## Allometry

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## Problem

How do length and thickness of bones scale with overall size of animal ?


A study about the growth of body parts at different rates, resulting in a change of body proportions.

## Proportions



$$
\frac{2}{3}=\frac{4}{6} \quad \frac{5}{15}=\frac{1}{3}
$$

## Proportions

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## Proportions



## What Is Allometric Growth

## ?

- Pattern of growth
- $Y=b x^{\wedge} a$
- $Y=$ mass of an organ

- $X=$ mass of the organism
- a = slope
- $\mathrm{b}=\mathrm{a}$ constant



## What Is Allometric Scaling?

- $\mathrm{Y}=\mathrm{aM}^{\wedge} \mathrm{b}$
- $\log y=\log a+b^{*} \log m$
- Y = biological variable
- $M=$ measure of a body size
- $\mathrm{b}=$ scaling exponent
- Presented in logarithmic




## Kinds of Allometry (1)

## Positive Allometry

## Negative Allometry

( | $a>1$ |
| :--- |
| positive |
| allometry |
| $\ln (X)=X^{\prime}$ |
| Yositive Allometry: |
| relative to $X$ |

ln

## Kinds of Allometry (2)



## Independence

## Inverse Allometry

## Isometric Growth

- Opposite of Allometric growth
- Animal's body parts grow at the same rate
- Unchange proportions



# Relationship Between Thickness of an ANIMAL Bone to the Overall Mass 



## Elephant

## Mouse

## MY Experiment

- To test the relationship between height and weight of human to the overall surface area
- Variable tested :

1. Height (Independent)
2. Weight (Independent)
3. Surface area (Dependent)

Relationship Between Height and Weight of Human to the Overall Surface

| No. | Height (cm) | Area <br> Weight $(\mathrm{kg})$ | Surface Area (m2) |
| :---: | :---: | :---: | :---: |
| 1 | 158 | 34 | 1.51 |
| 2 | 155 | 42 | 1.81 |
| 3 | 146 | 45 | 1.81 |
| 4 | 154 | 39 | 1.67 |
| 5 | 156 | 61 | 2.66 |
| 6 | 168 | 59 | 2.75 |
| 7 | 177 | 51 | 2.51 |
| 8 | 162 | 68 | 3.06 |
| 9 | 158 | 53 | 2.34 |


| 10 | 147 | 42 | 1.72 |
| :--- | :--- | :--- | :--- |
| 11 | 160 | 43 | 1.93 |
| 12 | 162 | 44 | 1.98 |
| 13 | 157 | 40 | 1.74 |
| 14 | 162 | 44 | 1.97 |
| 15 | 142 | 28 | 1.11 |
| 16 | 159 | 56 | 2.47 |
| 17 | 162 | 49 | 2.21 |
| 18 | 162 | 43 | 1.93 |
| 19 | 156 | 47 | 2.04 |
| 20 | 149 | 36 | 2.96 |
| 21 | 142 | 42 | 1.64 |
| 22 | 160 | 59 | 2.62 |
| 23 | 155 | 38 | 1.65 |
| 24 | 173 | 63 | 3.03 |

## Average

| Height (cm) | Weight (kg) | Surface Area (m2) |
| :---: | :---: | :---: |
| 157.56 | 46.93 | 2.13 |

## Variables

| No. | Variables | Height (cm) | Weight (kg) | Surface Area (m2) |
| :---: | :---: | :---: | :---: | :---: |
| 1. | The Tallest | 177 | 51 | 2.51 |
| 2. | The Shortest | 1. 142 <br> 2. 142 | $\begin{aligned} & 28 \\ & 42 \end{aligned}$ | $\begin{aligned} & 1.11 \\ & 1.64 \end{aligned}$ |
| 3. | The Heaviest | 162 | 68 | 3.06 |
| 4. | The Lightest | 142 | 28 | 1.11 |
| 5. | The Widest (Body Surface) | 162 | 68 | 3.06 |
| 6. | The Smallest (Body Surface) | 142 | 28 | 1.11 |

## Conclusion (1)

- Allometry = change body proportions
- Allometric >< Isometric
- Proportions : 2 equal fractions
- Size bone proportions
- Positive allometry >< Negative Allometry
- Isometry = Neutral = (b=1)
- Negative Allometry, Independence, And Inverse Allometry ( $b<0$ )
- Positive Allometry (b>1)


## Conclusion (2)

- Height + Weight = Surface Area
- Height + Weight = Surface Area
- Height + Weight = Height + Weight
- Allometric scaling equation :

1. Exponensial : $\mathrm{Y}=\mathrm{aM} \wedge^{\wedge} \mathrm{b}$
2. Logarithmic $: \log y=\log a+b^{*} \log m$

- Allometric growth equation :

1. $Y=b x^{\wedge} a$

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