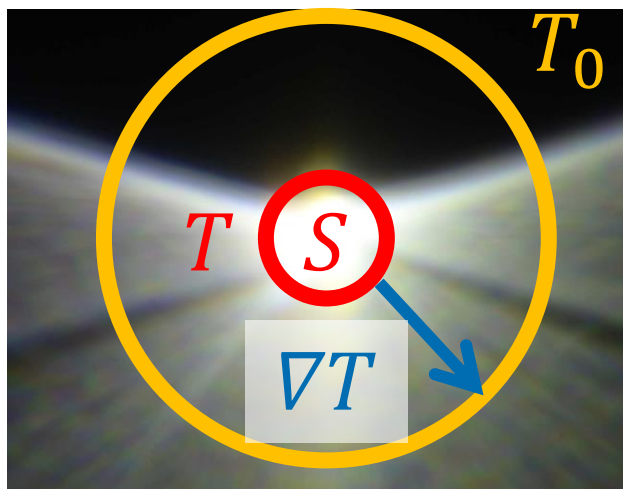
Heat dissipated to surroundings by...

Power dissipated
by radiation

Net power input

conduction

convection



Heating equation

$$mk \frac{dT}{dt} = \epsilon I_{in} S - \left(c \frac{S}{l} + h S \right) \Delta T - \sigma \epsilon S T^4$$

Change in internal energy

Heat dissipated to surroundings by...

Power dissipated
by radiation

Net power input

conduction

convection

Typical times of ignition (without considering losses)

$$t = \frac{mk(T_{scorching} - T_0)}{\epsilon I_{in} S} = 1.76 \text{ s}$$

$$m = 7 \times 10^{-7} \text{ kg}$$

$$k = 2000 \frac{\text{J}}{\text{kg K}}$$

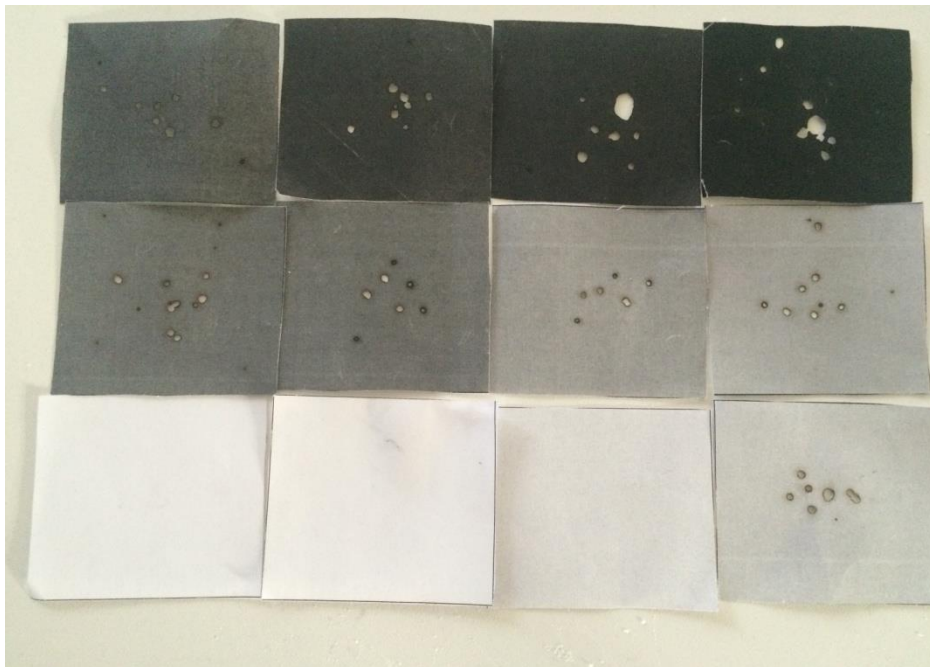
$$T_{scorching} = 670 \text{ K}$$

$$I_{in} = 320 \frac{\text{kW}}{\text{m}^2}$$

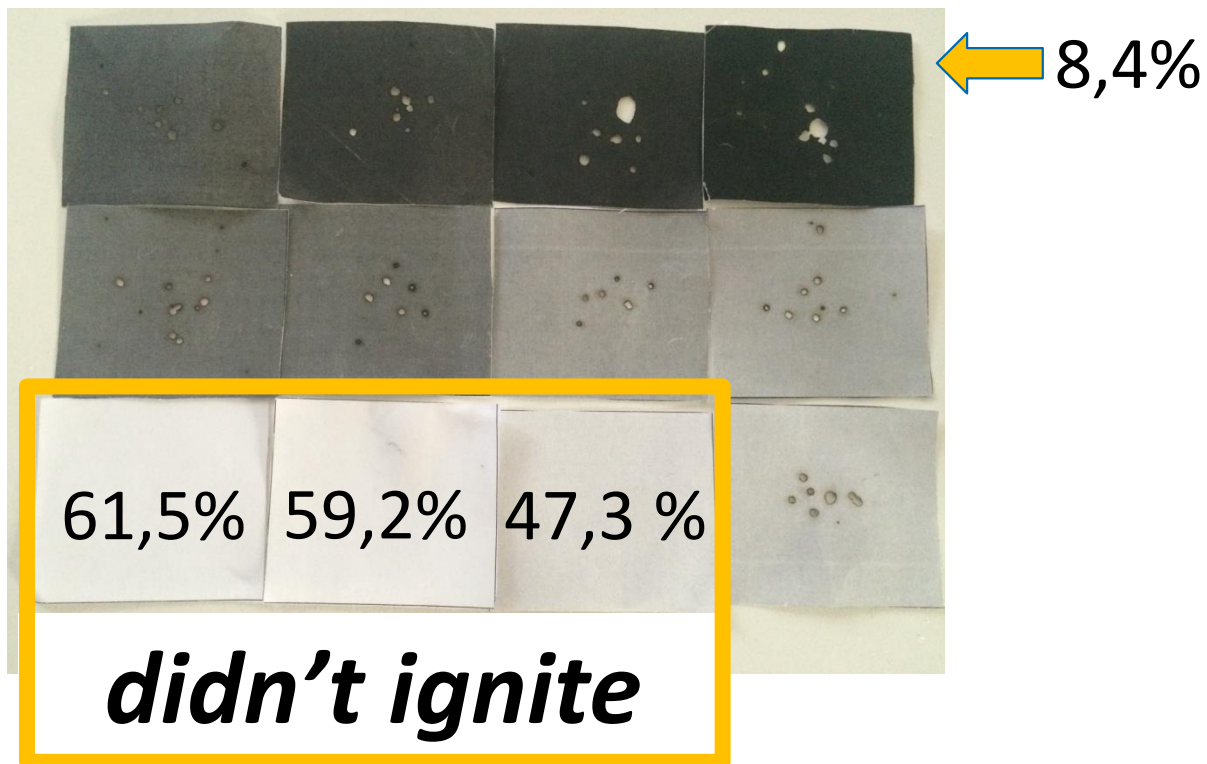
$$S = 10^{-6} \text{ m}^2$$

$$\epsilon = 0.92$$

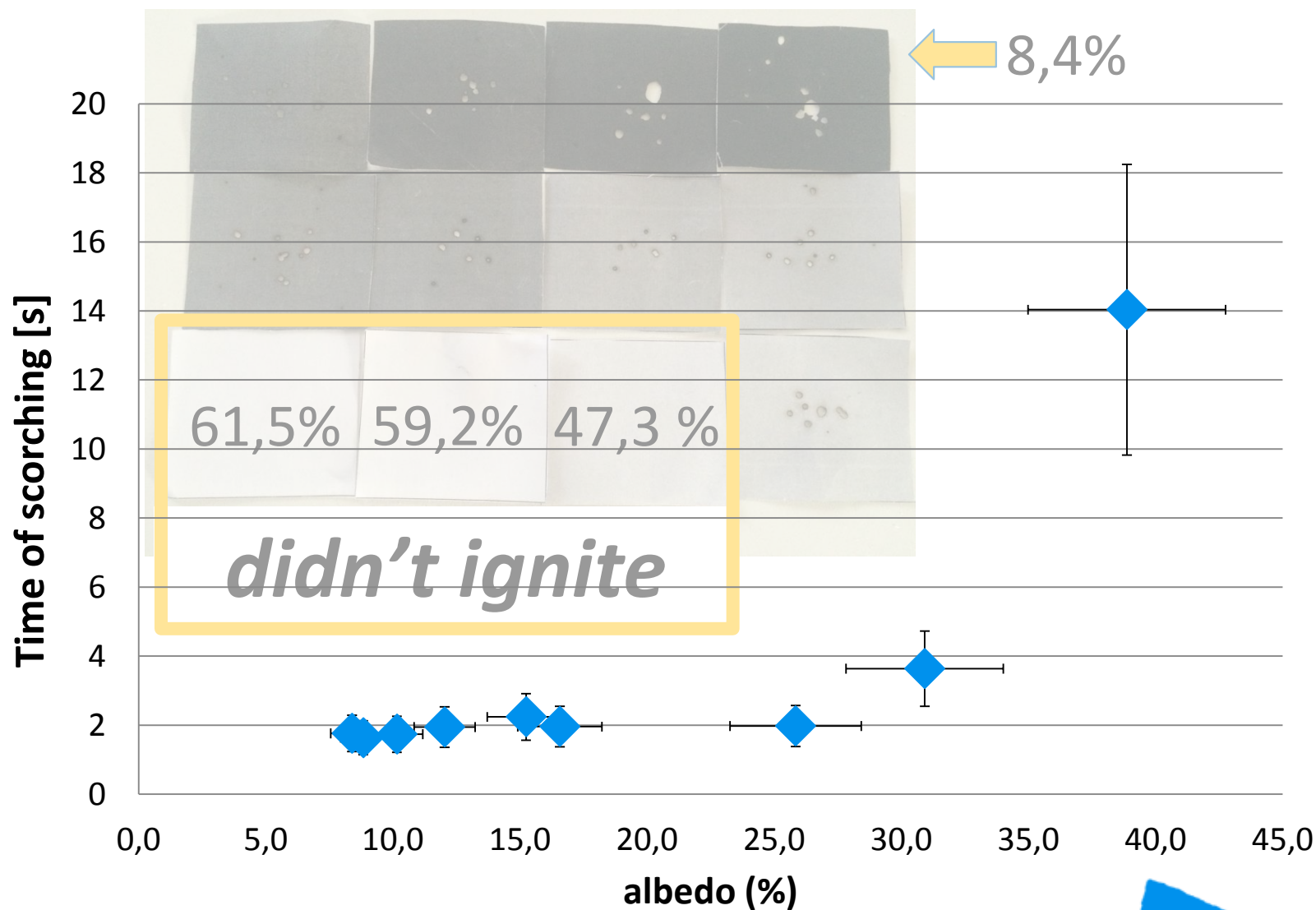
Significance of albedo



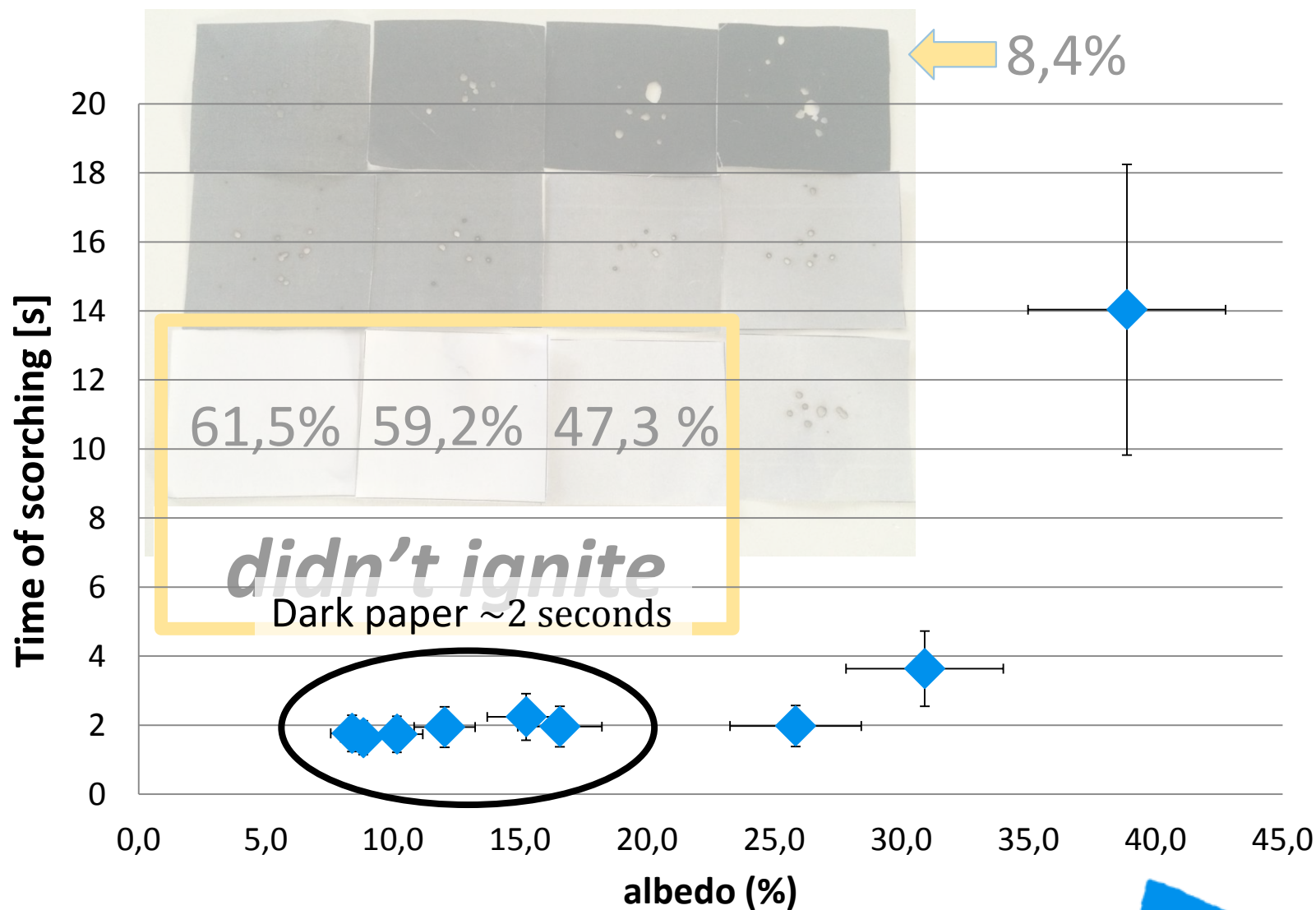
Significance of albedo



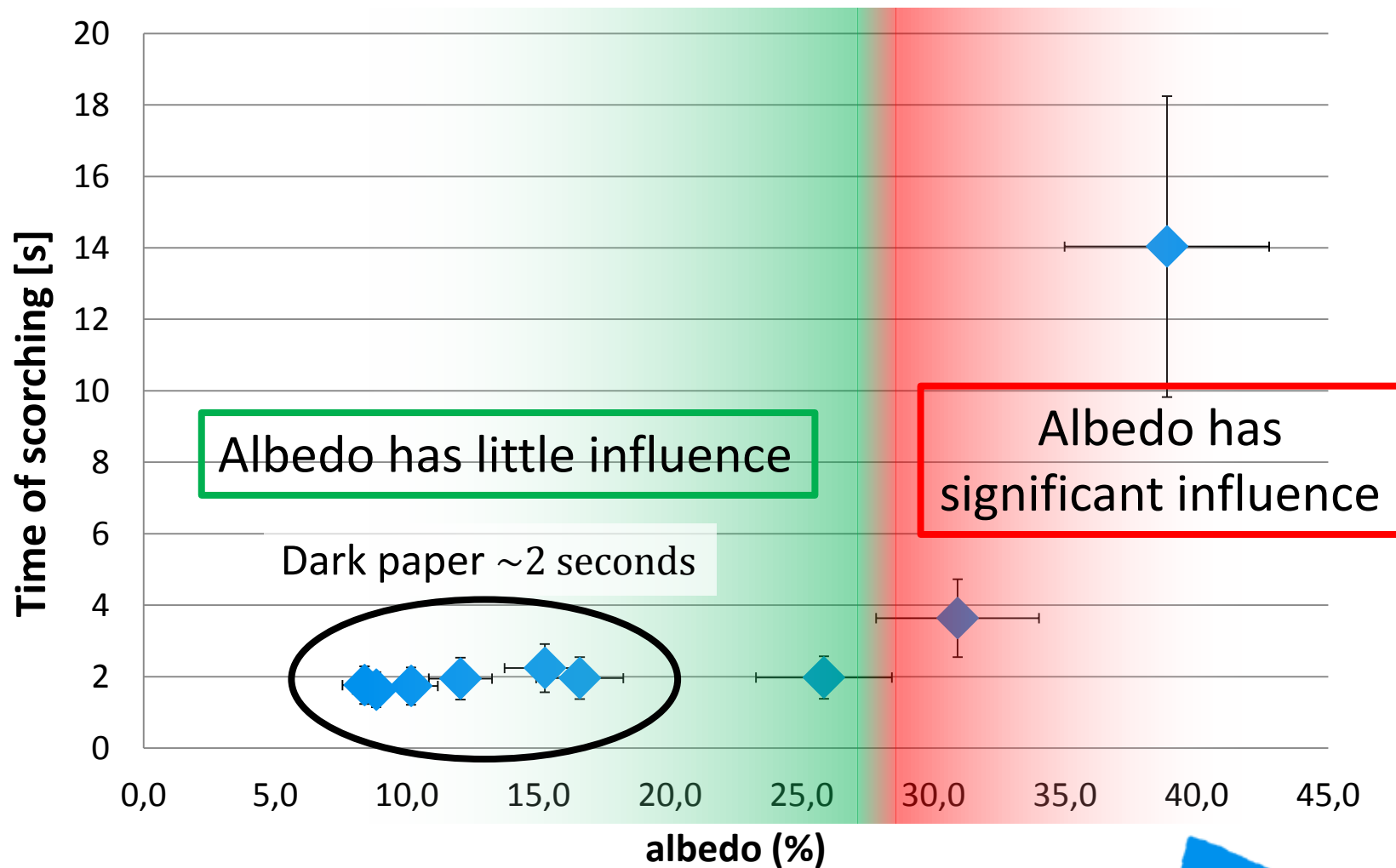
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Significance of albedo

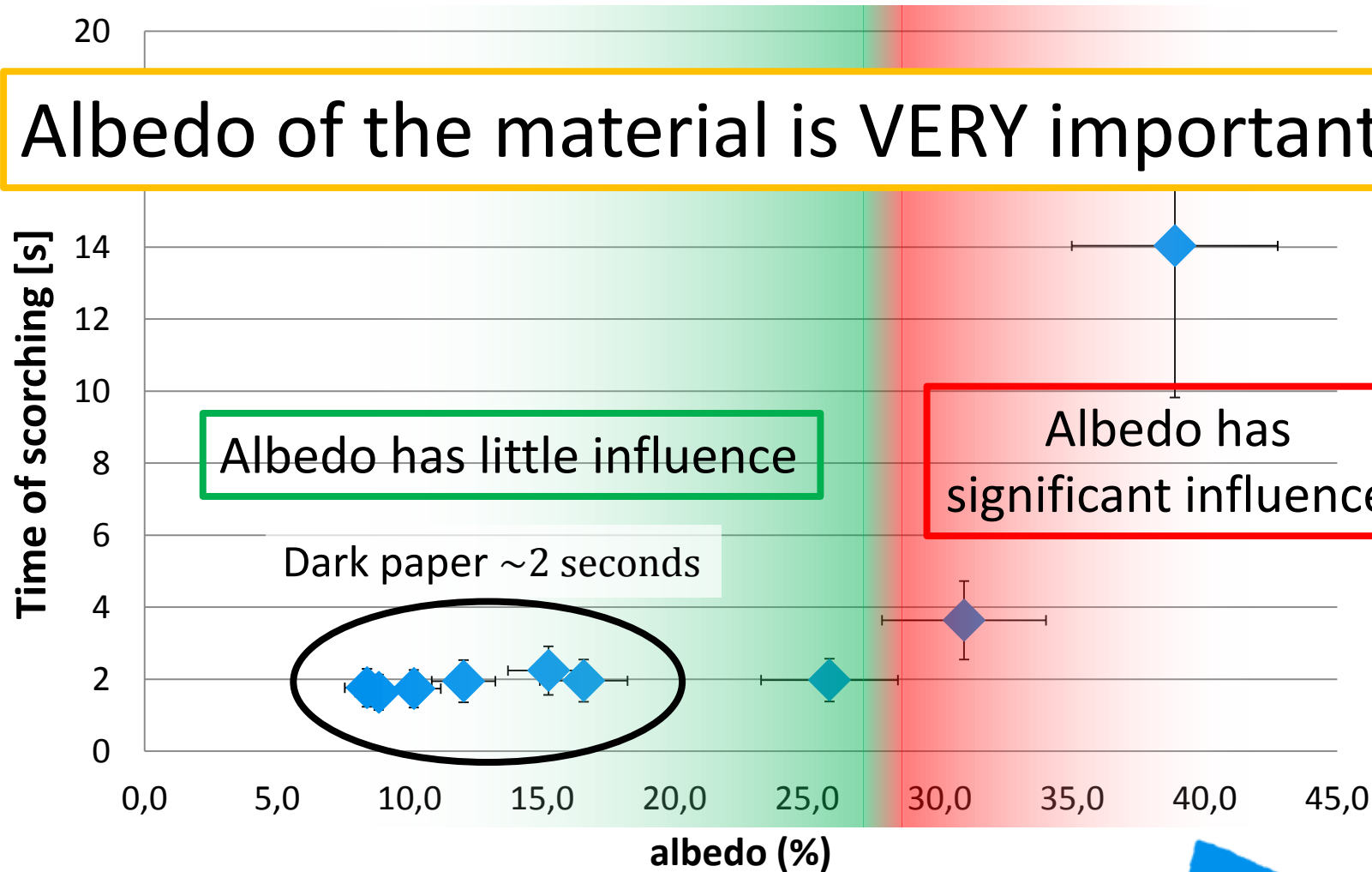


Significance of albedo



Significance of albedo

Albedo of the material is VERY important.



Basic condition for ignition

To heat the material further, this condition must be satisfied:

$$P_{incoming} \geq P_{losses}(T_{ignition})$$

Reflection

Conduction

Convection

Radiation

Basic condition for ignition

To heat the material further, this condition must be satisfied:

$$P_{incoming} \geq P_{losses}(T_{ignition})$$

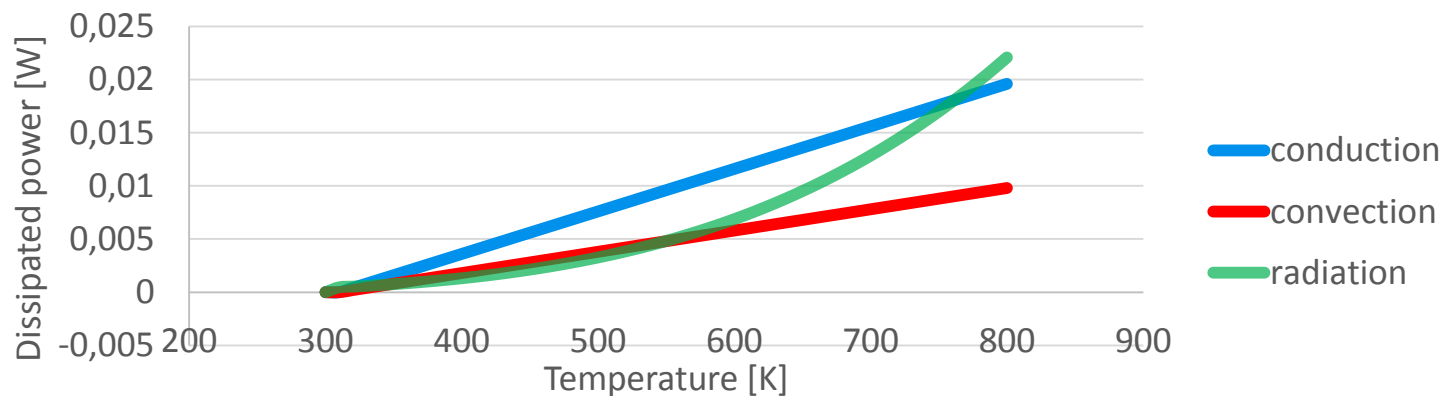
Reflection

Conduction

Convection

Radiation

Comparison of dissipated heat
by conduction, convection and radiation



Basic condition for ignition

To heat the material further, this condition must be satisfied:

$$P_{incoming} \geq P_{losses}(T_{ignition})$$

Reflection

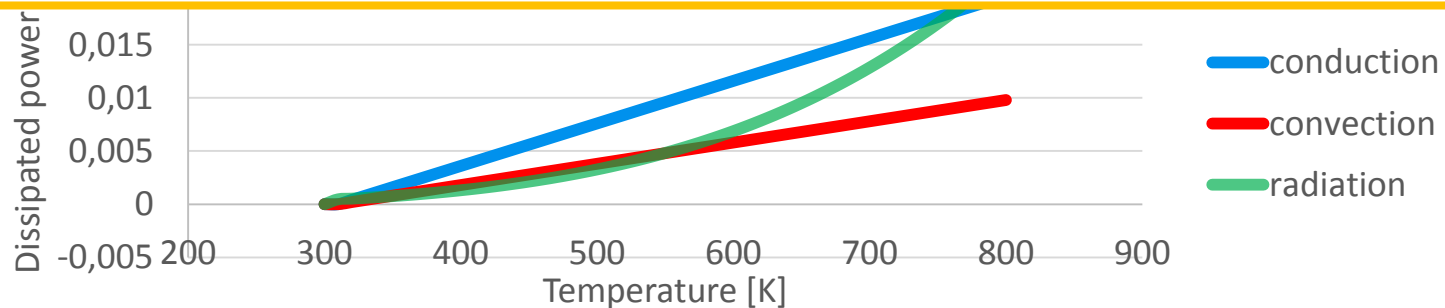
Conduction

Convection

Radiation

Comparison of dissipated heat

All of them are comparably significant.



Condition for ignition

$$P_{in}(T) \geq \epsilon P_{in} + \left(c \frac{S}{l} + h S \right) \Delta T + \sigma \epsilon S T^4$$

If incoming intensity is sufficiently large,



temperature rises until ignition



Condition for ignition

$$P_{in}(T) \geq \epsilon P_{in} + \left(c \frac{S}{l} + h S \right) \Delta T + \sigma \epsilon S T^4$$

If incoming intensity is sufficiently large,

What is sufficient?

temperature rises until ignition



Condition for ignition

$$P_{in}(T) \geq \epsilon P_{in} + \left(c \frac{S}{l} + h S \right) \Delta T + \sigma \epsilon S T^4$$

Critical intensity *(peak) intensity of incoming radiation that ignites the surface*



Condition for ignition

$$P_{in}(T) \geq \epsilon P_{in} + \left(c \frac{S}{l} + h S \right) \Delta T + \sigma \epsilon S T^4$$

Critical intensity *(peak) intensity of incoming radiation that ignites the surface*

Calculation

$$P_{dissipated} = c \frac{S}{l} \Delta T + h S \Delta T + \sigma \epsilon S T^4$$

At ignition temperature for wood: $T = 670 \text{ K}$

$$0.015 \text{ W} + 0.0074 \text{ W} + 0.0114 \text{ W} = 0.033 \text{ W}$$

Condition for ignition

$$P_{in}(T) \geq \epsilon P_{in} + \left(c \frac{S}{l} + h S \right) \Delta T + \sigma \epsilon S T^4$$

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$$I_{critical} \cong 33 \frac{\text{kW}}{\text{m}^2}$$

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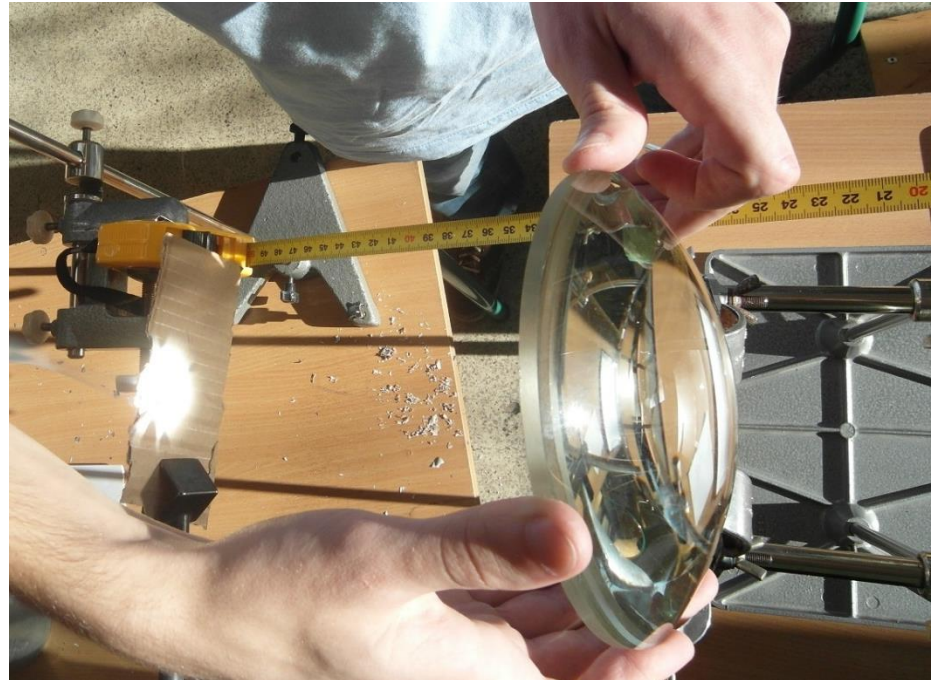
$$I_{critical} \cong 33 \frac{\text{kW}}{\text{m}^2}$$

Measurement...



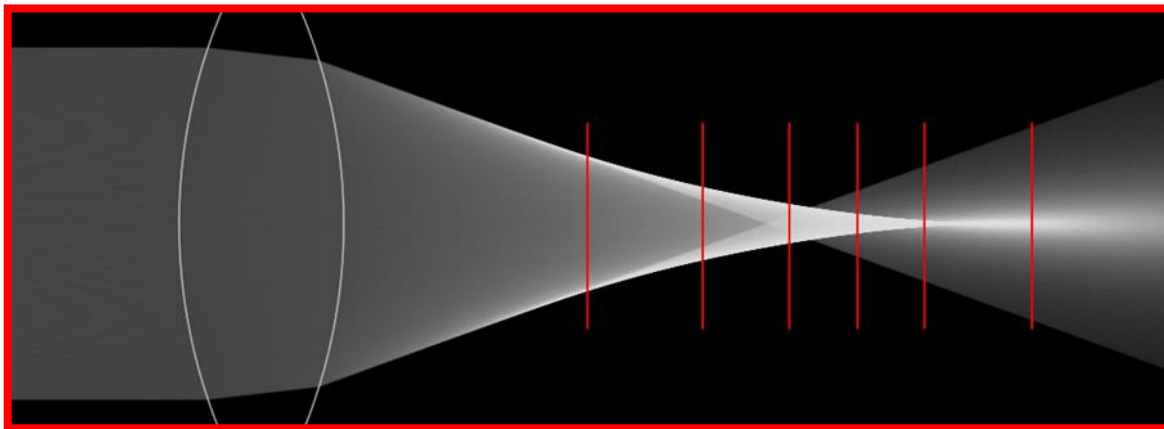
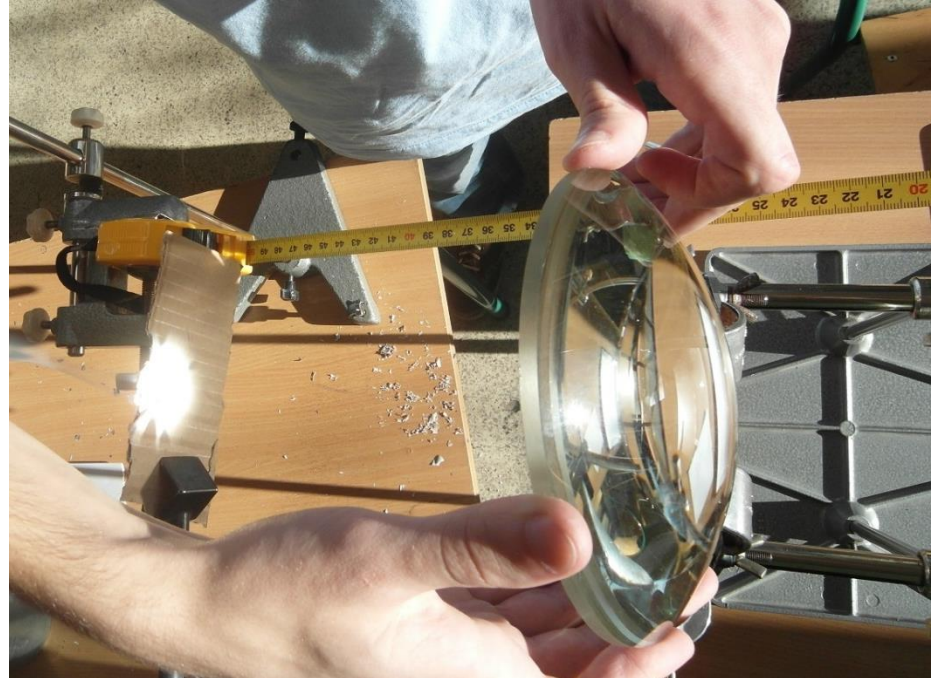
Critical intensities (the measurement)

- We change distance between the lens and the target
- What is the range of distances in which the material scorch?
- Conditions of the experiment
 - Sunlight intensity 380 W/m^2
 - Typical shifts: 1 – 5 cm



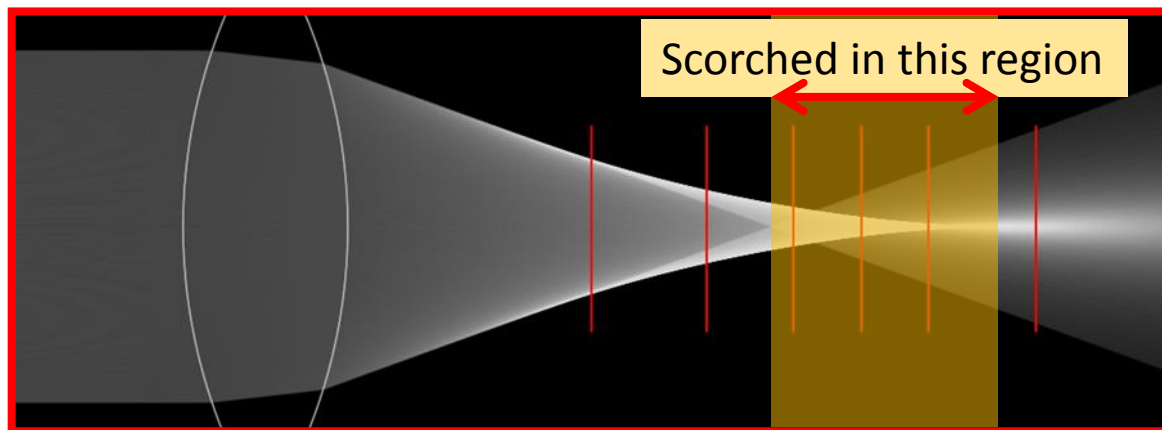
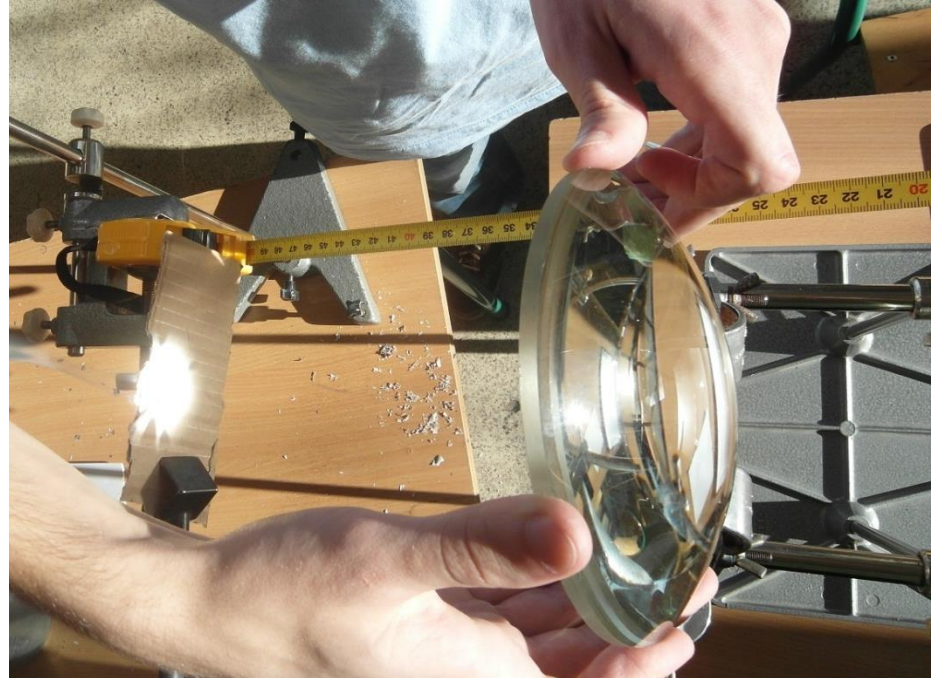
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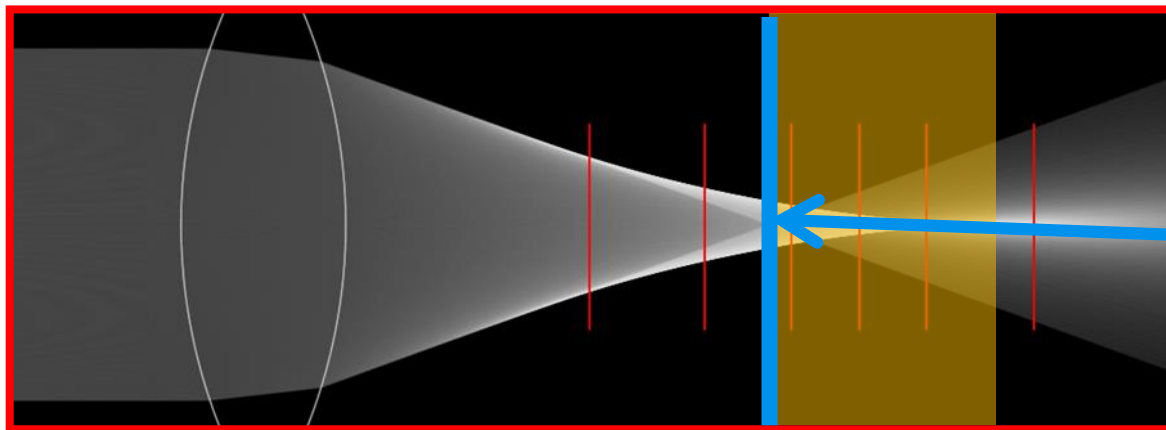
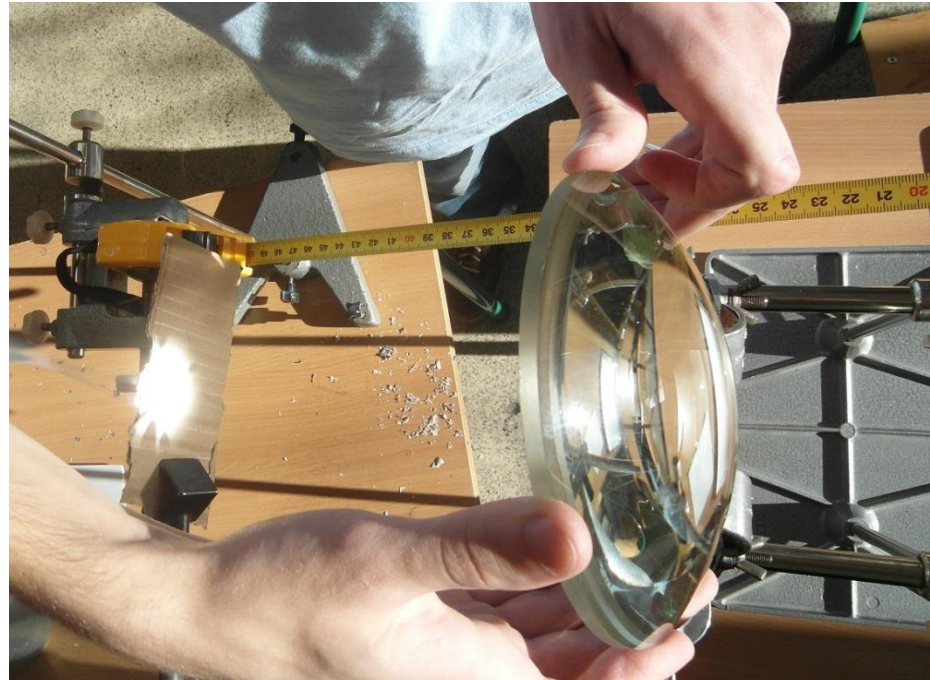
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Critical intensities (the measurement)

- We change distance between the lens and the target
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 - Sunlight intensity 380 W/m^2
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Critical intensity
value calculated
from geometry



Comparison



Comparison

Light intensity achieved by lens in the **experiment**
to **scorch** the wooden sample

$$I_{charring} = 14 \pm 1.4 \frac{kW}{m^2}$$

Comparison

Calculated light intensity from the condition of **ignition**

$$I_{critical} \cong 33 \frac{kW}{m^2}$$

Light intensity achieved by lens in the **experiment**
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Calculated light intensity from the condition of **ignition**

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Light intensity achieved by lens in the **experiment**
to **scorch** the wooden sample

$$I_{charring} = 14 \pm 1.4 \frac{kW}{m^2}$$

Heat flux used to ignite a wooden sample in the article*

$$\phi_{heat} = 15 - 30 \frac{kW}{m^2}$$

Measurements

Material	Critical Intensity* ($\pm 10\%$) [W/m ²]
Bond paper (white)	500 000
Dot matrix printing paper	175 000
Cardboard	10 000
Wood	14 000
Black scarf (100% polyacryl)	4 000
Thin blue plastic bag (polyethylen)	3 000

*to damage the surface

Measurements

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Bond paper (white)	500 000
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scorched
or burned

melted

*to damage the surface

Measurements

Theoretical maximum
for Brusnianska is $\sim 1\,280\,000\text{ W/m}^2$
(depends on Sunlight intensity)

Bond paper (white)	500 000
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Cardboard	10 000
Wood	14 000
Black scarf (100% polyacryl)	4 000
Thin blue plastic bag (polyethylen)	3 000

scorched
or burned

melted

CONFIRMED BY AN EXPERIMENT

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(depends on Sunlight intensity)

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Albedo > 60%
¼ energy absorbed by water in IR region

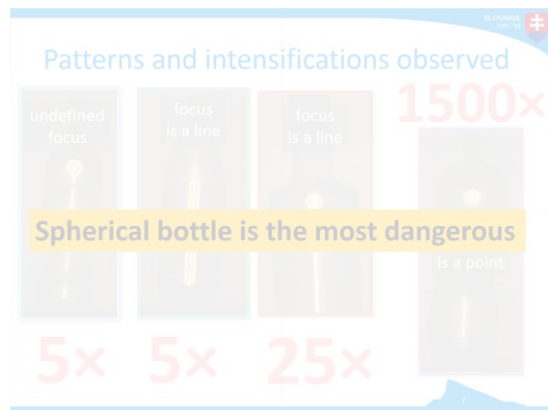
scorched
burned

melted

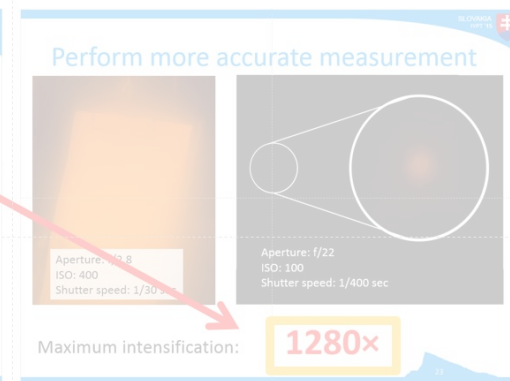
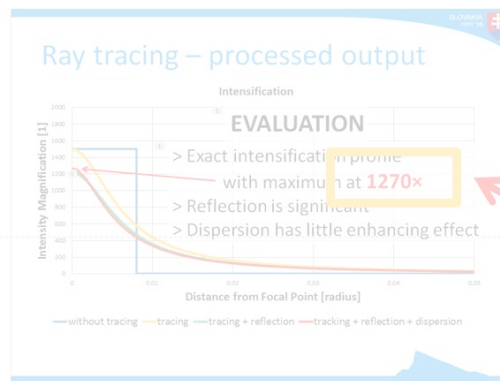
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Conclusion

Section 1



Ray tracing vs. accurate measurement



99% correlation!

Lost power

$$P_{losses}(T) = (1 - \epsilon)P_{incoming} + c\nabla T A + h \Delta T S + \sigma \epsilon S T^4$$

Reflection term

Conduction and convection term

Radiation term

Time evolution of temperature

$$mk \frac{dT}{dt} = (1 - \epsilon)I_{in}S + T_0 \left(c \frac{A}{l} + hS \right) - \left(c \frac{A}{l} + hS \right) T - \sigma \epsilon S T^4$$

Change in internal energy

Net power input

Heat dissipated to surroundings by...

conduction

convection

Power dissipated by radiation

Measurements

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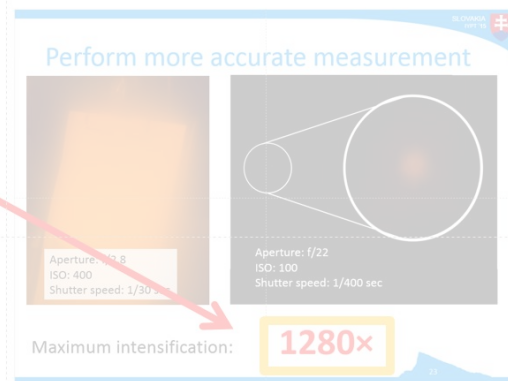
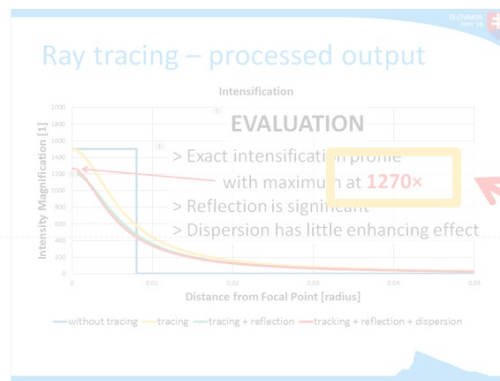
CONFIRMED BY AN EXPERIMENT

Section 2

Conclusion



Ray tracing vs. accurate measurement



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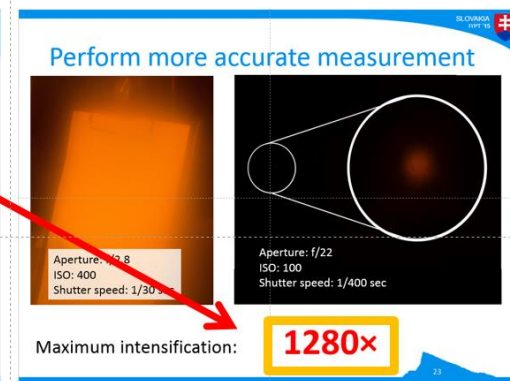
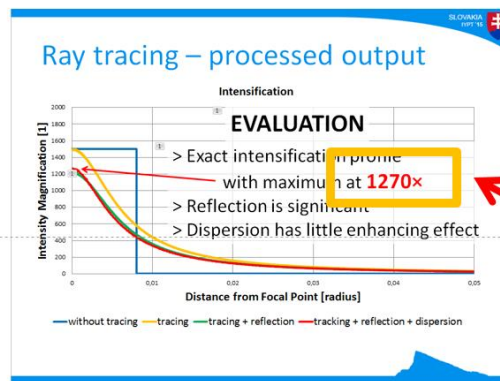
melted

CONFIRMED BY AN EXPERIMENT

Conclusion



Ray tracing vs. accurate measurement



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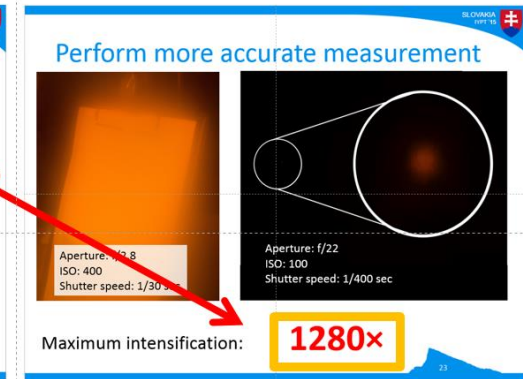
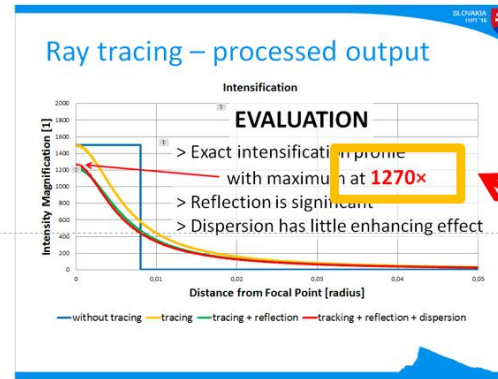
melted

CONFIRMED BY AN EXPERIMENT

Conclusion



Ray tracing vs. accurate measurement



99% correlation!

Lost power

$$P_{losses}(T) = (1 - \epsilon)P_{incoming} + c\sqrt{TA} + h\Delta TS + \sigma\epsilon ST^4$$

Reflection term

Conduction and convection term

Radiation term

Time evolution of temperature

$$mk \frac{dT}{dt} = (1 - \epsilon)I_{in}S + T_0 \left(c \frac{A}{l} + hS \right) - \left(c \frac{A}{l} + hS \right) T - \sigma\epsilon ST^4$$

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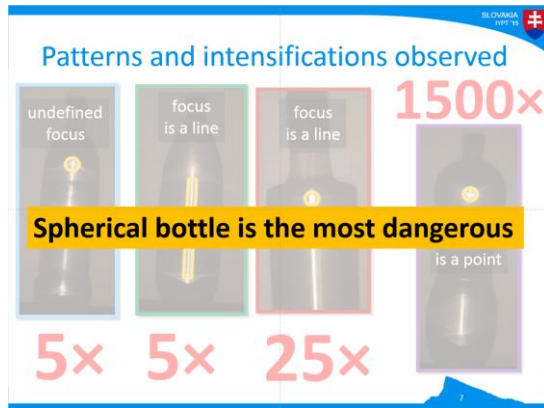
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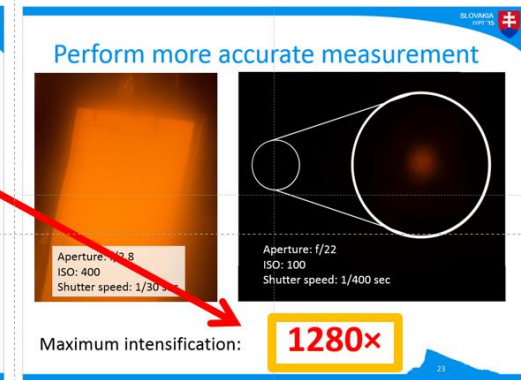
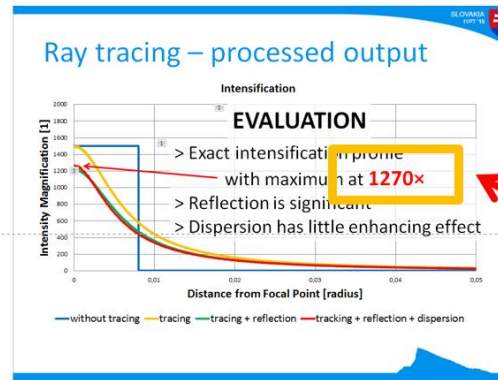
melted

CONFIRMED BY AN EXPERIMENT

Conclusion



Ray tracing vs. accurate measurement



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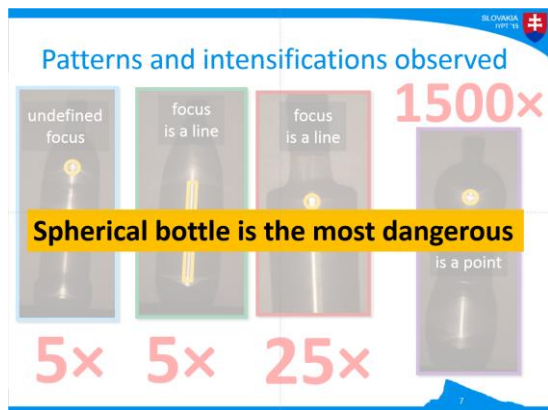
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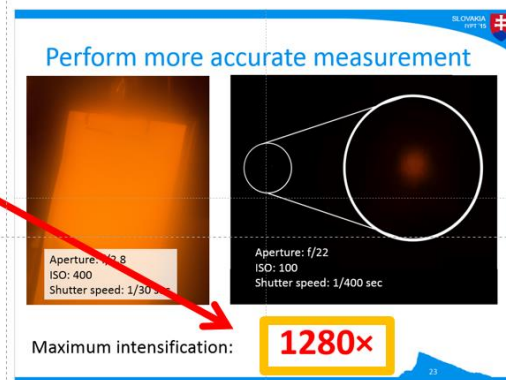
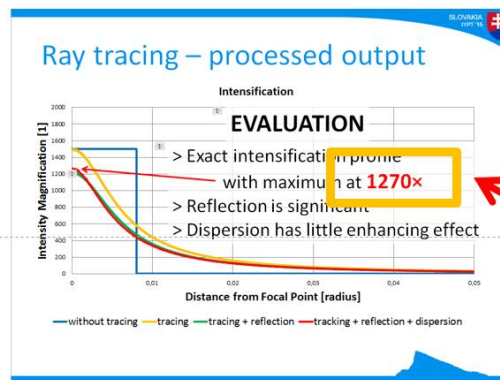
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CONFIRMED BY AN EXPERIMENT

Conclusion



Ray tracing vs. accurate measurement



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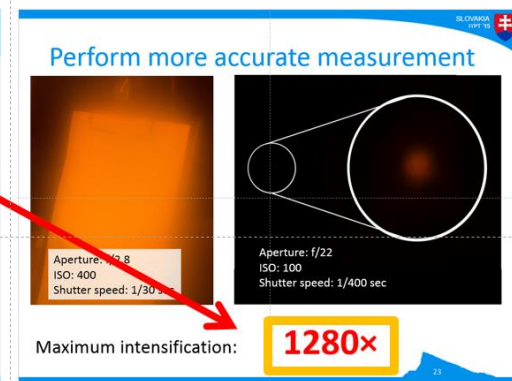
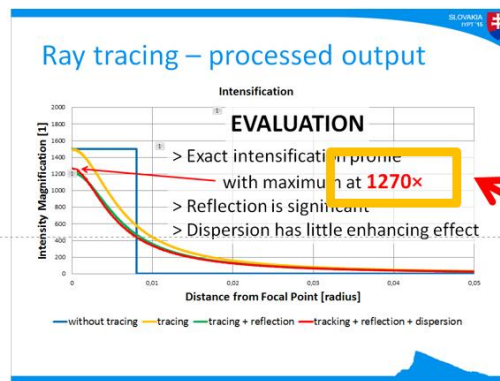
melted

CONFIRMED BY AN EXPERIMENT

Thank you for your attention!

surement

Section 1



99% correlation!

Lost power

$$P_{losses}(T) = (1 - \epsilon)P_{incoming} + c\nabla T A + h \Delta T S + \sigma \epsilon S T^4$$

Reflection term

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Net power input

Heat dissipated to surroundings by...

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Section 2

Measurements

Maximum for Brusnianska is $\sim 1\,280\,000\,W/m^2$
(depends on Sunlight intensity)

Bond paper (white)	1 500 000	scorched or burned
Dot matrix printing paper	175 000	
Cardboard	10 000	
Wood	14 000	
Black scarf (100% polyacryl)	4 000	melted
Thin blue plastic bag (polyethylen)	3 000	

CONFIRMED BY AN EXPERIMENT

A blue silhouette of a mountain range with several peaks of varying heights, spanning the width of the slide.

THANK YOU FOR YOUR ATTENTION!

Martin Murin



APPENDICES



Appendix A: Derivation of intensification

Power is conserved

$$I \times S_{image} = k I_0 \times S_{lens}$$

$$I = k I_0 \frac{S_{lens}}{S_{image}}$$

$$S_{image} = S_{sol} \times magnification^2$$

$$I = k I_0 \frac{S_{lens}}{S_{sol} M^2}$$

$$S_{sol} = 1.52 \times 10^{18} \text{ m}^2 \quad magnification = \left(\frac{h'}{h} = \frac{a'}{a} = \frac{\frac{fa}{f-a}}{a} = \frac{f}{f-a} \right) = \frac{f}{f-d_{sol}}$$

$$I = k I_0 \frac{S_{lens}}{S_{sol} \left(\frac{f}{f-d_{sol}} \right)^2} \quad \Rightarrow \quad I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$

Appendix B: Different liquids in bottle

- The only relevant optical property of liquid is the index of refraction

“Lensmaker’s equation”

$$\frac{1}{f} = (n - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} + \frac{(n - 1)d}{nR_1R_2} \right] \quad (\text{for sphere})$$

- The smaller the focal length, the smaller the magnification

$$\begin{aligned} \text{image area} &= \text{Solar area} \times \text{magnification}^2 \\ \text{magnification} &= \frac{f}{f - d_{sol}} \end{aligned}$$

- The smaller the magnification, the higher the intensity

$$I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$

Appendix B: Different liquids in bottle

- The only relevant optical property of liquid is the index of refraction

“Lensmaker’s equation”

$$\frac{1}{f} = (n - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} + \frac{(n - 1)d}{nR_1R_2} \right] \longrightarrow f = \frac{nR}{2n - 2} \quad (\text{for sphere})$$

- The smaller the focal length, the smaller the magnification

$$\begin{aligned} \text{image area} &= \text{Solar area} \times \text{magnification}^2 \\ \text{magnification} &= \frac{f}{f - d_{sol}} \end{aligned}$$

- The smaller the magnification, the higher the intensity

$$I = k I_0 \frac{S_{lens}}{S_{sol}} \frac{d_{sol}^2}{f^2}$$

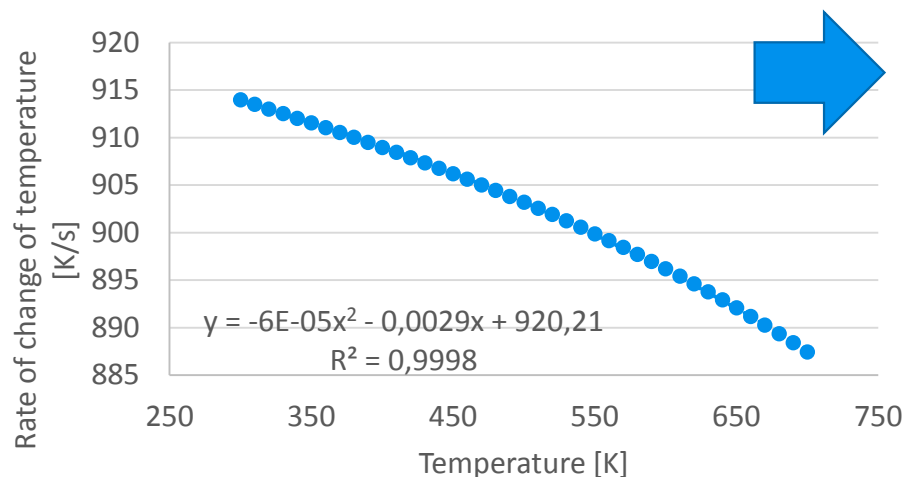
Appendix C: Time evolution of temperature

$$mk \frac{dT}{dt} = (1 - \epsilon) I_{in} S + \left(c \frac{S}{l} + hS \right) \Delta T - \sigma \epsilon S T^4$$

Using constants for ignition of wood

$\epsilon = 0.5$	$I_{in} = 1000 \frac{W}{m^2}$	$T_0 = 300 \text{ K}$	$c = 0.05 \frac{W}{m \text{ K}}$
$\sigma = 5.67 \times 10^{-8} \frac{W}{m^2 \text{ K}^4}$	$k = 2000 \frac{J}{kg \text{ K}}$	$S = 10^{-6} m^2$	$h = 20 \frac{W}{m^2 \text{ K}}$
$m = 7 \times 10^{-7} kg$		$l = 5 \times 10^{-4} m$	

Plotted relation



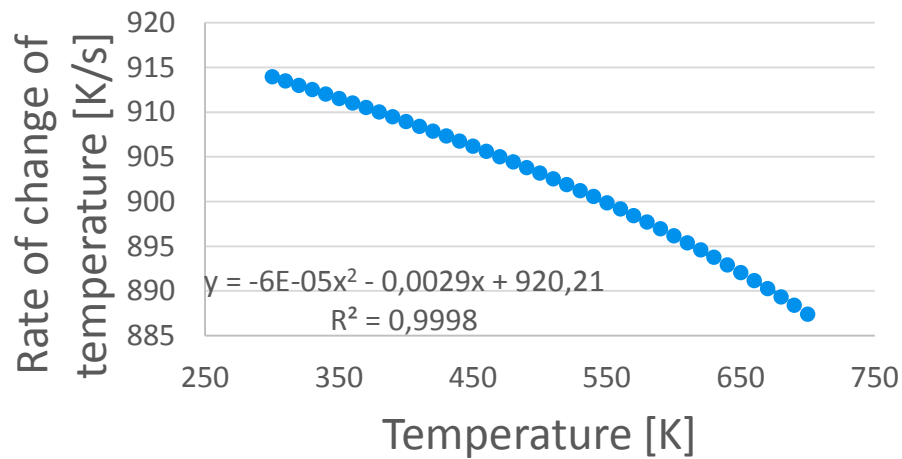
$$\frac{dT}{dt} = -6 \times 10^{-5} T^2 - 2.9 \times 10^{-3} T + 920.21$$

$$T = \frac{-3379.95 + 3940.47 e^{0.47 t}}{0.868404 + e^{0.47 t}}$$

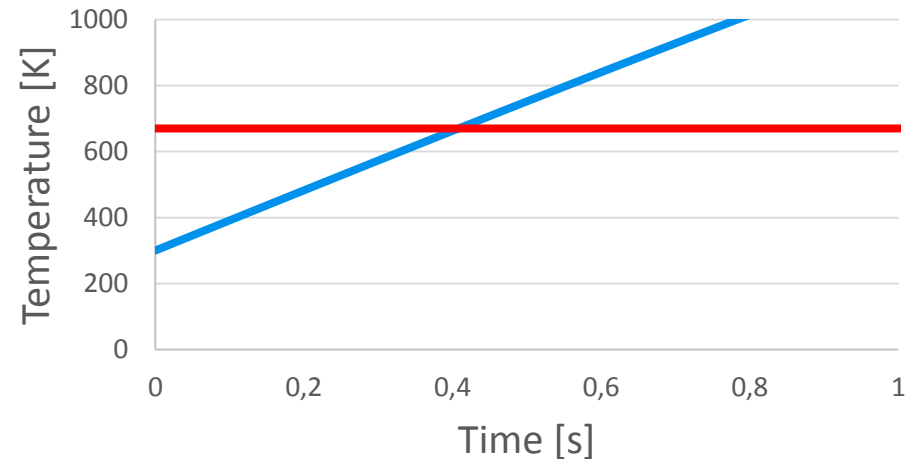
Appendix C: Time evolution of temperature

$$mk \frac{dT}{dt} = (1 - \epsilon) I_{in} S + T_0 \left(c \frac{A}{l} + hS \right) - \left(c \frac{A}{l} + hS \right) T - \sigma \epsilon S T^4$$

Plotted relation



Temperature of wood



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$$\frac{dT}{dt} = -6 \times 10^{-5} T^2 - 2.9 \times 10^{-3} T + 920.21$$



$$T = \frac{-3379.95 + 3940.47 e^{0.47 t}}{0.868404 + e^{0.47 t}}$$

Appendix D: Used materials – dot matrix paper



Appendix E: Experiments – conditions during critical intensity measurement

Lens parameters:

focal length		0.216 ± 0.004 m
radius of curvature	0.137 m	
lens radius	0.073 m	
index of refraction*	1.517	* crown glass, 589 nm, encyclopedia Britannica

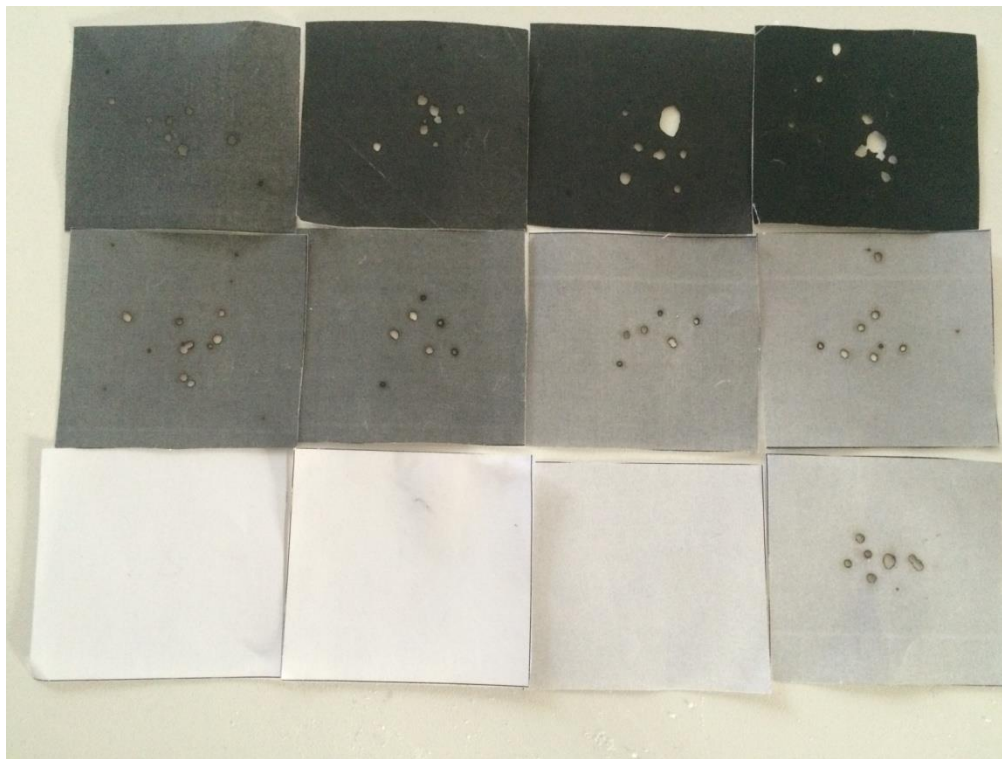
Measurement data:

date and time	6 th January 2015 at 12:00 - 13:00
weather	sunny, no clouds
sunlight intensity [W/m ²]	<u>380 (Bratislava airport)</u> , 330 (Koliba)

Position of the Sun

altitude	12:10	19° 16' 37''
	12:30	18° 59' 57''
	13:00	17° 59' 47''
apparent diameter		00° 32' 32"
Solar diameter		1.391×10^9 m
distance from Earth		$0.98328 \text{ AU} = 1.47097 \times 10^{11}$ m

Appendix E: Experiments – time vs albedo



Round bottom boiling flask



$$r = 4.2 \text{ cm}$$

Paper with different color (albedo) measured by albedometer

Appendix F: Light intensity ratio from a photo

1. Capture in RAW format
2. Convert to TIFF using *dcraw** program
 - *No color interpolations, compression, white balance...*
3. Set linear colorspace in Photoshop
4. Open linear TIFF in PS canceling any suggestions for “improvements”
5. Read RGB values and compare them within one image
6. Try different exposition times and verify that 2x longer exposition gives 2x greater RGB values

Appendix G: Visual data – caustic curve

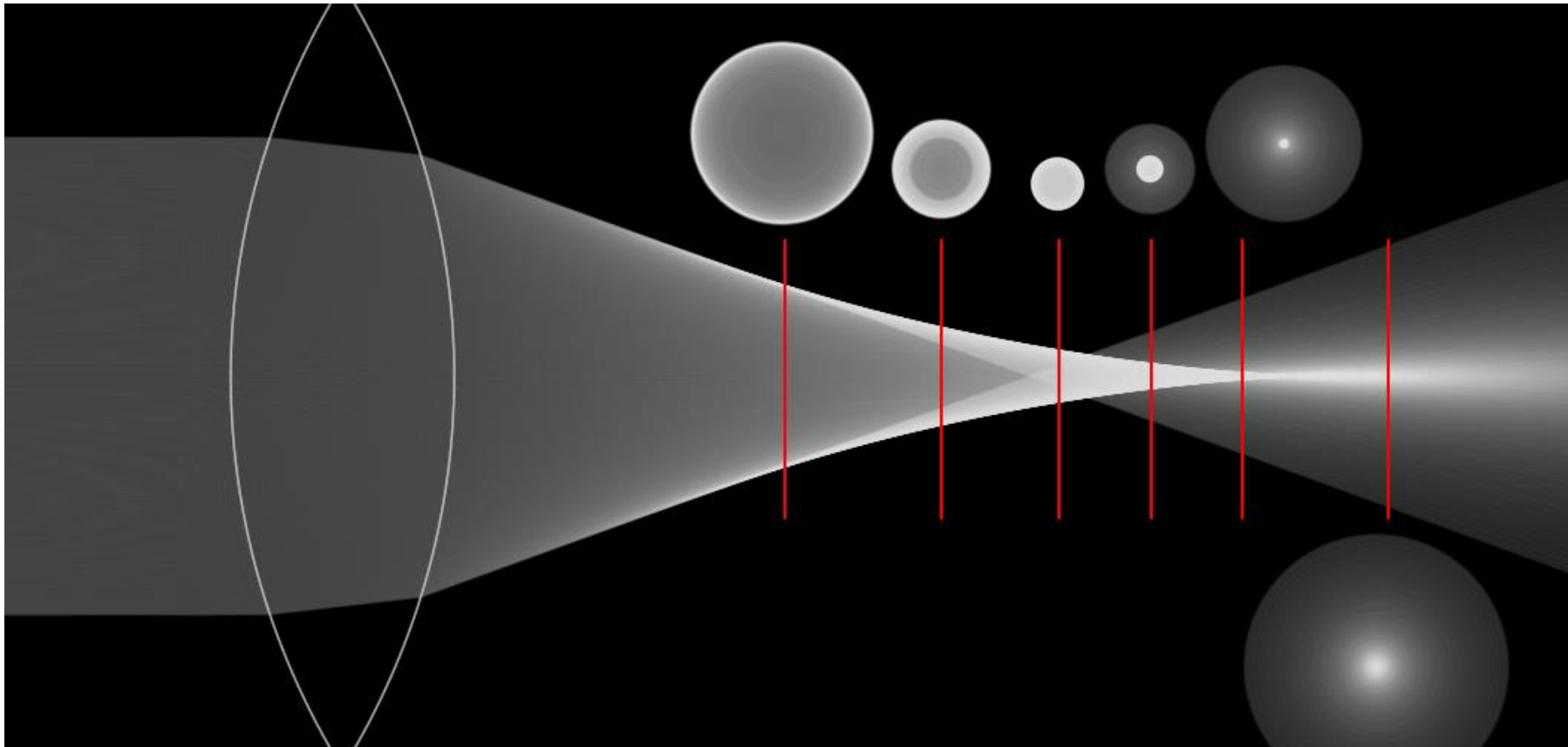
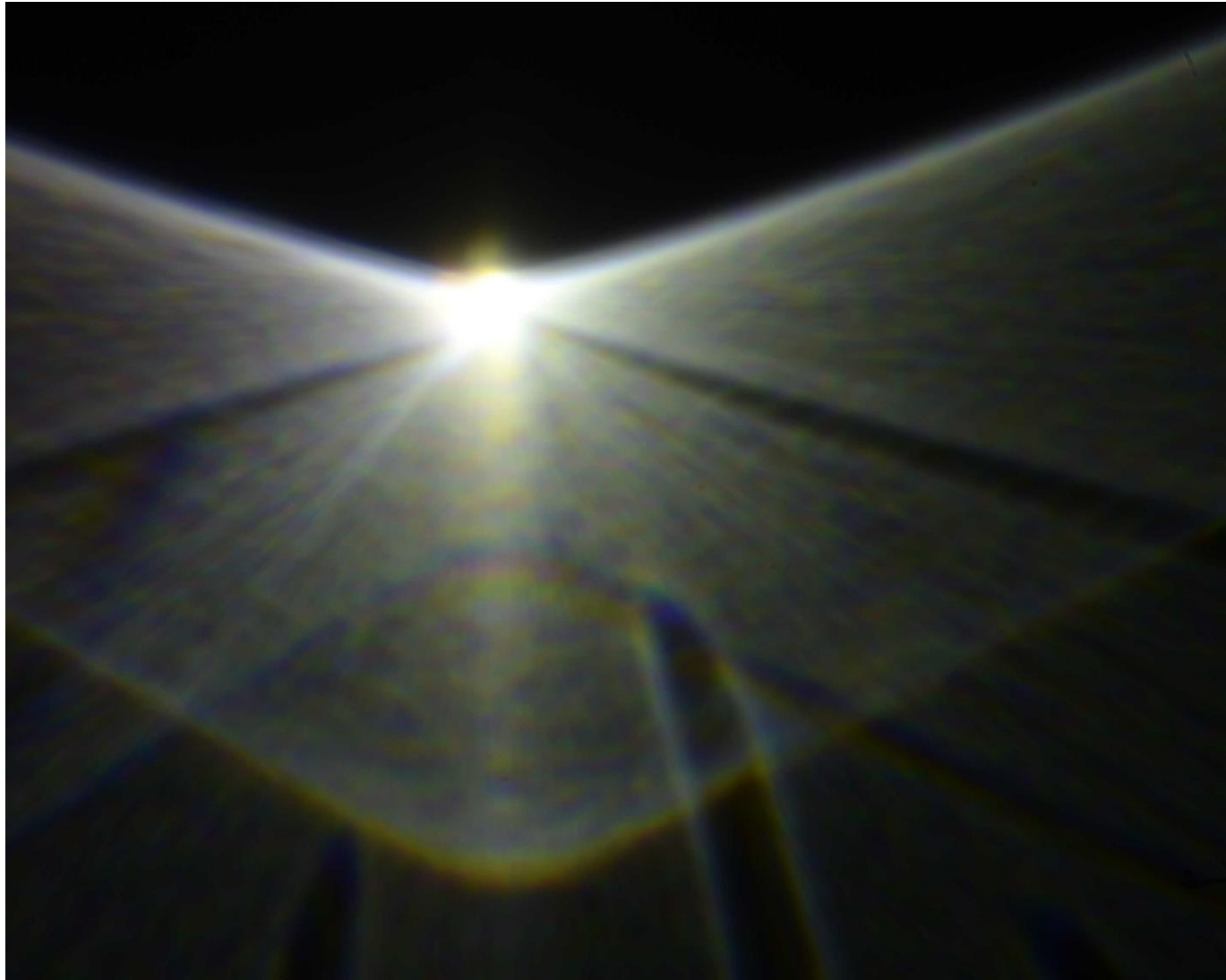
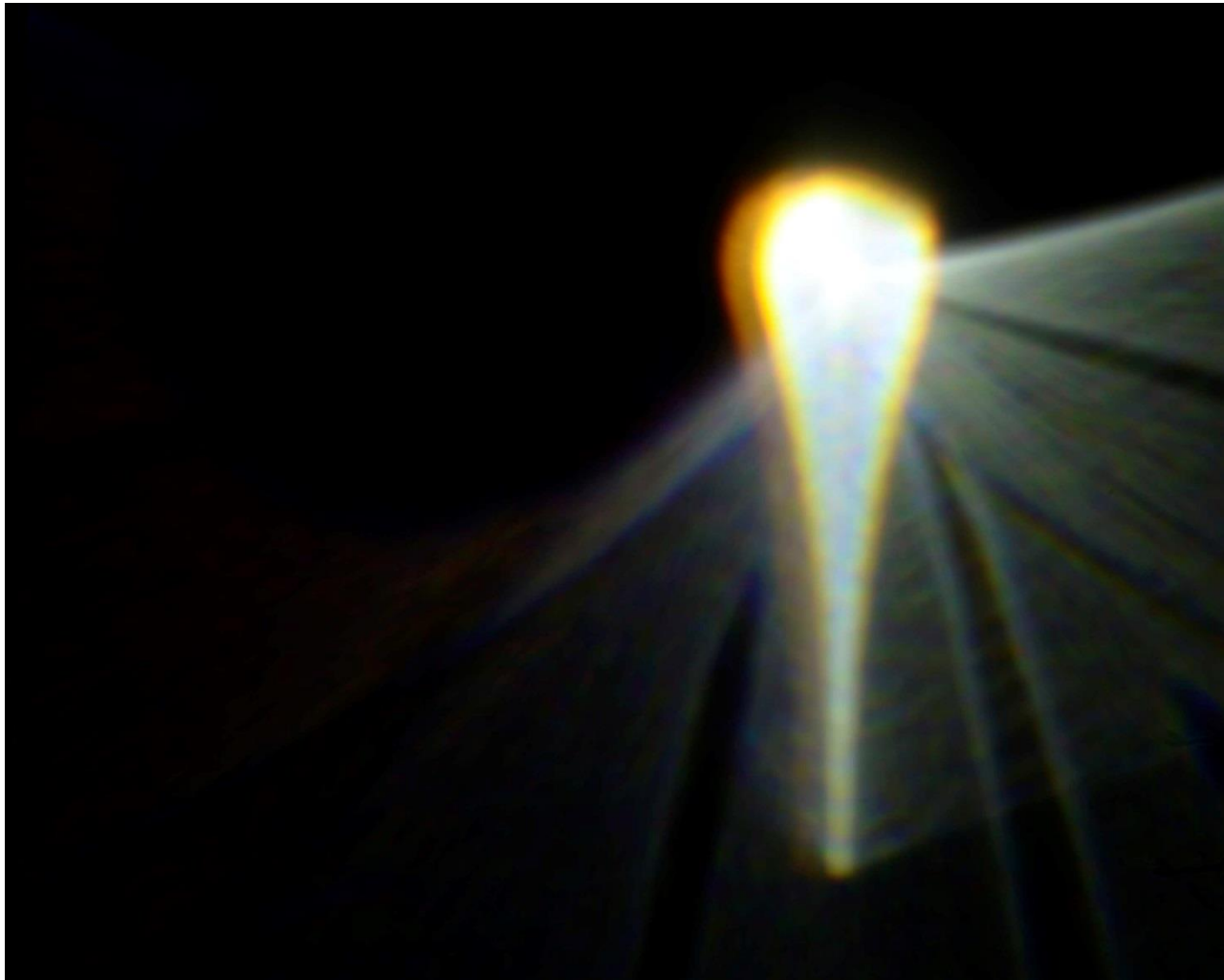


Image courtesy of Jakub Trávník at <http://jtra.cz>

Appendix G: Visual data – focused light on CMOS



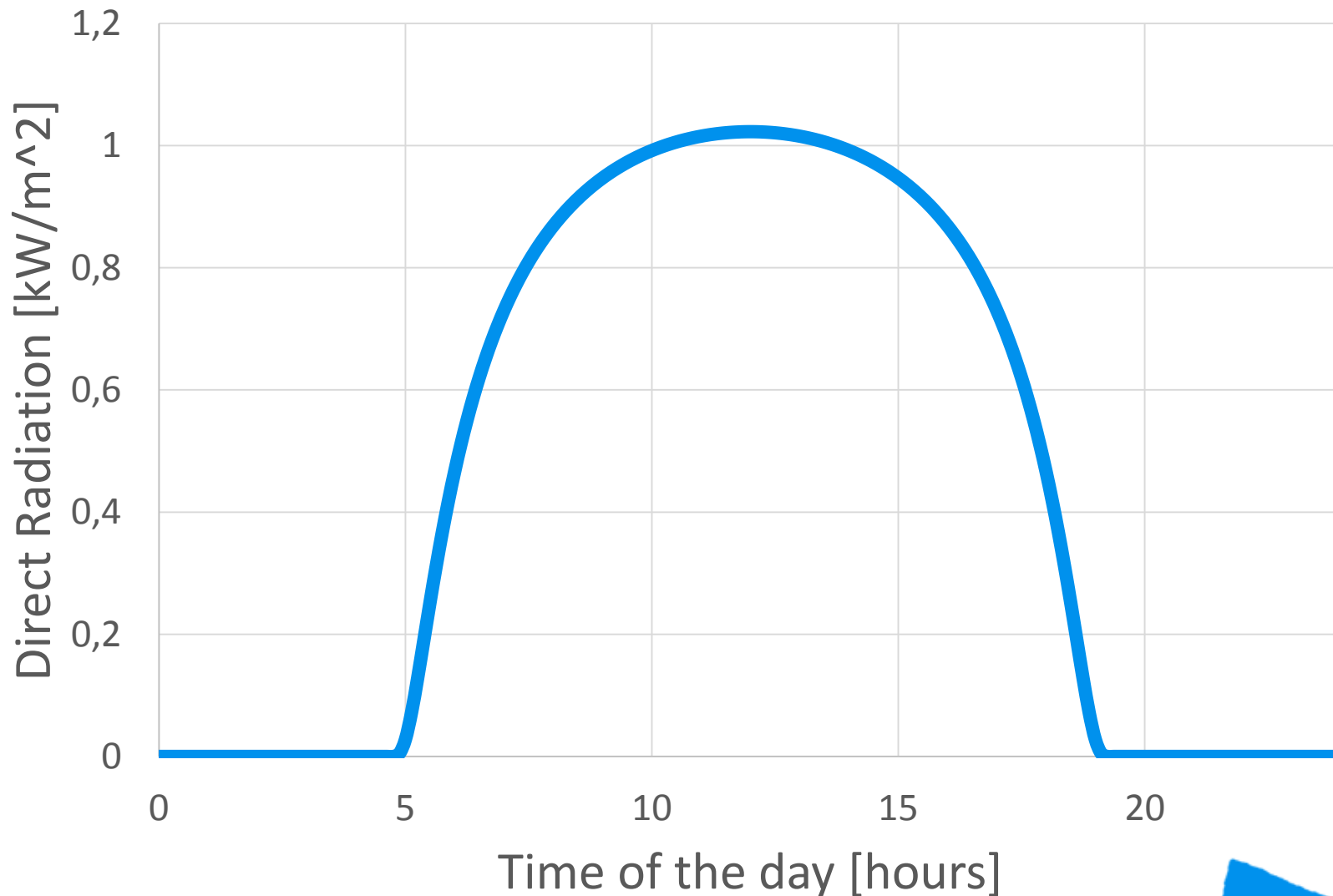
Appendix G: Visual data – focused light on CMOS (comma aberration)



Appendix H: Additional data – electromagnetic absorption by water



Appendix H: Additional data – intensity of solar irradiance during the day

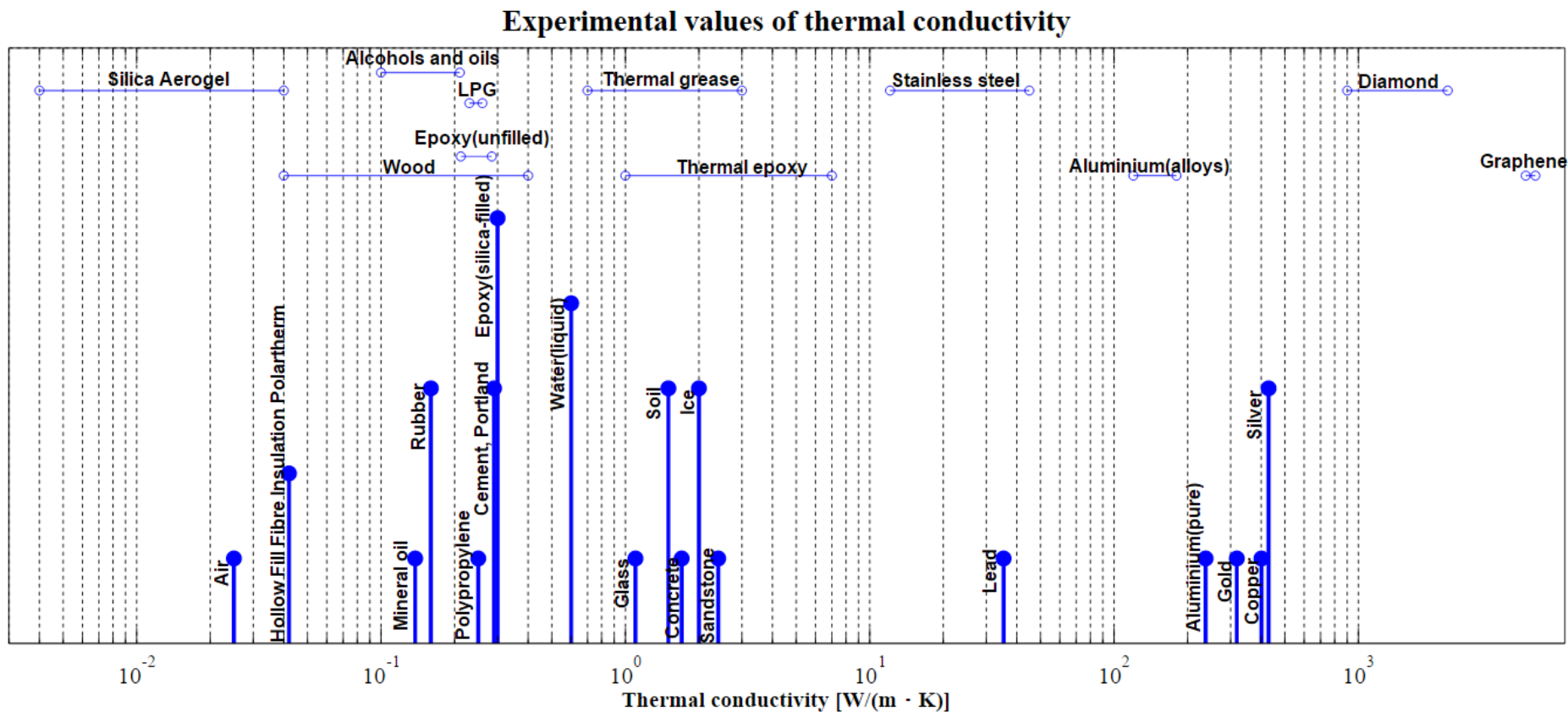


Appendix H: Additional data – ignition data

Table 2 Ignition data (present study).

Species (Density, g/cm ³)	Heat flux (kW/m ²)	Average T _{ig} (°C)	Standard deviation	Plateau Temp. (°C)	Standard deviation	Average t _{ig} (s)	Standard deviation	No. of Samples Tested
Mahogany (0.54)	15.4	465	21	365	3	850	80	7
	19.7	427	14	385	3	324	39	7
	24.0	364	8	-	-	90	7	8
	28.7	360	6	-	-	60	7	7
	31.7	353	10	-	-	38	4	9
Western Red Cedar (0.28)	15.4	450	19	366	1	583	95	6
	19.7	431	12	379	8	216	29	8
	24.0	365	4	-	-	57	8	7
	28.7	346	6	-	-	30	3	9
	31.7	354	7	-	-	23	1	8
Obeche (0.35)	15.4	497	74	359	7	684	121	9
	19.7	442	30	361	18	176	39	7
	24.0	364	8	-	-	60	5	6
	28.7	344	14	-	-	39	4	8
	31.7	340	12	-	-	29	3	8
White Pine (0.36)	15.4	446	13	354	4	1094	162	8
	19.7	411	25	380	11	257	69	11
	24.0	397	3	-	-	95	18	7
	28.7	387	4	-	-	48	4	7
	31.7	375	17	-	-	32	3	9

Appendix H: Additional data – thermal conductivities





Appendix H: Additional data – Fresnel equations

$$t_p = \frac{2n_1 \cos(\theta_i)}{n_1 \cos(\theta_t) + n_2 \cos(\theta_i)}$$

$$r_s = \frac{n_1 \cos(\theta_i) - n_2 \cos(\theta_t)}{n_1 \cos(\theta_i) + n_2 \cos(\theta_t)}$$

$$t_s = \frac{2n_1 \cos(\theta_i)}{n_1 \cos(\theta_i) + n_2 \cos(\theta_t)}$$

$$r_p = \frac{n_2 \cos(\theta_i) - n_1 \cos(\theta_t)}{n_1 \cos(\theta_t) + n_2 \cos(\theta_i)}$$